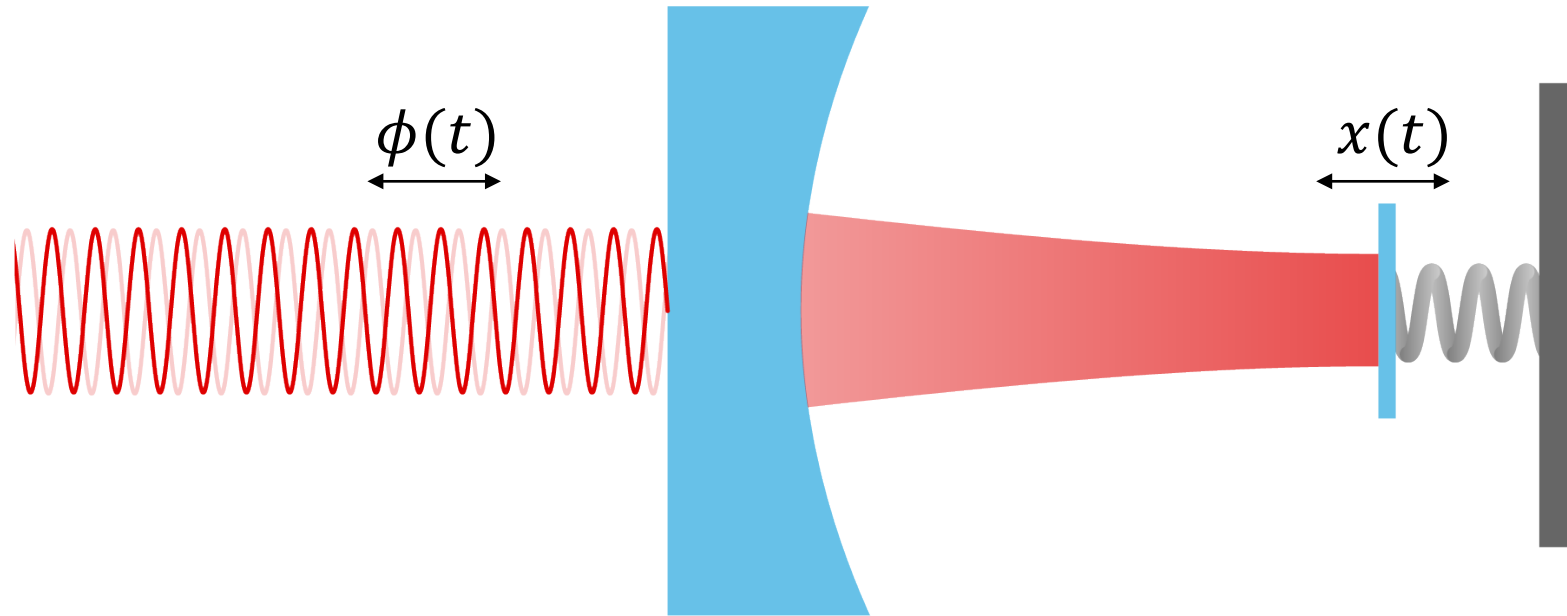


# Ultracoherent mechanical resonators for quantum optomechanics

Nils J. Engelsen, Sergey A. Fedorov, Mohammad J. Beryehi, Amir H. Ghadimi, Amirali Arabmoheghi, Alberto Beccari, Ryan Schilling, Dalziel J. Wilson, Tobias J. Kippenberg  
Laboratory of Photonics and Quantum Measurements – EPFL, Switzerland

# An idealized optomechanical system



- Mechanical oscillator position maps onto phase shift of light
- Radiation pressure from the light interacts with mechanical oscillator
- Cavity enhances interaction strength

M. Aspelmeyer, T. J. Kippenberg and F. Marquardt, *Rev. Mod. Phys.* **86**, 1391

# History of optomechanics

## Quantum-Mechanical Radiation-Pressure Fluctuations in an Interferometer

Carlton M. Caves

*W. K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125*  
(Received 29 January 1980)

The interferometers now being developed to detect gravitational waves work by measuring small changes in the positions of free masses. There has been a controversy whether quantum-mechanical radiation-pressure fluctuations disturb this measurement. This Letter resolves the controversy: They do.



The idea of light exerting pressure has existed since Kepler (comet tails)

Late 1960s: Seminal papers from Braginsky explore effects of radiation pressure on mechanical resonators

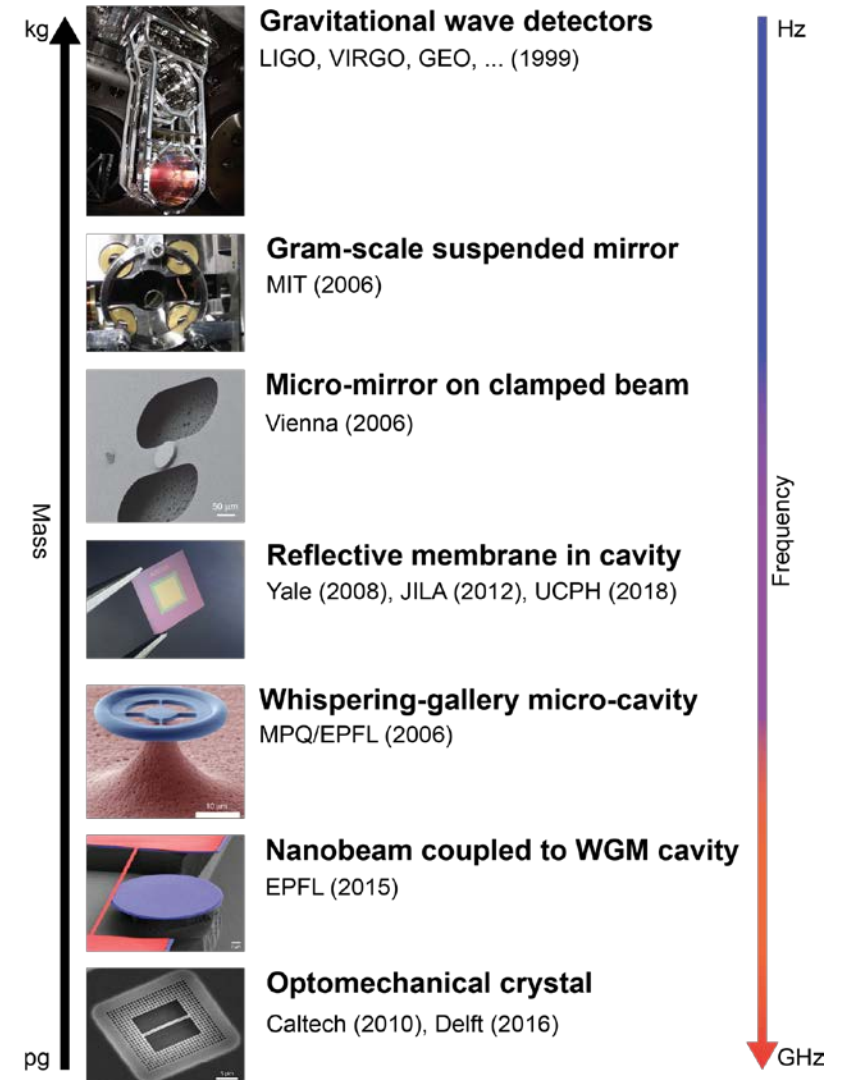
1980: First large interferometers (40m) built by Caltech

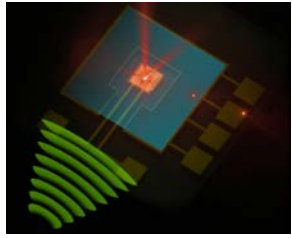
# Rise of modern optomechanics

2000s: Techniques are developed to control mechanics with light

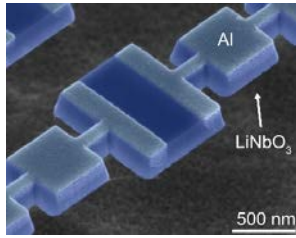
2010: First cooling to the quantum ground state of (macroscopic) mechanical resonators

2010s: Coupling to different systems, development of protocols for generating entanglement etc

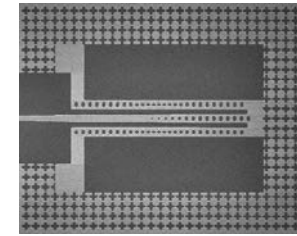




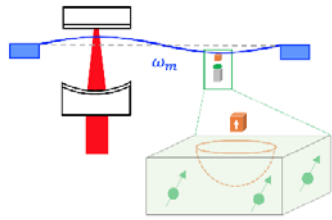
**Optical RF detection**  
Bagci et al., Nature (2014)



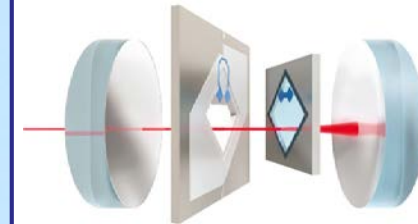
**Quantum networking**  
Arrangoiz-Arriola et al.,  
arXiv:1902.04681 (2019)



**Quantum memory**  
MacCabe et al.,  
arXiv:1901.04129 (2019)

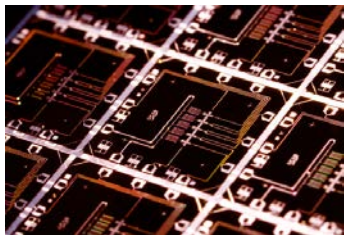


**Spin detection (MRFM)**  
Fischer et al., NJP (2019)

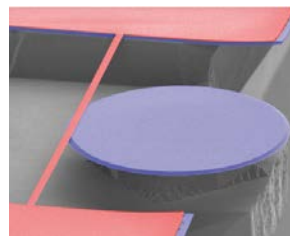


**Low noise microwave-to-optical conversion**  
Higginbotham et al., Nat. Phys. (2017)

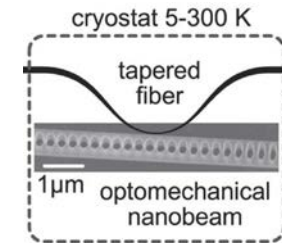
# Quantum technologies with optomechanics



**Coupling to qubits**  
Chu et al., Science 359, 6373 (2017)



**Room temperature optomechanics**  
Sudhir et al., Phys. Rev. X (2017)



**Quantum thermometry**  
Purdy et al., Science (2017)

# Introduction to optomechanical interaction

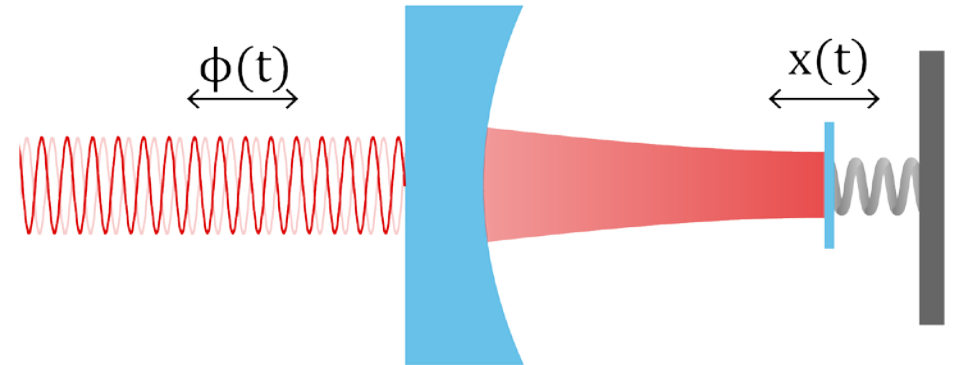
$$\hat{H}_0 = \hbar\omega_{\text{cav}}(x)\hat{a}^\dagger\hat{a} + \hbar\omega_m\hat{b}^\dagger\hat{b}$$

$$\omega_{\text{cav}}(x) = \omega_{\text{cav}} + x\partial\omega_{\text{cav}}/\partial x$$

$$\hbar\omega_{\text{cav}}(x)\hat{a}^\dagger\hat{a} \approx \hbar(\omega_{\text{cav}} - G\hat{x})\hat{a}^\dagger\hat{a}, \text{ where } G = -\partial\omega_{\text{cav}}/\partial x$$

$$\hat{x} = x_{\text{ZPF}}(\hat{b} + \hat{b}^\dagger), g_0 = Gx_{\text{ZPF}}$$

$$\hat{H} = -\hbar\Delta\hat{a}^\dagger\hat{a} + \hbar\omega_m\hat{b}^\dagger\hat{b} - \hbar g_0\hat{a}^\dagger\hat{a}(\hat{b} + \hat{b}^\dagger) \quad \Delta = \omega_L - \omega_{\text{cav}}$$



# A realistic optomechanical system

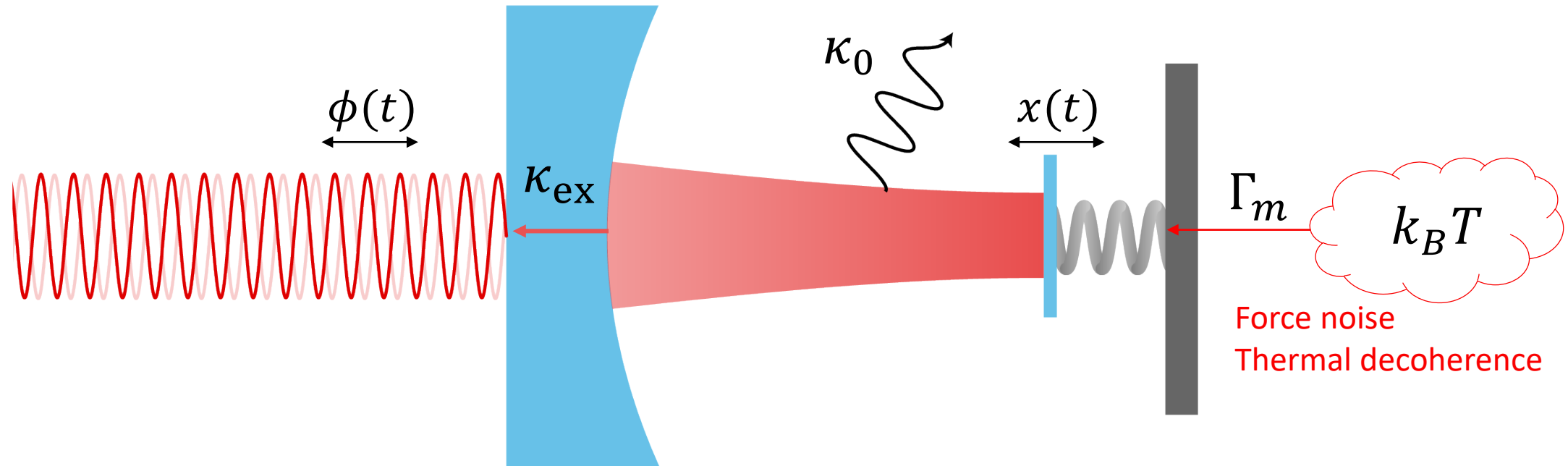


Figure of merit for optomechanical system (single-photon cooperativity):  $C_0 = \frac{4g_0^2}{\kappa\Gamma_m}$

# Equations of motion for optomechanical systems

$$\dot{\hat{a}} = -\frac{\kappa}{2}\hat{a} + i(\Delta + G\hat{x})\hat{a} + \sqrt{\kappa_{ex}}\hat{a}_{in} + \sqrt{\kappa_0}\hat{a}_{vac}$$

Cavity loss

Cavity-laser  
detuningOptomechanical  
interactionCavity driving  
termVacuum  
fluctuations

$$\dot{\hat{b}} = \left(-\frac{\Gamma_m}{2} - i\Omega_m\right)\hat{b} + ig_0\hat{a}^\dagger\hat{a} + \sqrt{\Gamma_m}\hat{b}_{in}$$

Mechanical loss

Optomechanical  
interaction

Thermal bath



# Linearized Hamiltonian and equations of motion

- Consider a steady-state solution where we set  $\hat{a} = \bar{\alpha} + \delta\hat{a}$ , where  $\bar{\alpha} = \sqrt{n_{cav}}$ , to get:

$$H_{\text{int}} = -\hbar\sqrt{n_{cav}}g_0(\delta\hat{a} + \delta\hat{a}^\dagger)(\hat{b} + \hat{b}^\dagger)$$

- Hamiltonian is now linear in the field operators with an effective interaction strength  $g = \sqrt{n_{cav}}g_0$
- Linearized equations of motion:

$$\delta\dot{\hat{a}} = \left(-\frac{\kappa}{2} + i\Delta\right)\delta\hat{a} + ig(\hat{b} + \hat{b}^\dagger) + \sqrt{\kappa_{ex}}\delta\hat{a}_{\text{in}} + \sqrt{\kappa_0}\hat{a}_{\text{vac}}$$

$$\dot{\hat{b}} = \left(-\frac{\Gamma_m}{2} - i\Omega_m\right)\hat{b} + ig(\delta\hat{a} + \delta\hat{a}^\dagger) + \sqrt{\Gamma_m}\hat{b}_{\text{in}}$$

# Fundamental optomechanical interactions

- Can select different interactions with detuning

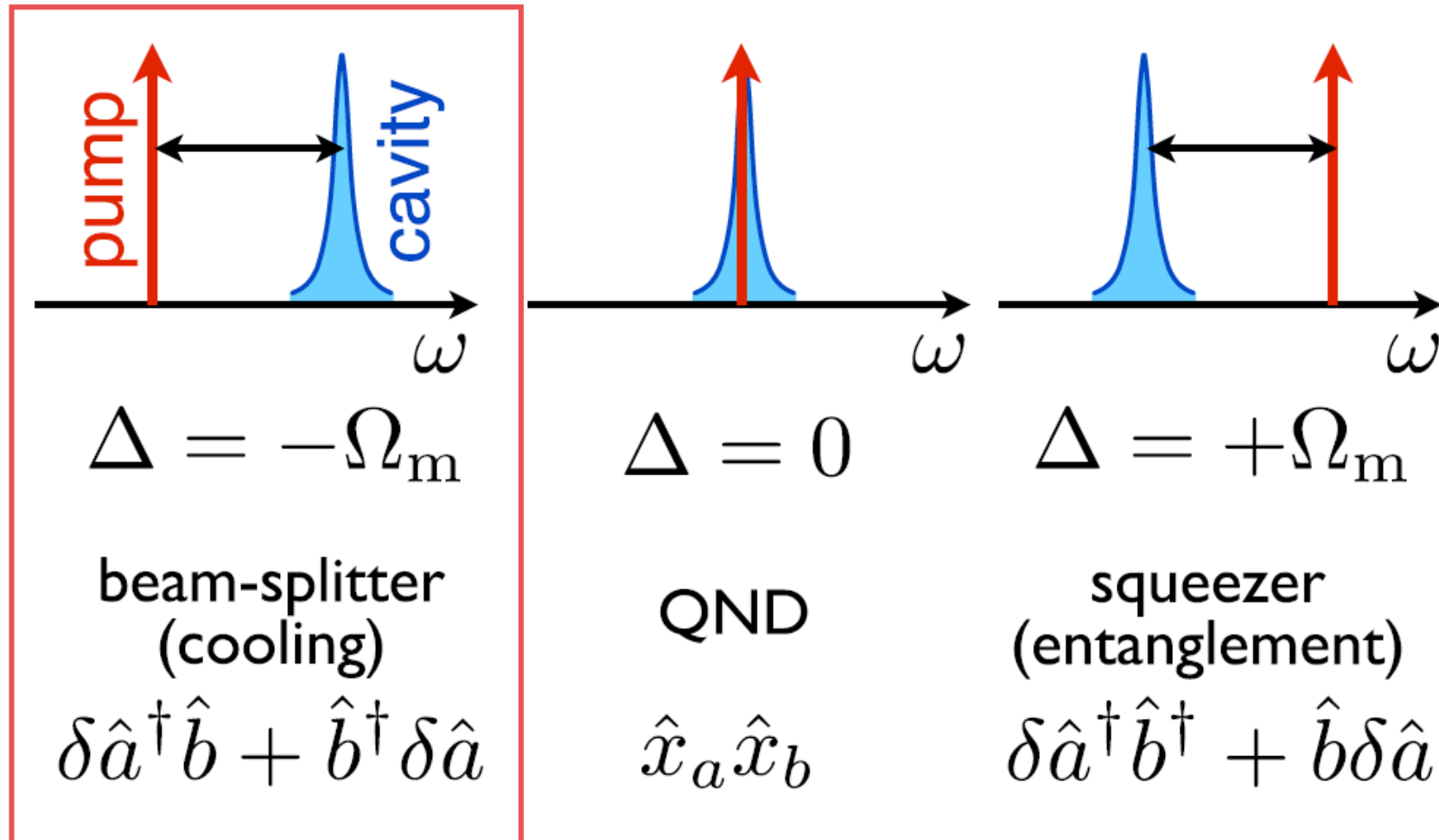


Figure from M. Aspelmeyer, T. J. Kippenberg and F. Marquardt, Rev. Mod. Phys. 86, 1391

# Dynamical backaction (cooling)

Interaction:  $-\hbar\sqrt{n_{\text{cav}}}g_0\hat{a}^\dagger\hat{b}$

Cooling rate:  $\Gamma_{\text{opt}} = n_{\text{cav}}C_0\Gamma_m$

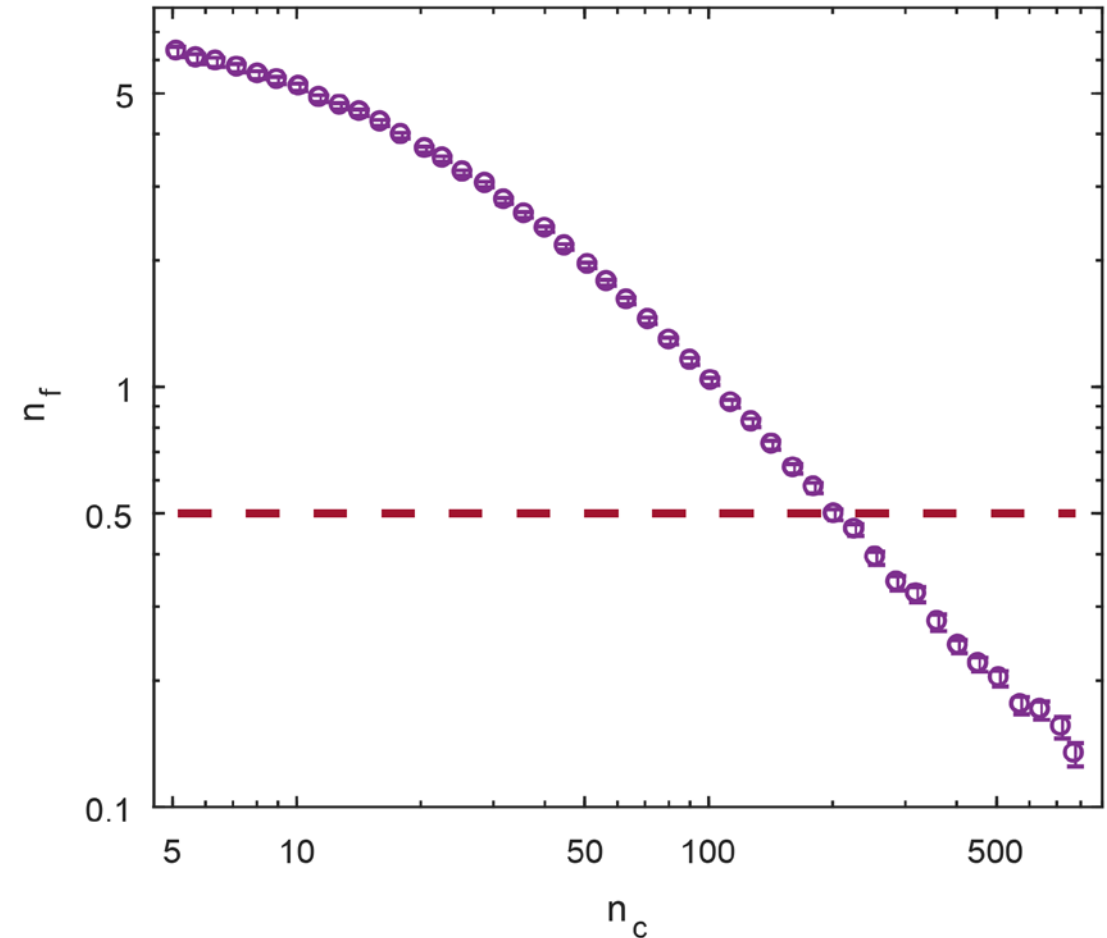
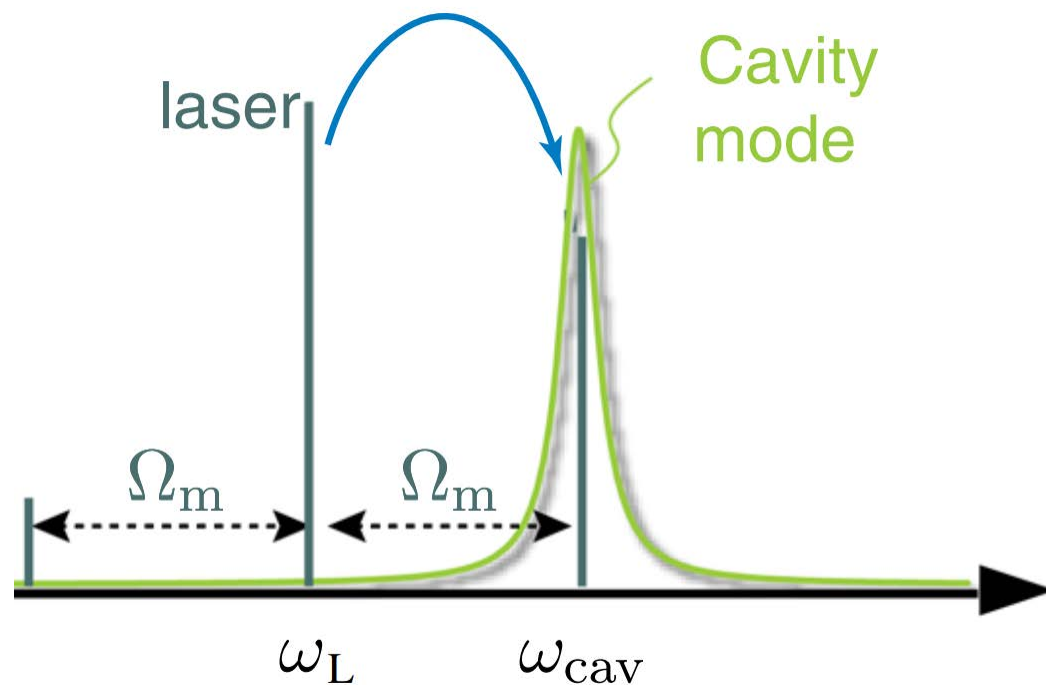


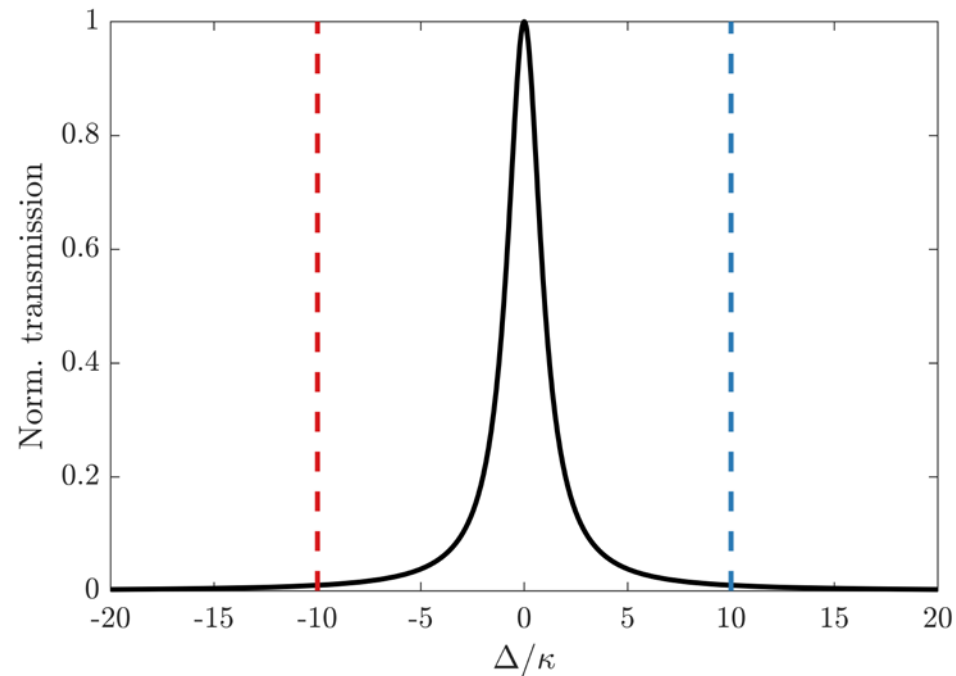
Figure from M. Aspelmeyer, T. J. Kippenberg and F. Marquardt, *Rev. Mod. Phys.* **86**, 1391

L. Qiu, I. Shomroni, T. J. Kippenberg (unpublished)

# Two regimes of optomechanics

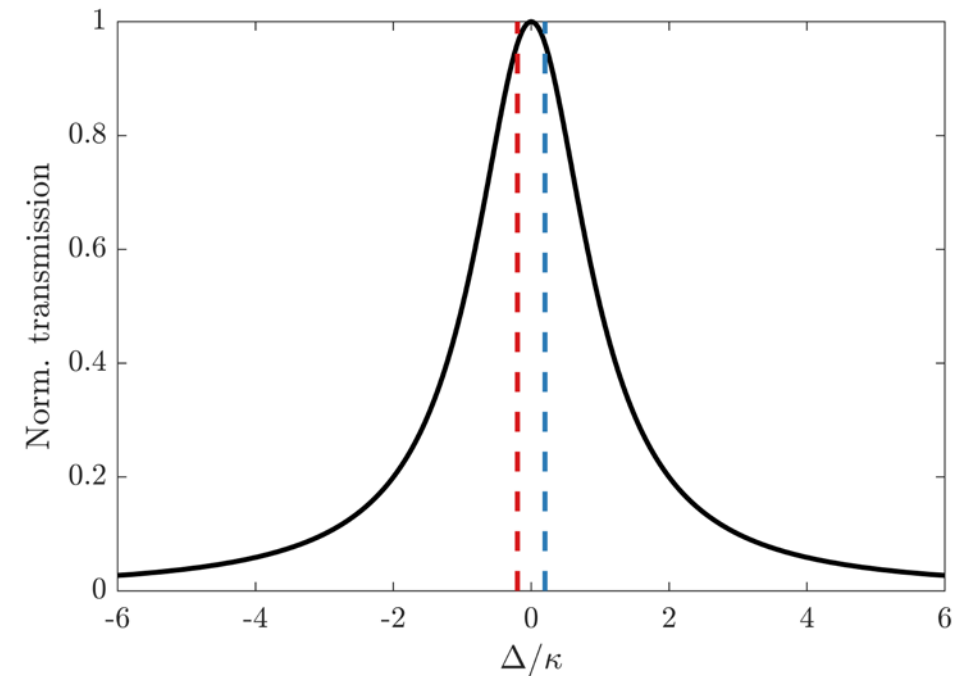
## Resolved sideband: $\omega_m \gg \kappa$

- Can be sideband cooled to the ground state
- Coherent quantum state swaps between light and mechanics



## Unresolved sideband: $\omega_m \ll \kappa$

- Can be feedback-cooled to the ground state
- Mechanical position can be measured in real time



# Standard quantum limit for position measurements

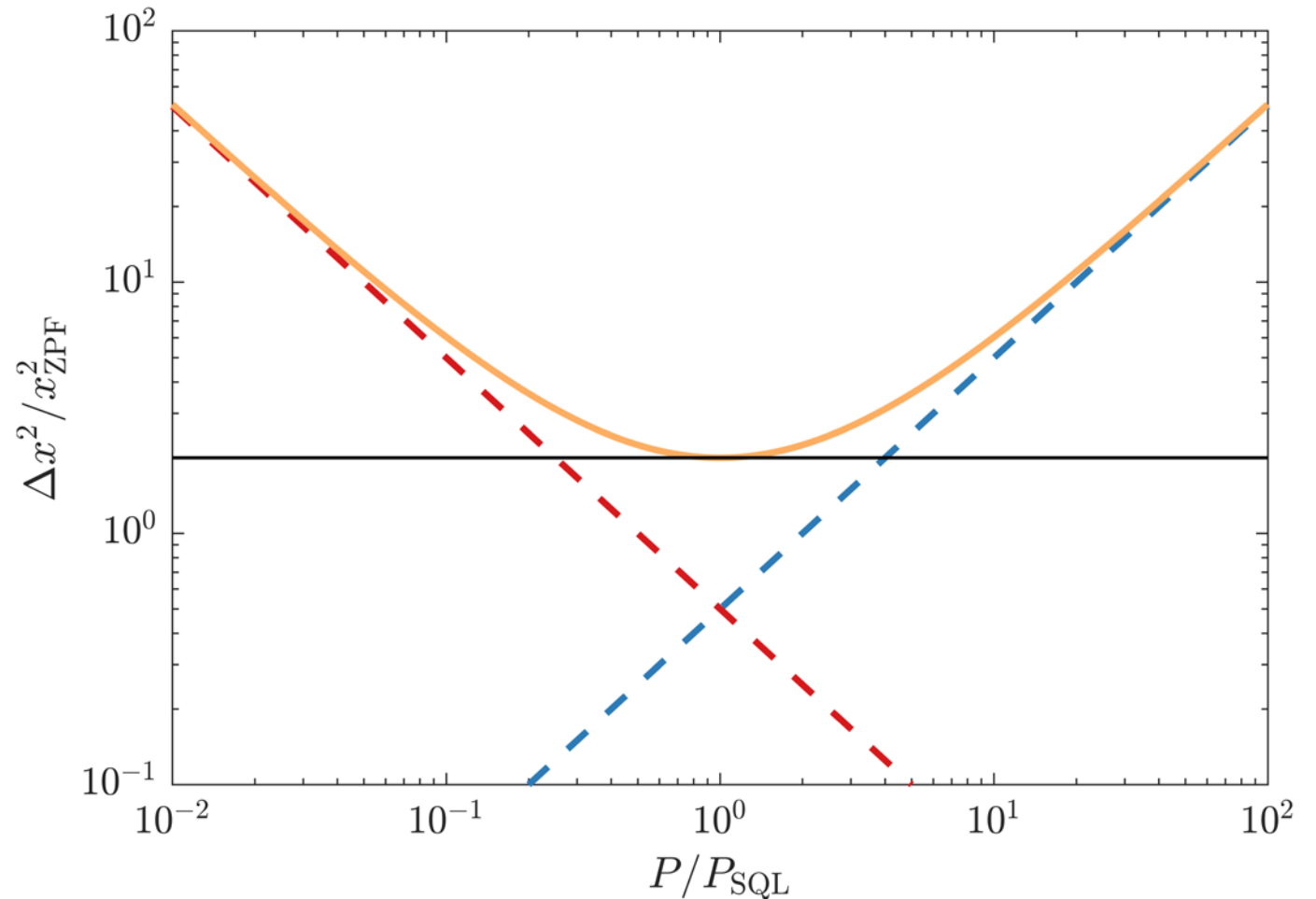
Arises from tradeoff between quantum backaction from radiation pressure and photon shot noise

Photon shot noise

Radiation pressure backaction

Sum

Standard quantum limit

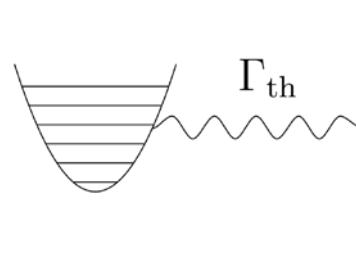


# Quantum challenges for controlling mechanics

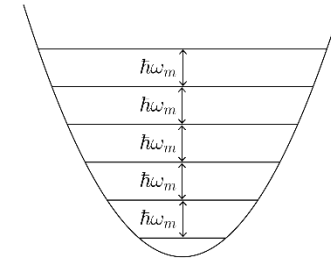
High thermal occupancy

$$n_{\text{th}} = \frac{k_B T}{\hbar \omega_m} \gg 1$$

Strong coupling to environment



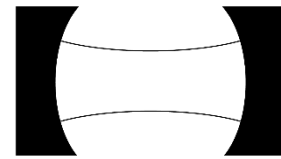
Lack of intrinsic nonlinearity



Sensitive readout required

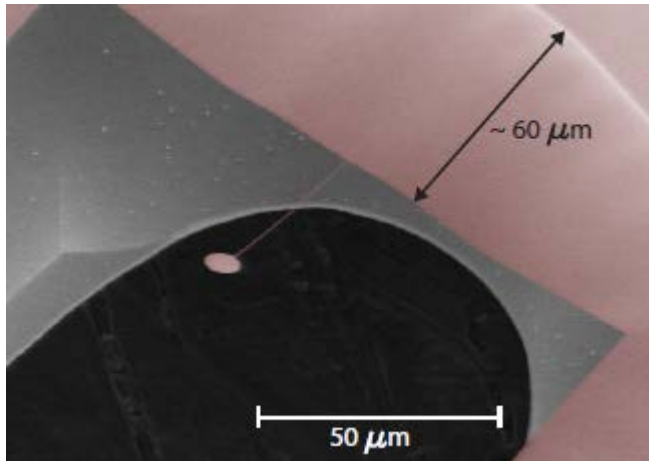
$$x_{\text{ZPF}} \sim \text{fm}$$

Hard to achieve strong coupling



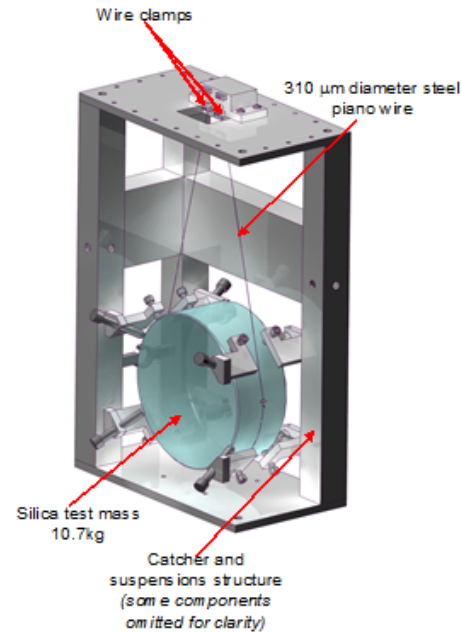
# Dissipation dilution

## Optical trapping



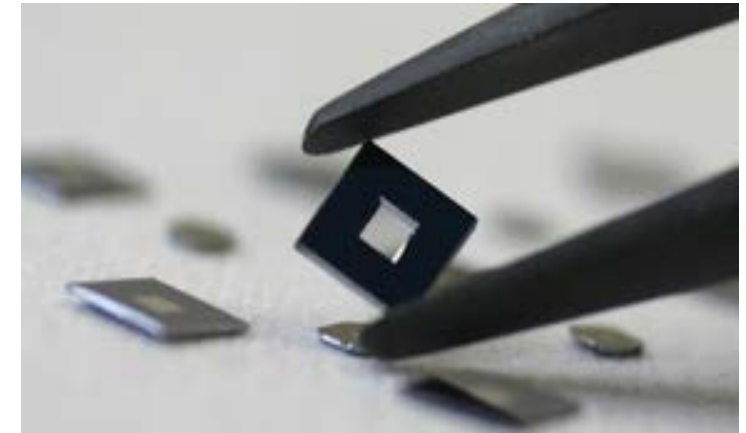
Ni et al., *Phys. Rev. Lett.* (2012)  
Cripe et al., *Nature* (2019)

## Gravitational potential



González and Saulson,  
*J. Acoust. Soc. Am.* (1994)

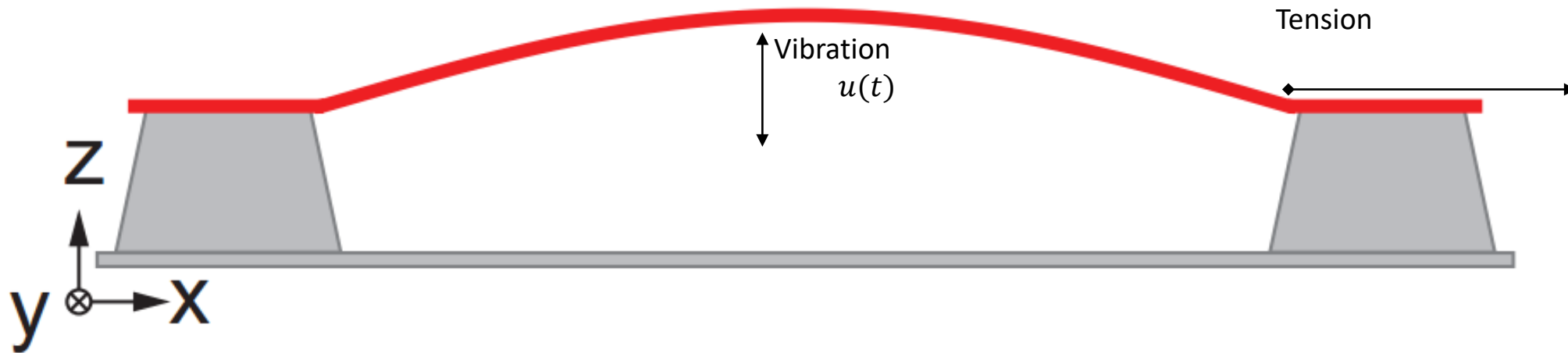
## Nanomechanical resonators



Thompson et al., *Nature* (2008)

# Dissipation dilution in strained materials

Key insight: Stress increases mechanical quality factors *regardless of the source of loss*



**Therefore: Use a high deposition stress material such as  $\text{Si}_3\text{N}_4$**

Fedorov, Engelsen et al., *Phys. Rev. B* **99** (2019)

G.I. Gonzalez and P.R. Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)

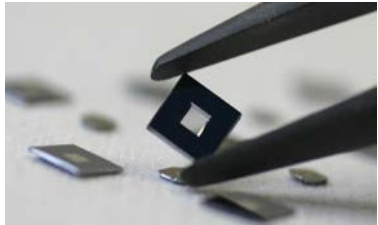
Q. P. Unterreithmeier, T. Faust, *Phys. Rev. Lett.* **105**, 027205 (2010)

P.-L. Yu, T.P. Purdy, C.A. Regal, *Phys. Rev. Lett.* **108**, 083603 (2012)



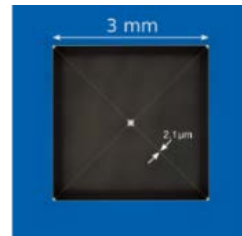
# A timeline of $\text{Si}_3\text{N}_4$ mechanics

## Millimeter-scale membranes



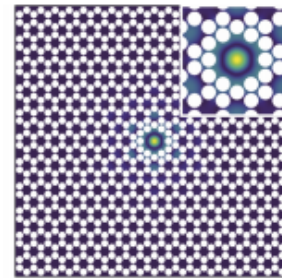
Thompson et al.,  
*Nature* 452, 72-75 (2008)

## Trampoline membranes



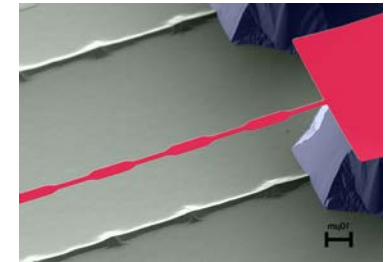
Sankey et al.,  
*PRX* 6, 021001 (2016)

## Soft-clamping



Y. Tsaturyan et. al.  
*Nat. Nano* 12, 776 (2017)

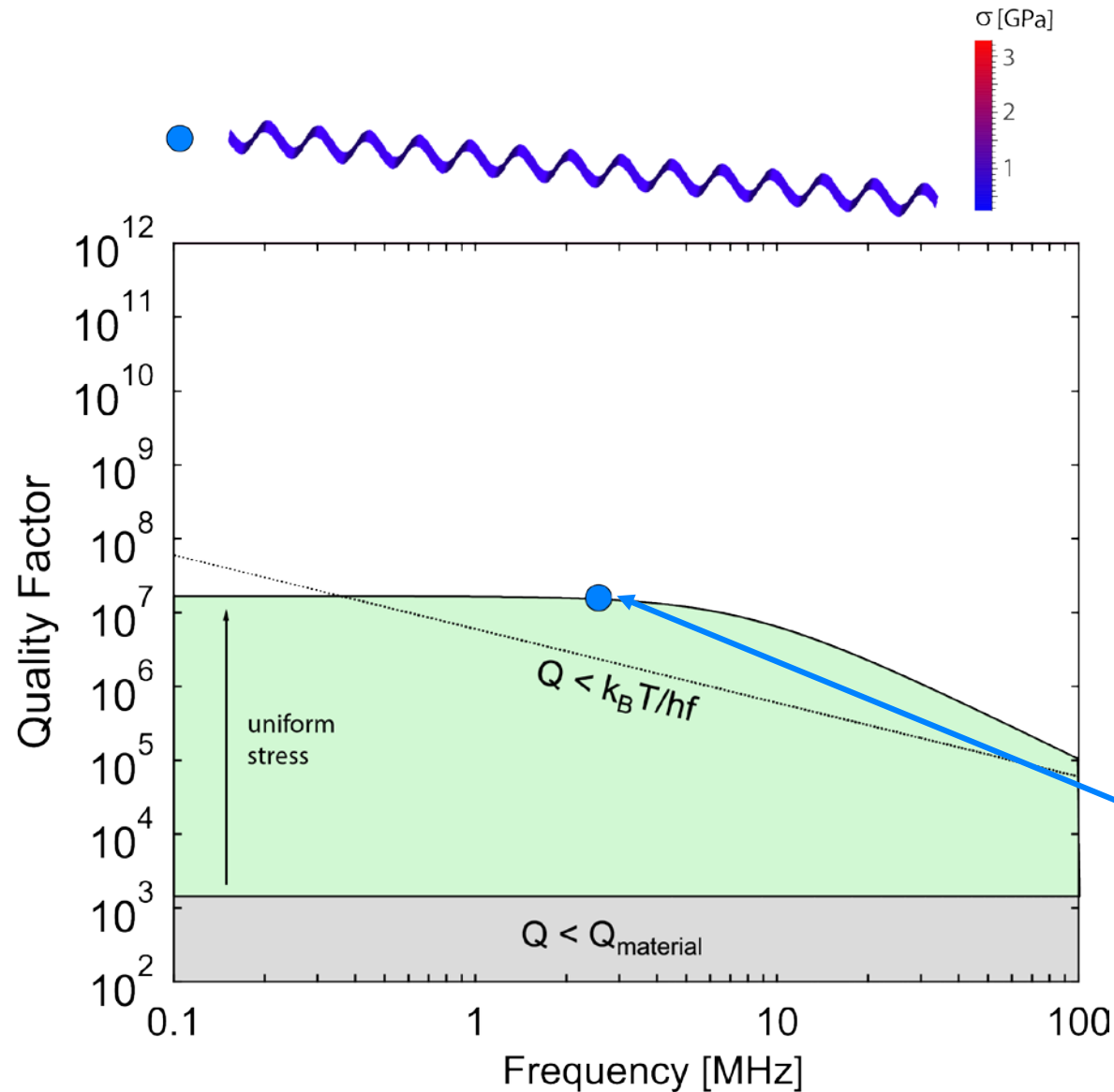
## Strain engineering



Ghadimi et al.,  
*Science* 360 (2017)

Higher aspect ratios and engineered geometry has enabled 100-1000 times higher mechanical quality factor

# Increasing the $Q$ with dissipation dilution

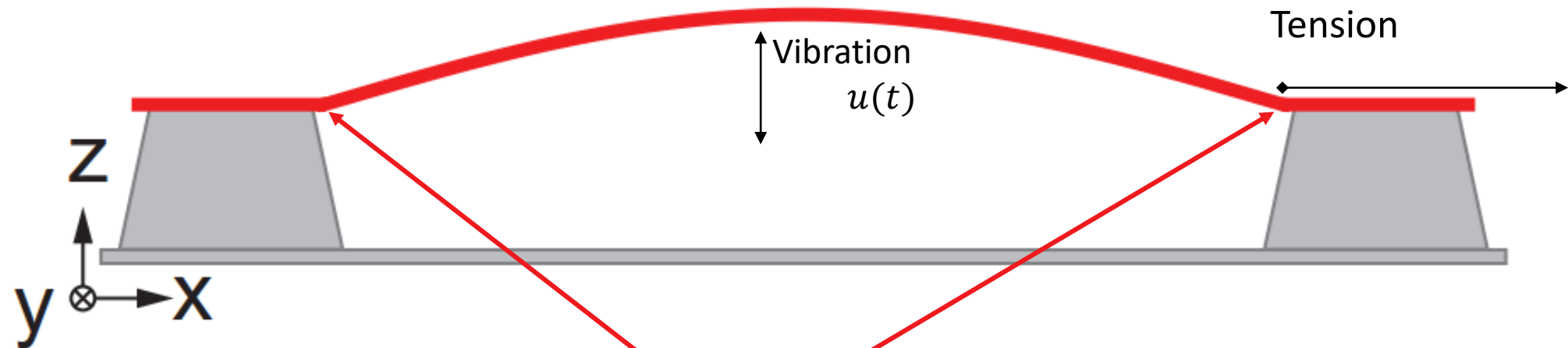


Deposition stress	1.1 Gpa
Thickness	20 nm
Length	3 mm

High stress  
material,  $\text{Si}_3\text{N}_4$

# Dissipation dilution

Key insight: Stress increases mechanical quality factors *regardless of the source of loss*

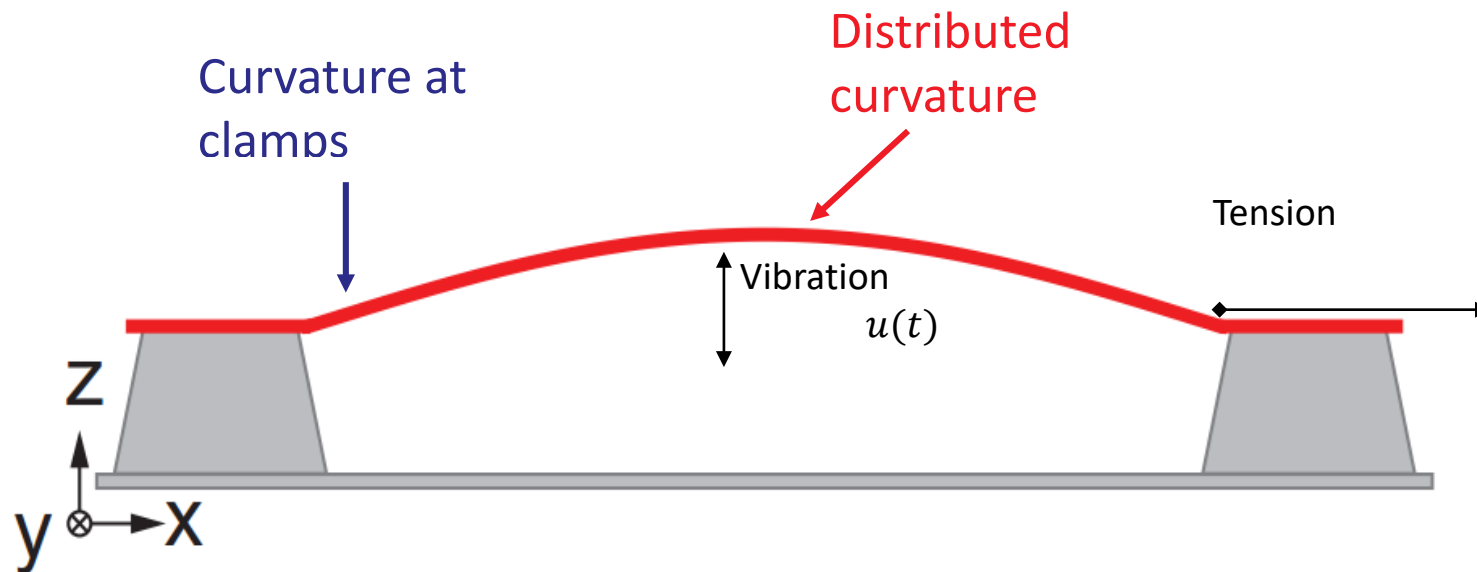


High curvature clamping region:  
Main limitation on  $Q$

- Fedorov, Engelsen et al., *Phys. Rev. B* **99**, 054107 (2019)  
 Gonzalez and Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)  
 Unterreithmeier et al., *Phys. Rev. Lett.* **105**, 027205 (2010)  
 Yu et al., *Phys. Rev. Lett.* **108**, 083603 (2012)

# Dissipation dilution

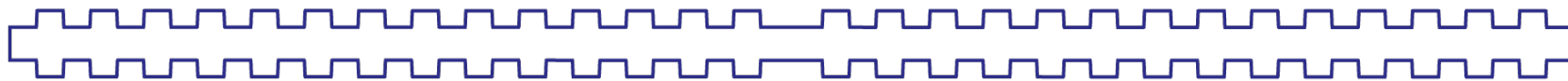
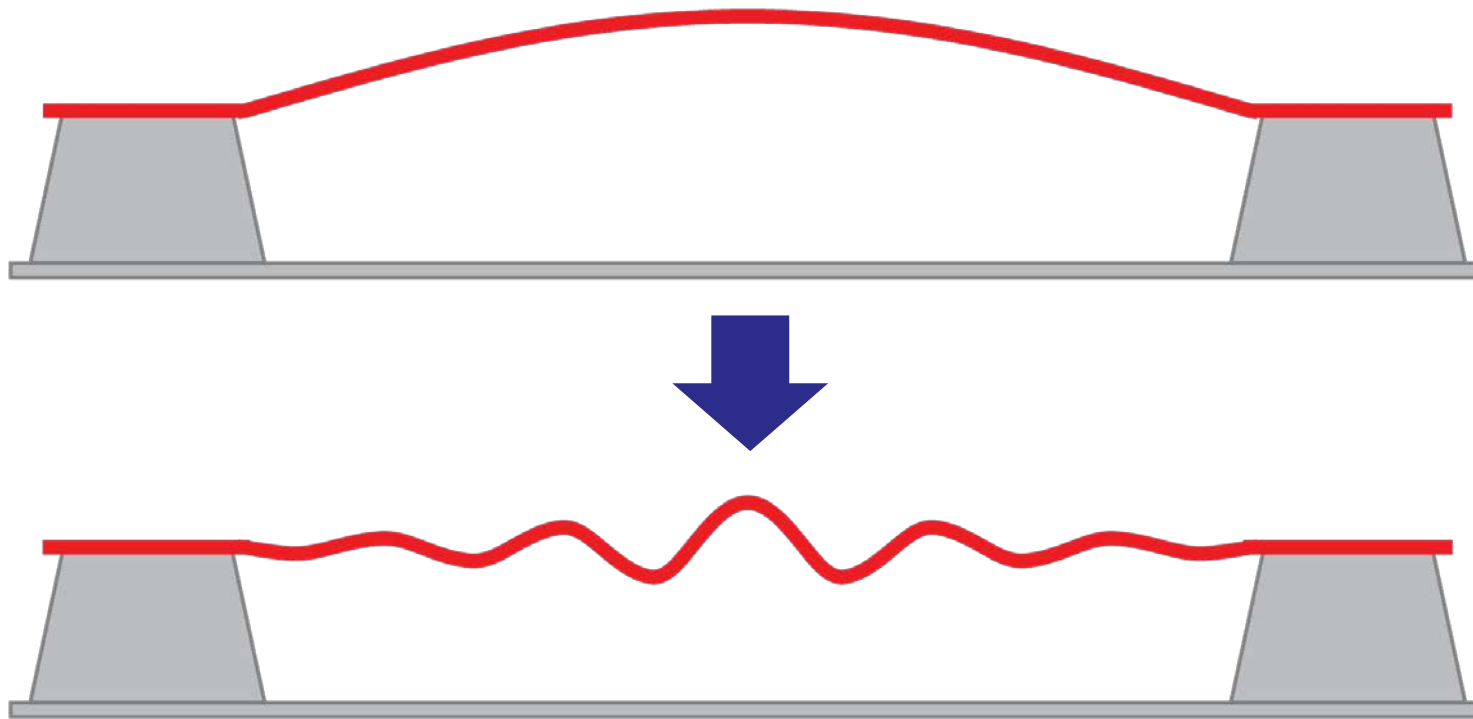
$$\frac{Q}{Q_{\text{int}}} = \frac{1}{2\lambda + n^2 \pi^2 \lambda^2} \quad \lambda = \frac{h}{L} \sqrt{\frac{E_0}{12\sigma}} \ll 1$$



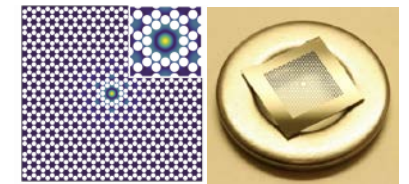
$Q_{\text{int}}$	Intrinsic $Q$
$n$	Mode number
$h$	Thickness
$L$	Length
$E_0$	Young's modulus
$\sigma$	Material stress

Fedorov, Engelsen et al., *Phys. Rev. B* **99**, 054107 (2019)  
 Gonzalez and Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)  
 Unterreithmeier et al., *Phys. Rev. Lett.* **105**, 027205 (2010)  
 Yu et al., *Phys. Rev. Lett.* **108**, 083603 (2012)

# Soft clamping



Pattern a phononic crystal on the beam with a defect in the center, creating a localized mode

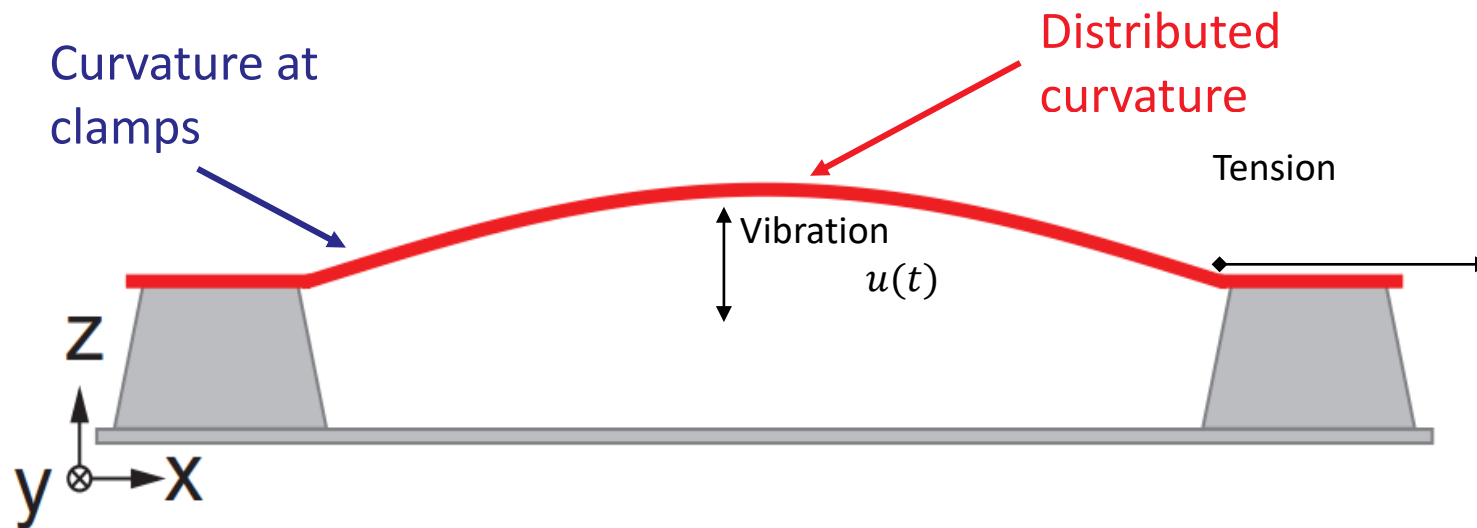


Y. Tsaturyan et. al. *Nature Nanotechnology* 12, 776 (2017)

# Dissipation dilution

$$\frac{Q}{Q_{\text{int}}} = \frac{1}{\cancel{2\lambda} + n^2 \pi^2 \lambda^2} \quad \lambda = \frac{h}{L} \sqrt{\frac{E_0}{12\sigma}} \lll 1$$

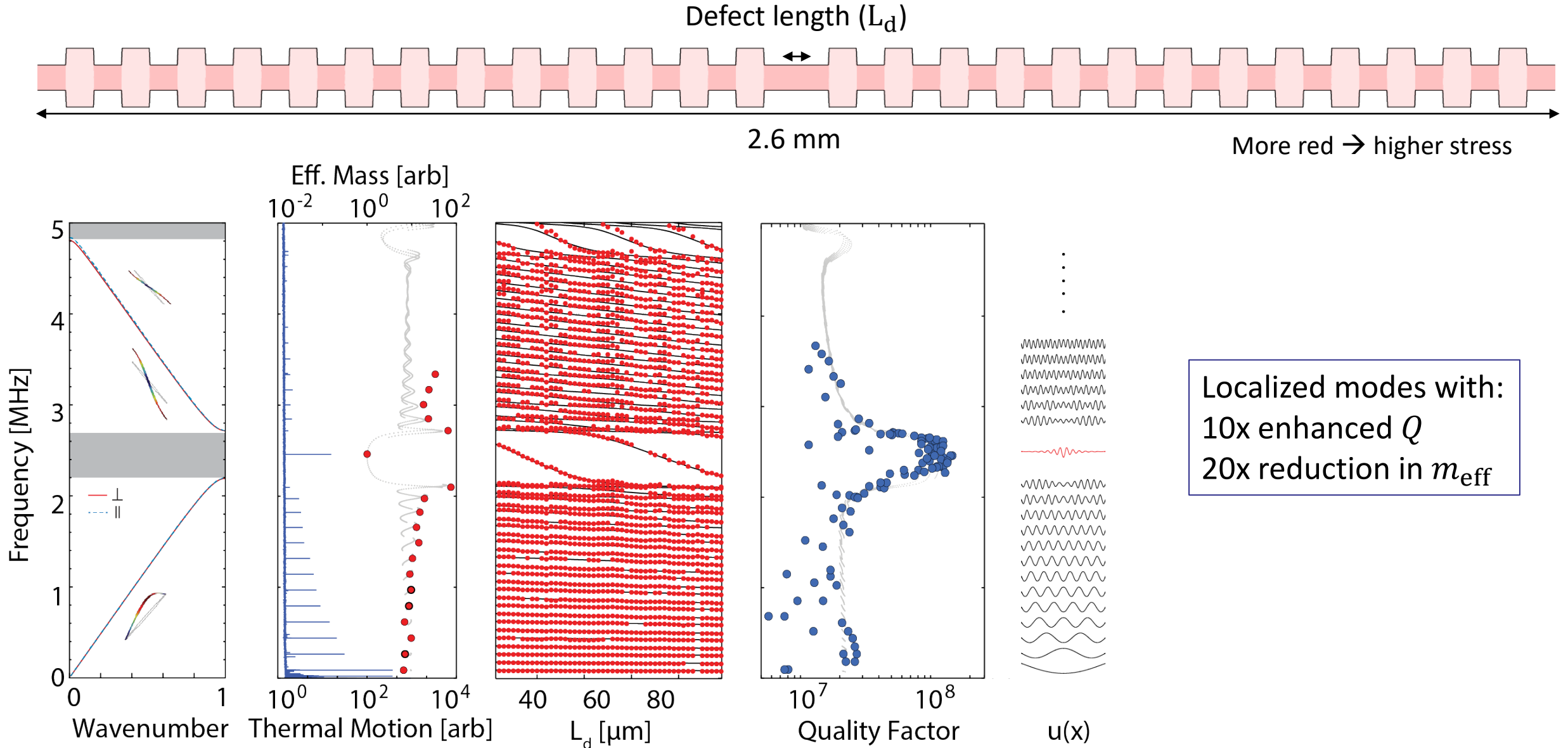
Soft clamping



$Q_{\text{int}}$  Intrinsic  $Q$   
 $n$  Mode number  
 $h$  Thickness  
 $L$  Length  
 $E_0$  Young's modulus  
 $\sigma$  Material stress

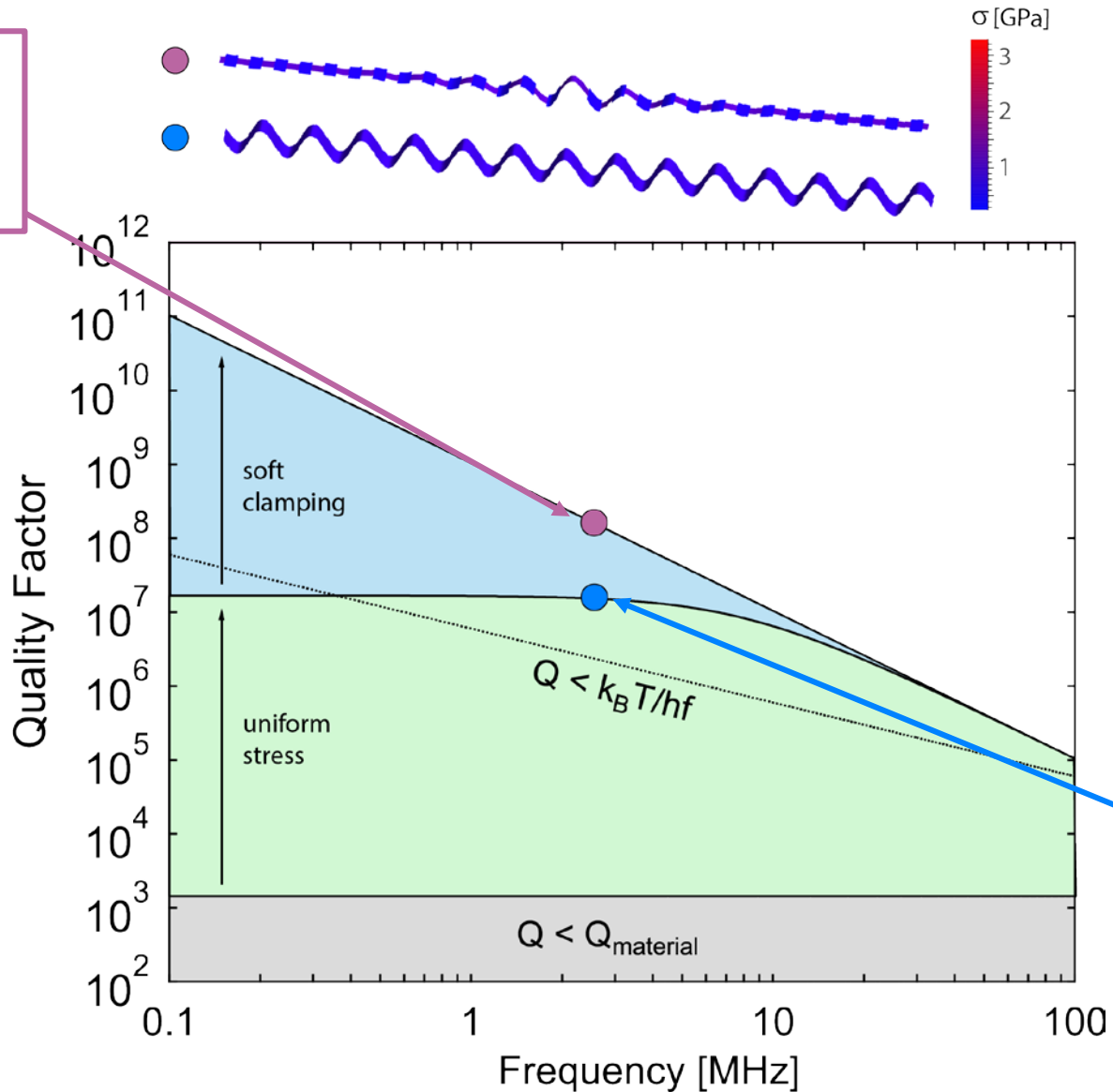
Fedorov, Engelsen et al., *Phys. Rev. B* **99**, 054107 (2019)  
 Gonzalez and Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)  
 Unterreithmeier et al., *Phys. Rev. Lett.* **105**, 027205 (2010)  
 Yu et al., *Phys. Rev. Lett.* **108**, 083603 (2012)

# Soft clamped nanobeams



# Increasing the $Q$ with dissipation dilution

Soft clamping  
removes clamping  
losses





# Dissipation dilution

$$\frac{Q}{Q_{\text{int}}} = \frac{1}{\cancel{2\lambda} + n^2 \pi^2 \lambda^2}$$

Soft clamping

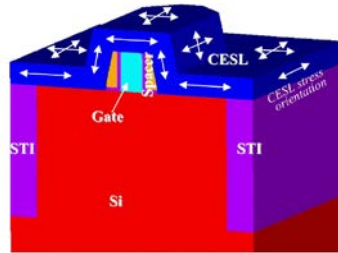
Now, minimize  $\lambda$ :

1. High aspect ratio ( $h/L$ )
2. High stress ( $\sigma$ )

$$\lambda = \frac{h}{L} \sqrt{\frac{E_0}{12\sigma}}$$

$Q_0$  Intrinsic  $Q$   
 $n$  Mode number  
 $h$  Thickness  
 $L$  Length  
 $E_0$  Young's modulus  
 $\sigma$  Material stress

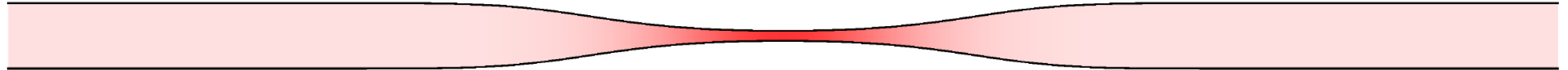
# Elastic strain engineering



## Elastic strain engineering for unprecedented materials properties

Ju Li, Zhiwei Shan, and Evan Ma, Guest Editors

Key insight: use geometry to locally increase the stress



More red → higher stress

A simple taper increases the stress in the center...  
...but loss near clamps will increase, leading to lower  $Q$ !

Li *et al.*, *MRS Bull.* **39**, 108-114 (2014)

Zhang *et al.*, *Appl. Phys. Lett.* **107**, 131110 (2015)

# Clamp-tapering – a strain engineering technique

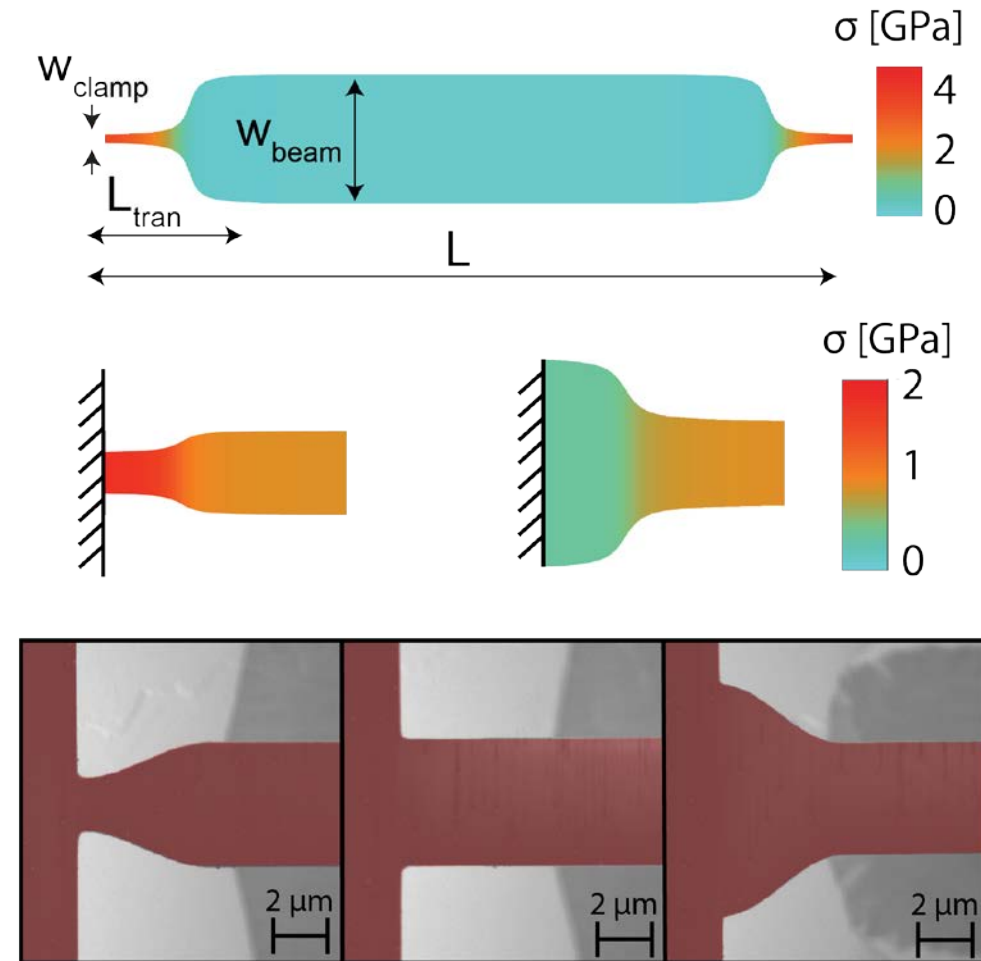
$$\frac{Q}{Q_{\text{int}}} = \frac{1}{2\lambda_{\text{cl}} + n^2 \pi^2 \lambda^2}$$

- Clamp taper increases stress at clamps → reduced loss at clamps
- Tapering enhances  $Q$  of lower-order modes including the *fundamental mode*
- Does not require increased device size

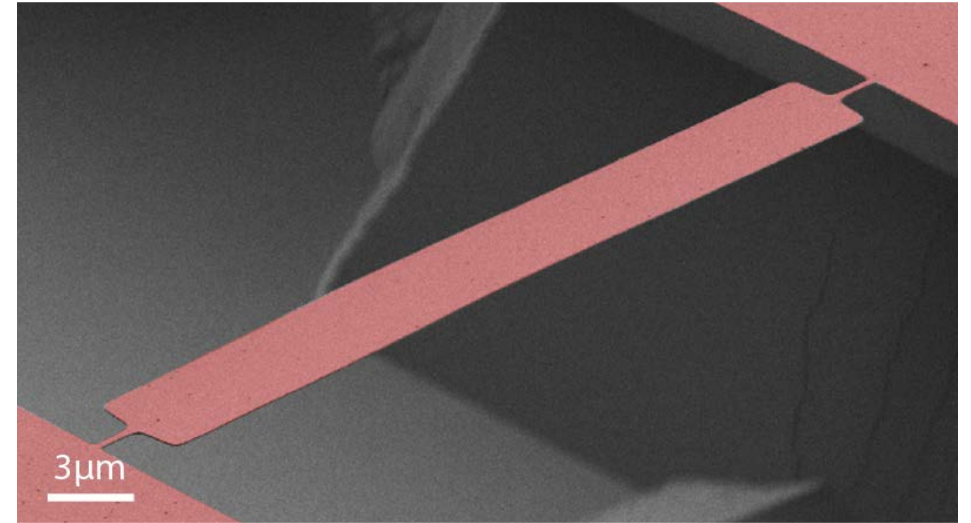
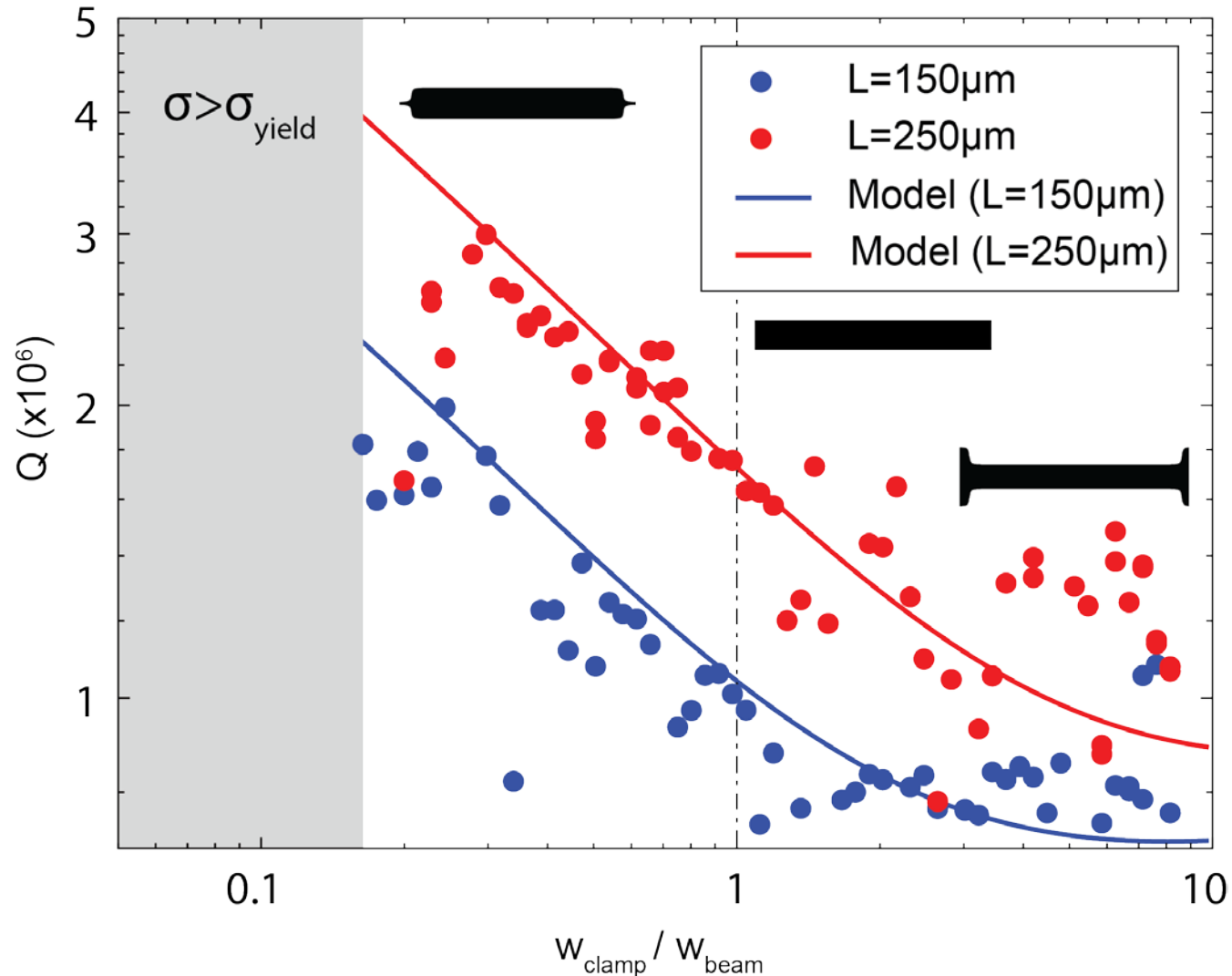
Bereyhi et al., *Nano Lett.* 19(4), 2019

Fedorov, Engelsen et al., *Phys. Rev. B* 99, 054107 (2019)

Sadeghi et al., *arXiv:1905.06730* (2019)



# Clamp-tapering for fundamental mode $Q$ enhancement



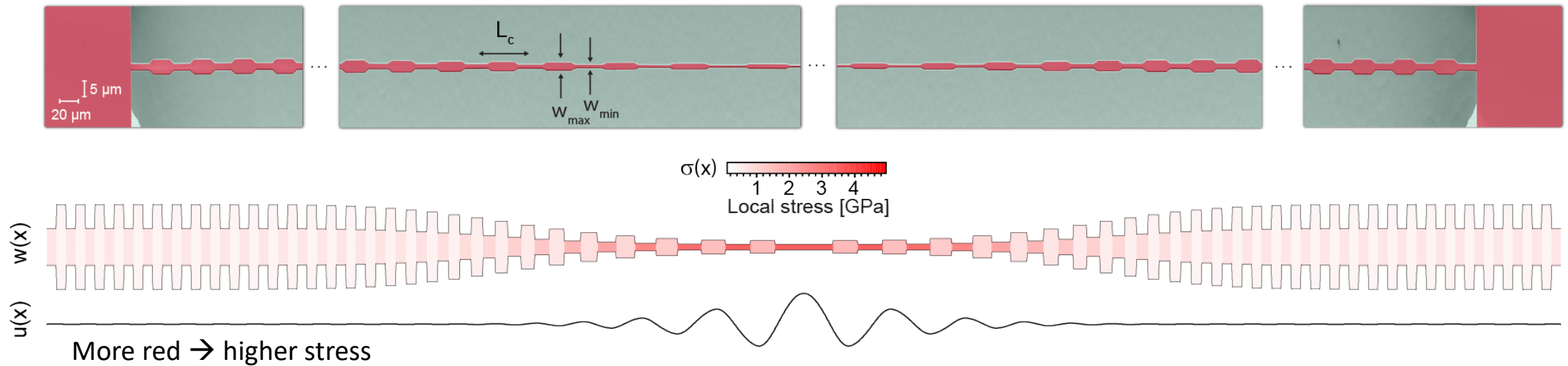
At yield stress, factor of  $\sim 2$  enhancement for  $\text{Si}_3\text{N}_4$

Bereyhi et al., *Nano Lett.* **19**(4), 2019

Fedorov, Engelsen et al., *Phys. Rev. B* **99**, 054107 (2019)

Sadeghi et al., *arXiv:1905.06730* (2019)

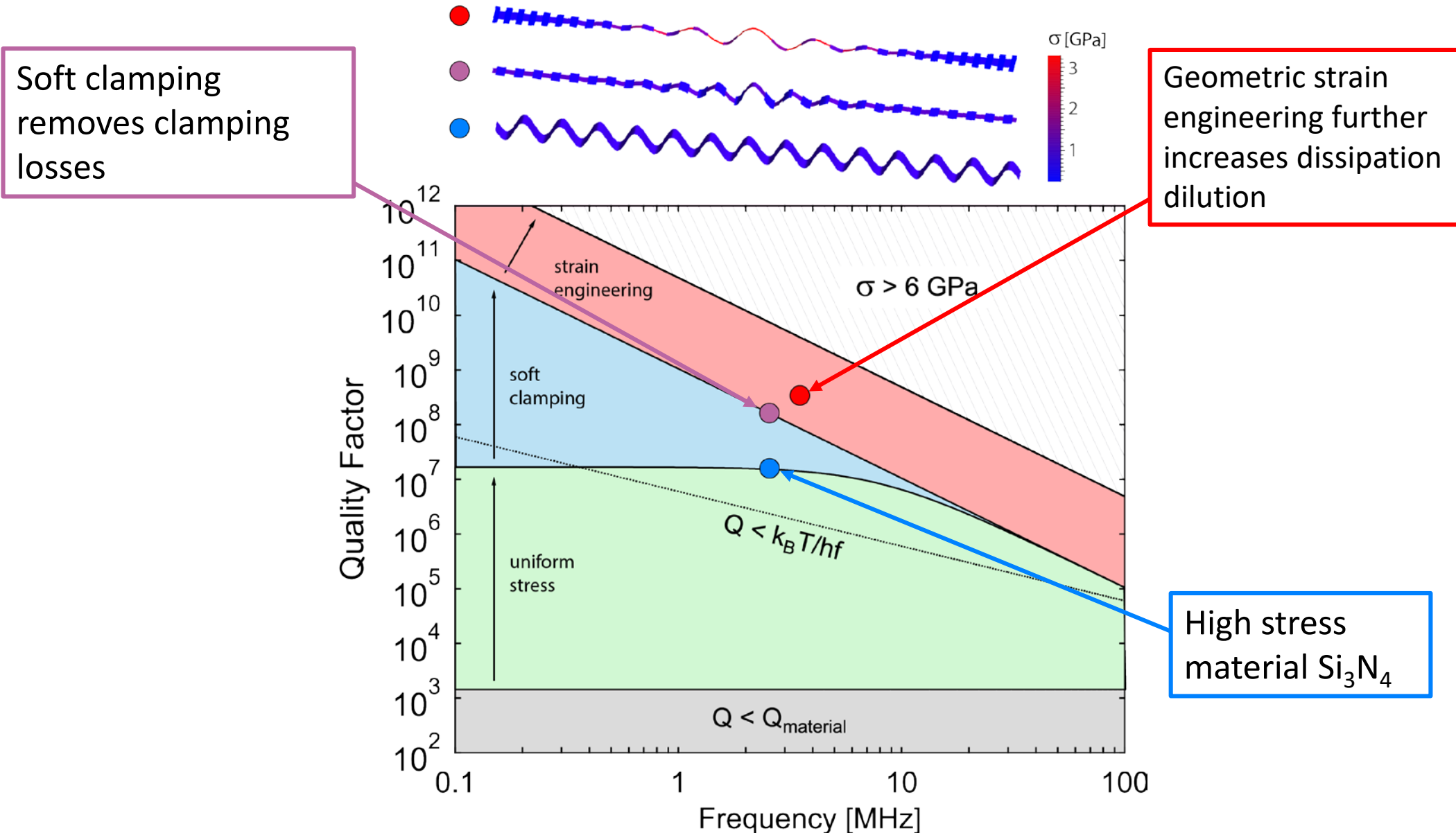
# Elastic strain engineering with soft clamping



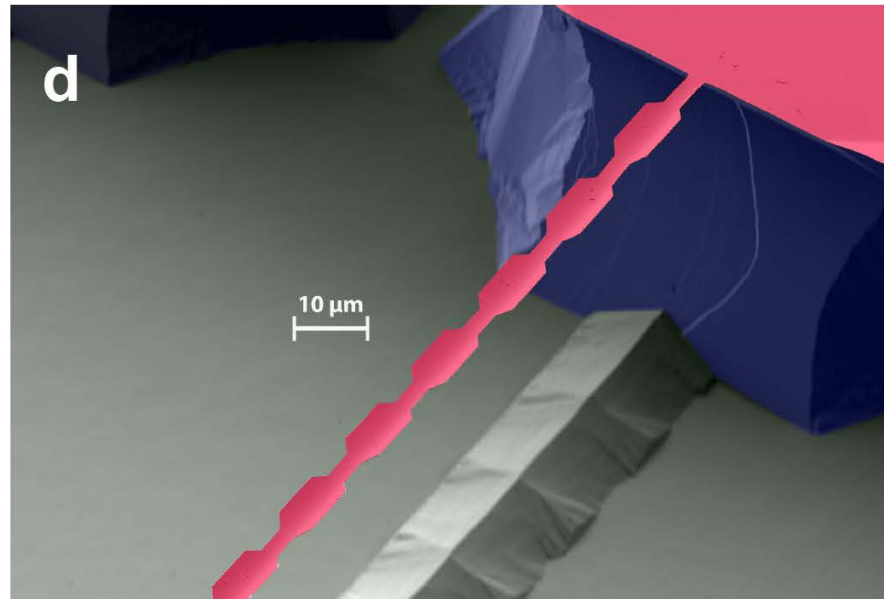
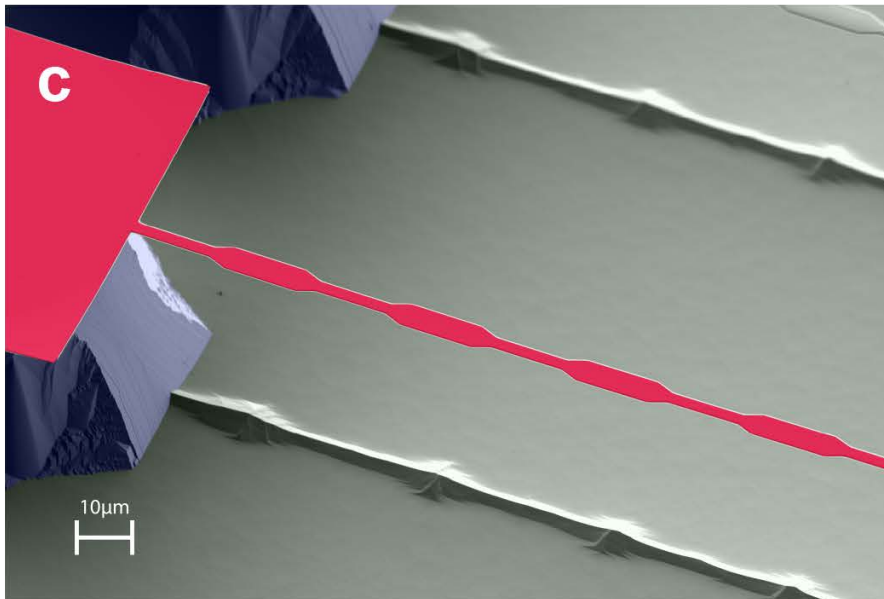
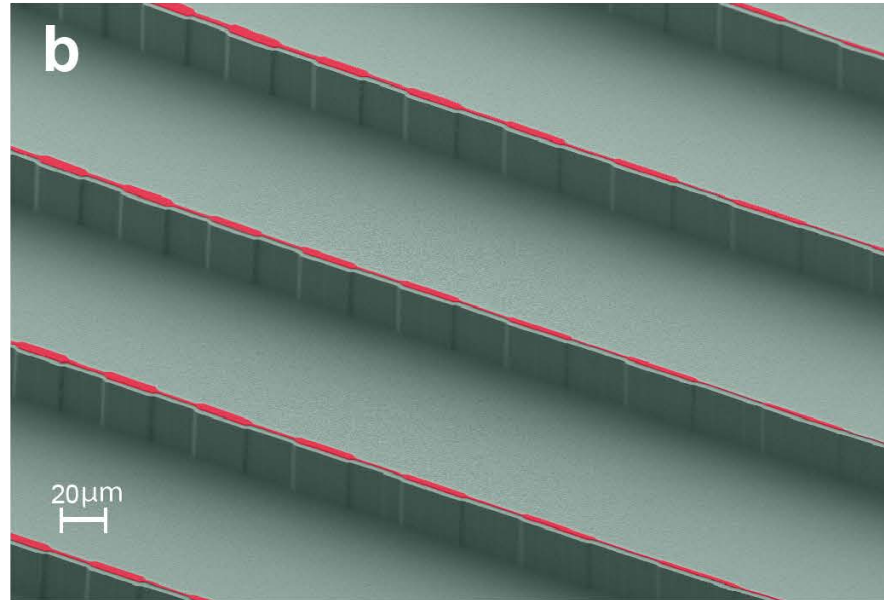
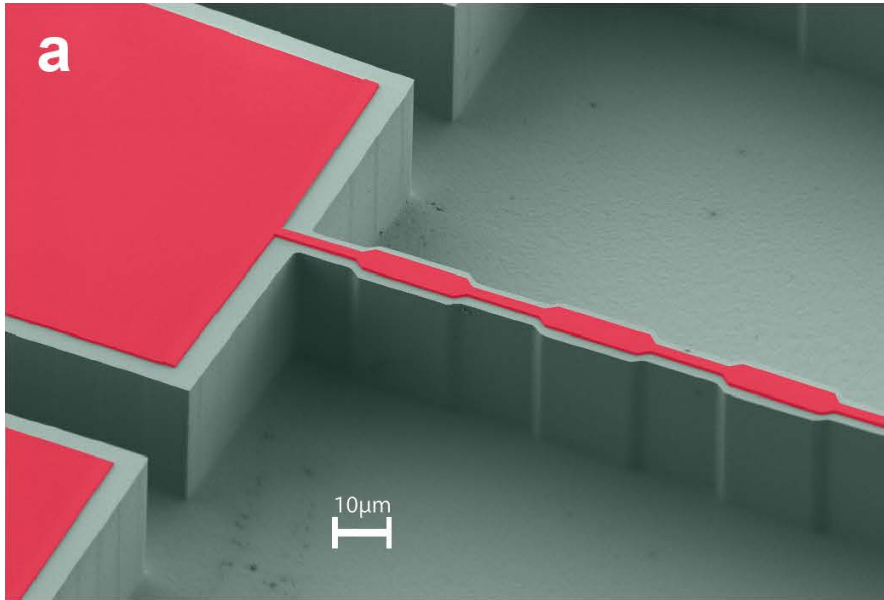
1. Localize the mechanical mode using soft clamping
2. Taper the beam to colocalize strain with the mechanical mode

Pitch of unit cells must be changed to maintain same bandgap throughout the beam

# Increasing the $Q$ with dissipation dilution



# SEMs of fabrication process

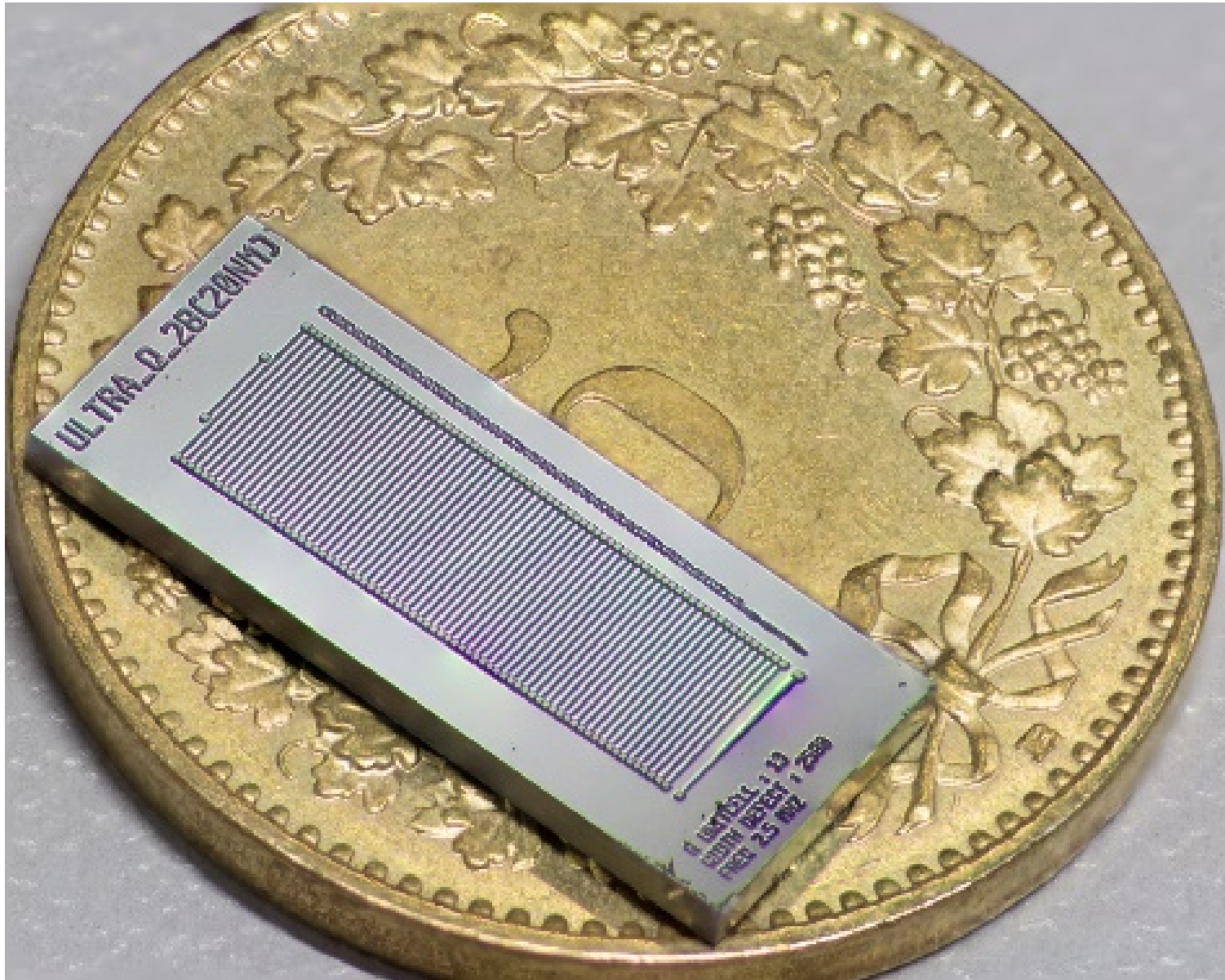


Red: Silicon nitride  
Green: Silicon  
Blue: Silicon pillar

## Fabrication outline

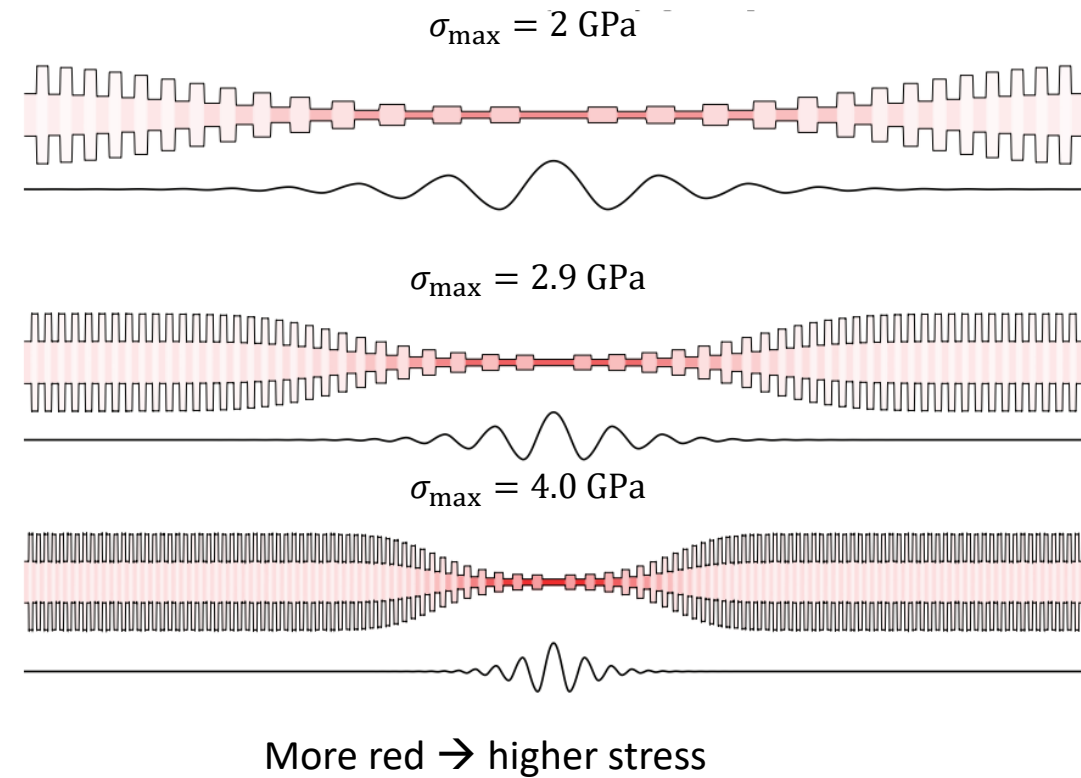
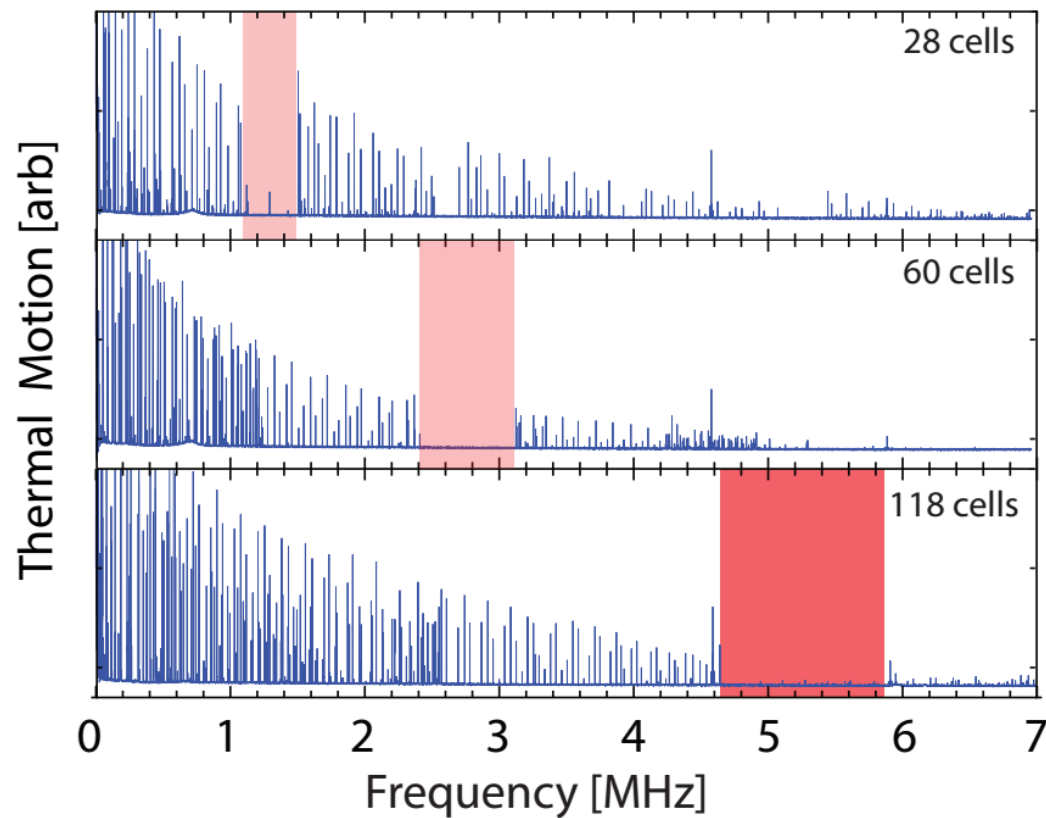
1. Ebeam lithography
2. Deep etch (RIE)
3. KOH undercut

# Final devices: 20 nm thick and 3-8 mm long

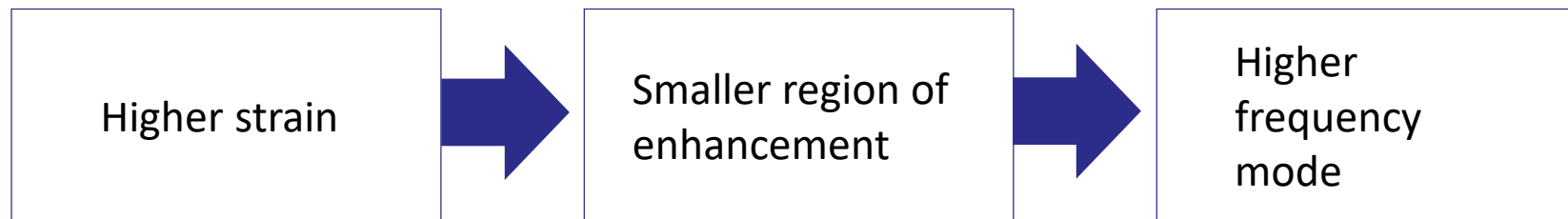




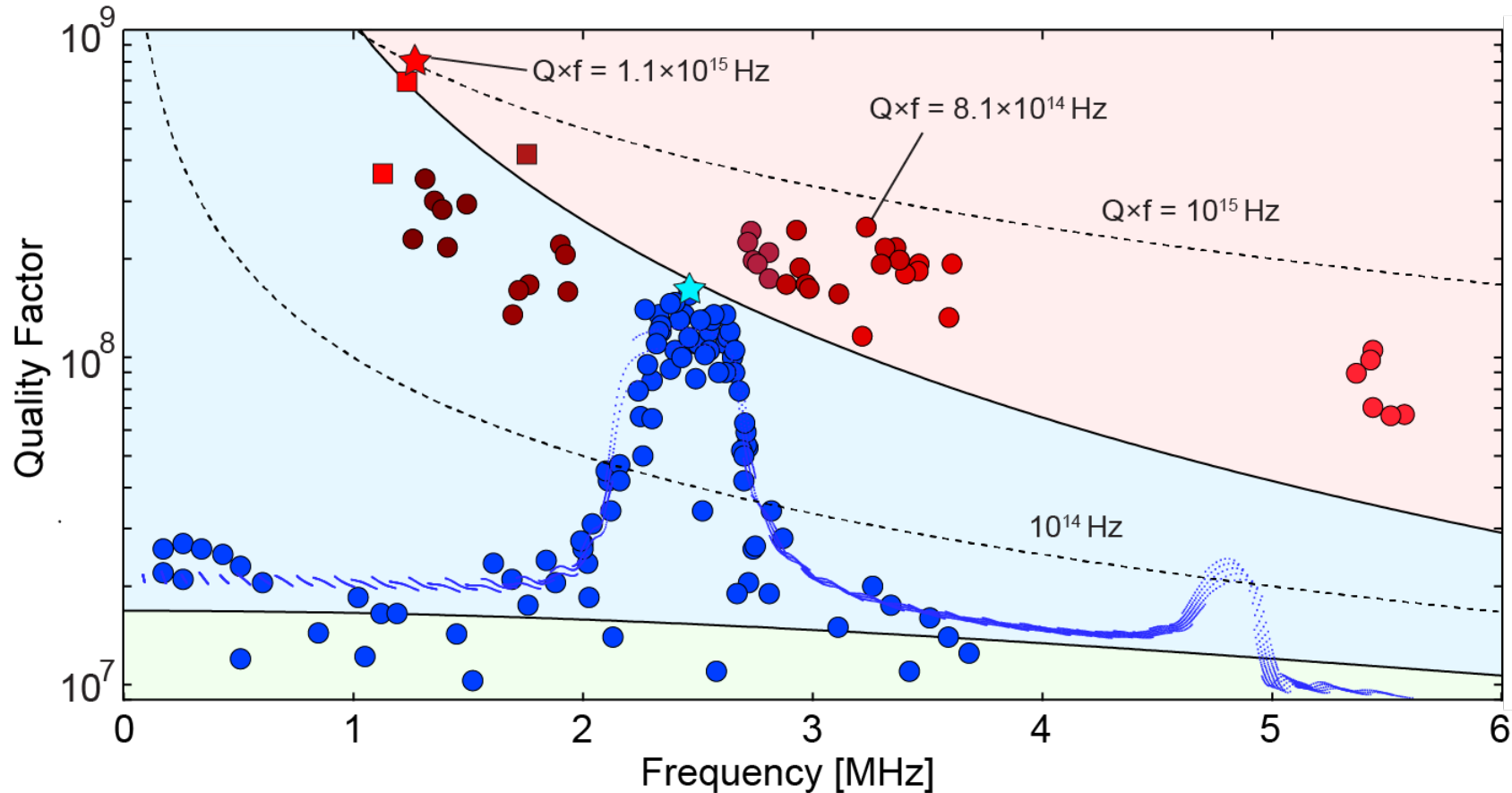
# Strain engineered beams - bandgaps



For fixed beam length (as high as limited by fabrication):



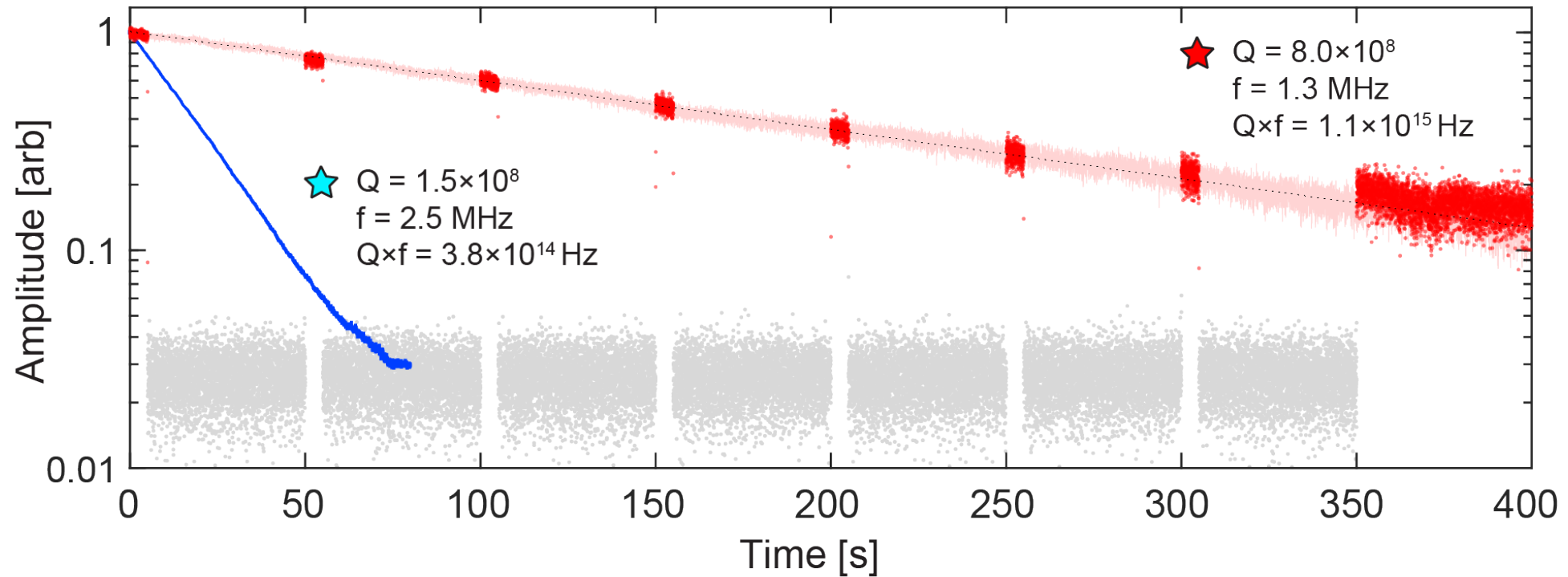
# Strain engineered beams – quality factors



Strain engineering allows high  $Qf (> 5 \times 10^{14}$  Hz) for a wide range of frequencies

	L [mm]	Cells	Shape
●	4	28	
↓		↓	
●	7	118	
★	7	50	
■	7	60	
★	2.6	26	

# $Q$ of 800 million at 1.3 MHz

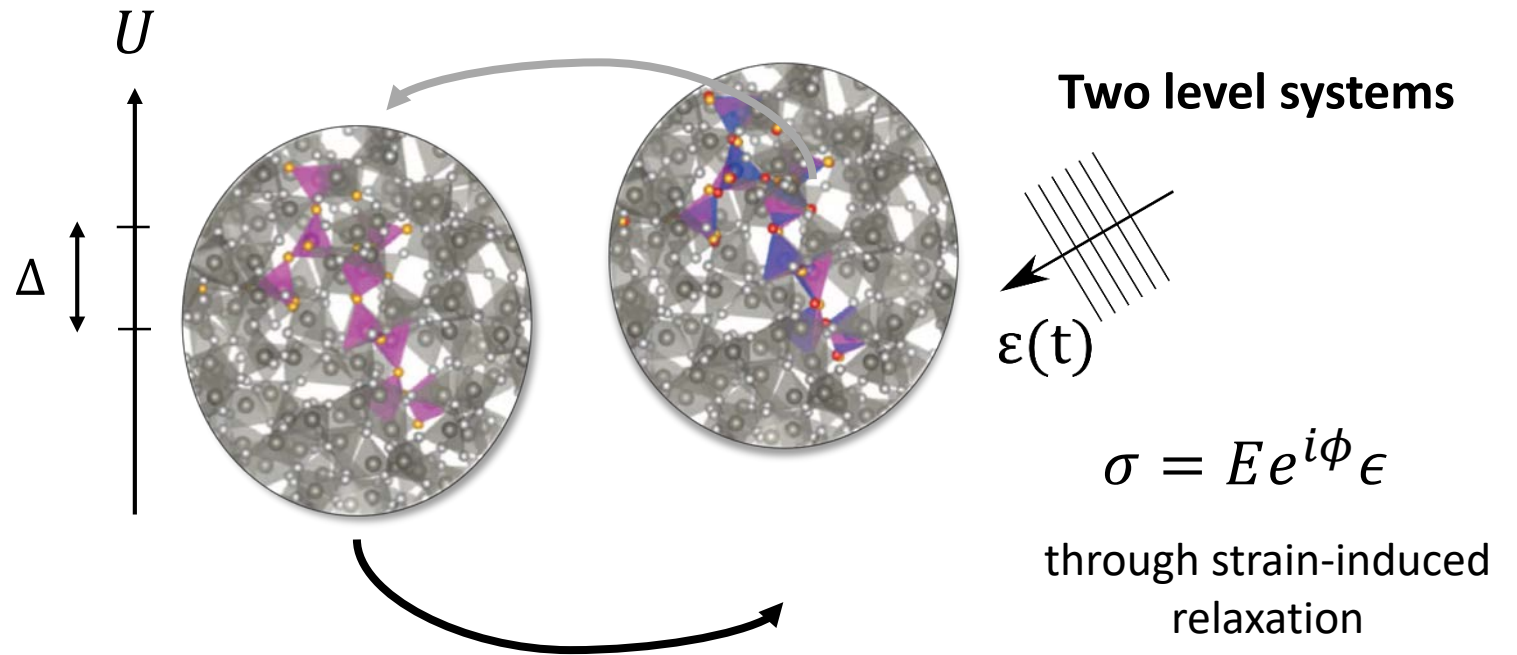
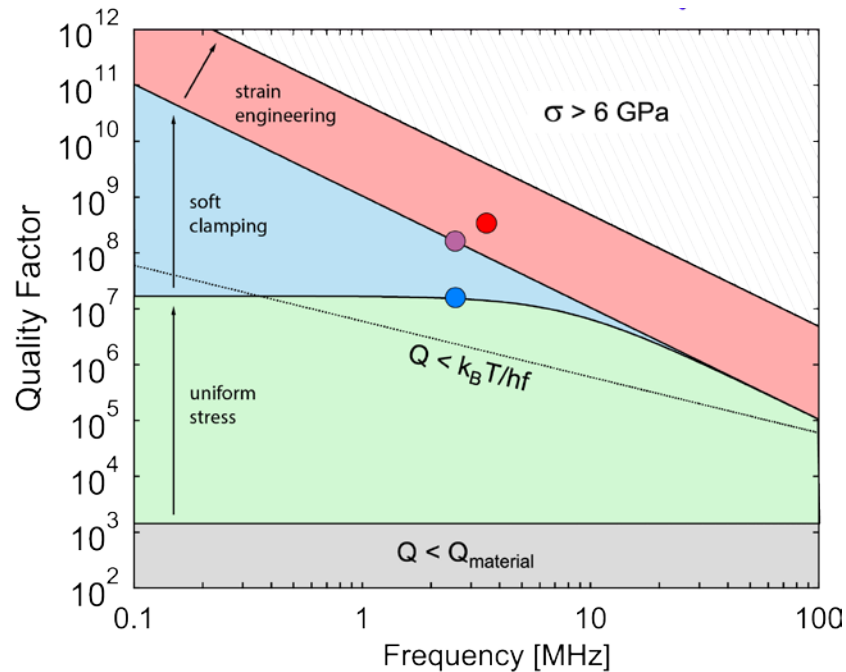


## Unprecedented mechanical dissipation

- Highest quality factor and  $Qf$  product achieved for a room temperature mechanical oscillator
- Stroboscopic measurement taken to control for photothermal anti-damping

# How can we go beyond Si<sub>3</sub>N<sub>4</sub>?

$$\frac{Q}{Q_{int}} = \frac{1}{2\lambda + n^2 \pi^2 \lambda^2}$$



Hamdan et al., *J. Chem. Phys.* 141, 054501 (2014)  
 Faust et al., *Phys. Rev. B* 89, 100-102 (2014)

# Soft-clamped devices of strained silicon

$L \approx 1 \text{ mm}$ ,  $h \approx 10 \text{ nm}$  Aspect ratio  $\approx 10^5$

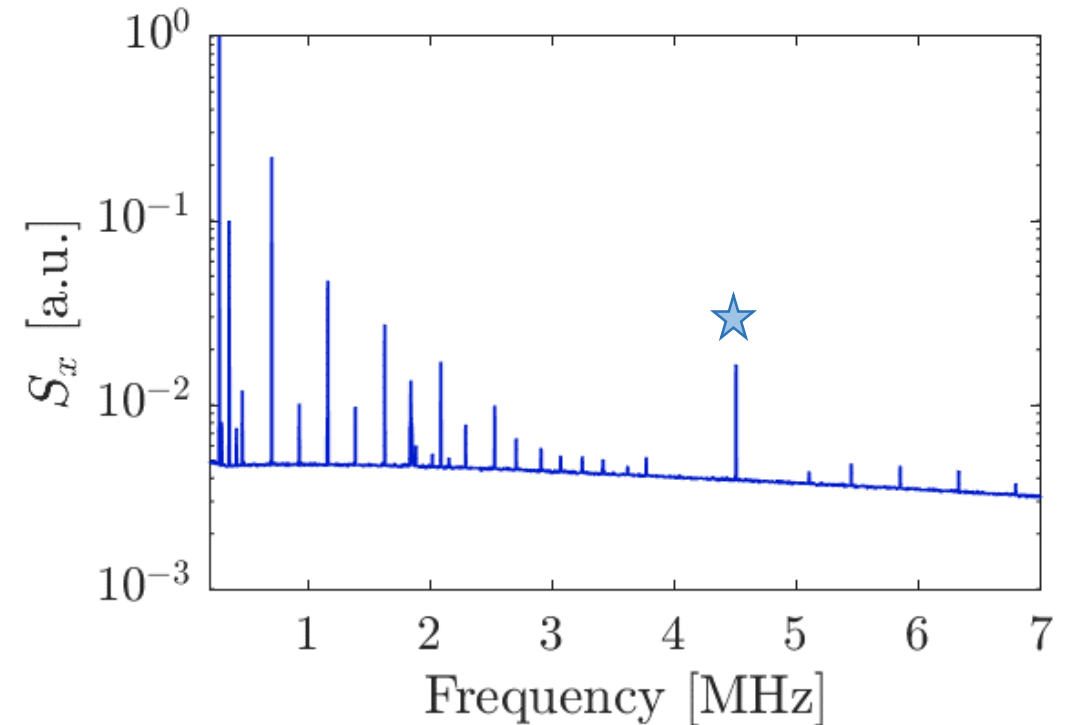


## Fundamental mode quality factor

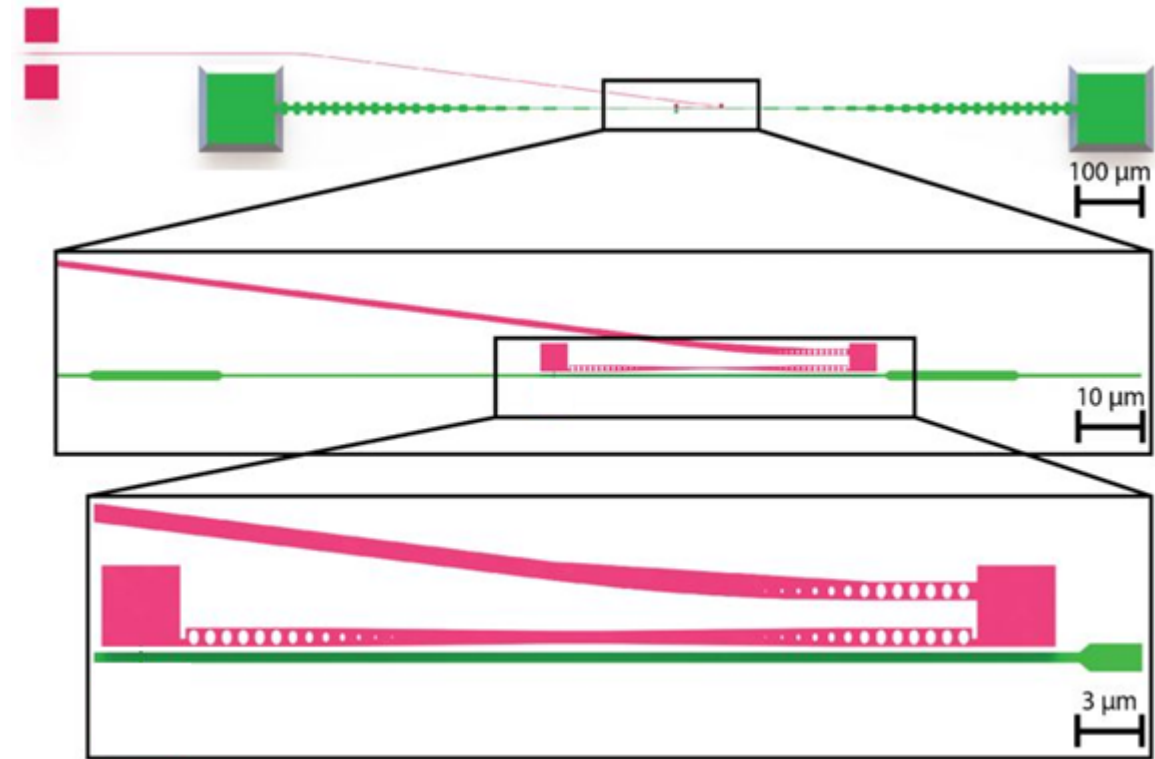
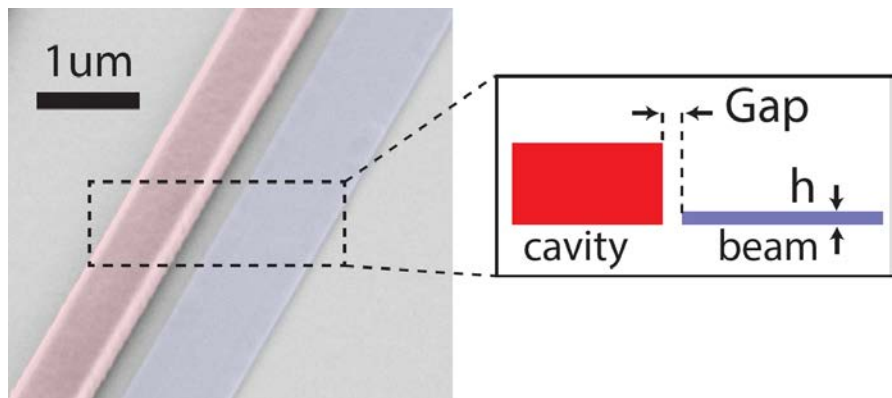
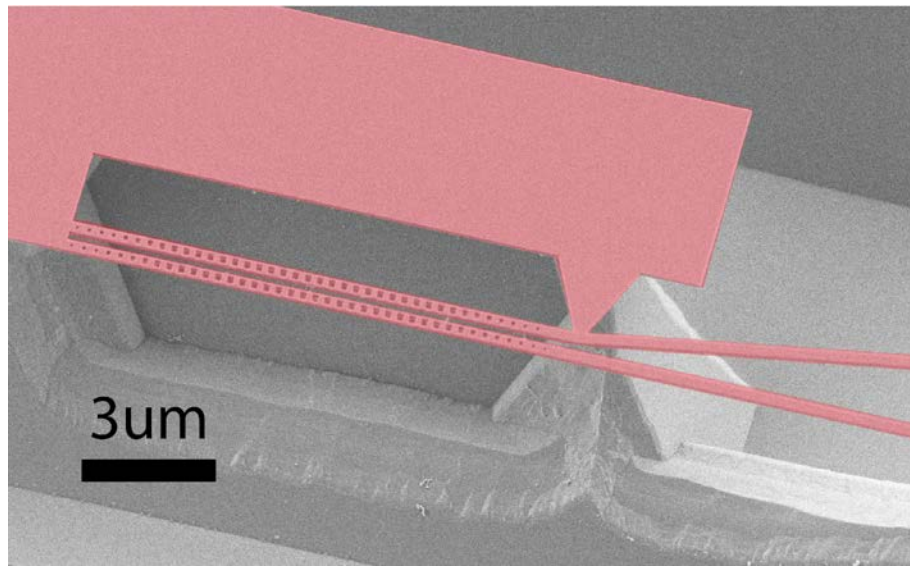
$$Q \approx \{5.5, 9.8\} \cdot 10^5 @ T = \{300, 6\} K$$

$$f = 279 \text{ kHz}$$

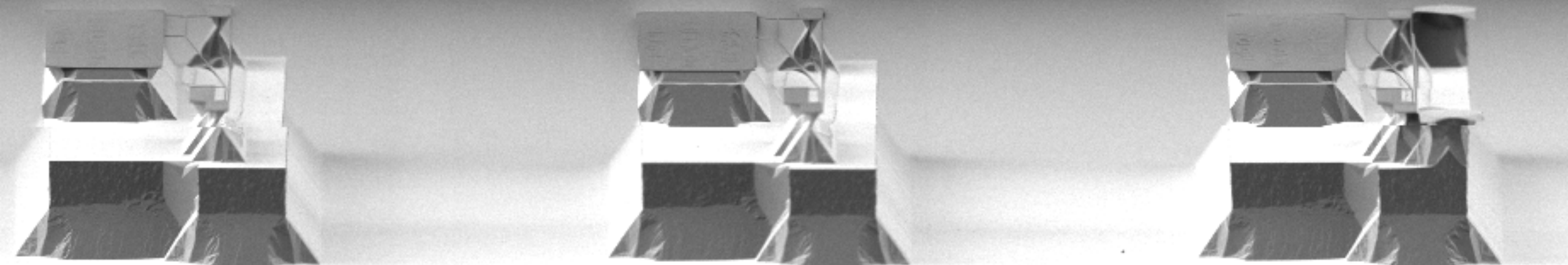
Single high order localized mode,  $m_{\text{eff}} \approx 2.5 \text{ pg}$



# Integration of high-aspect-ratio beams with 1D cavities

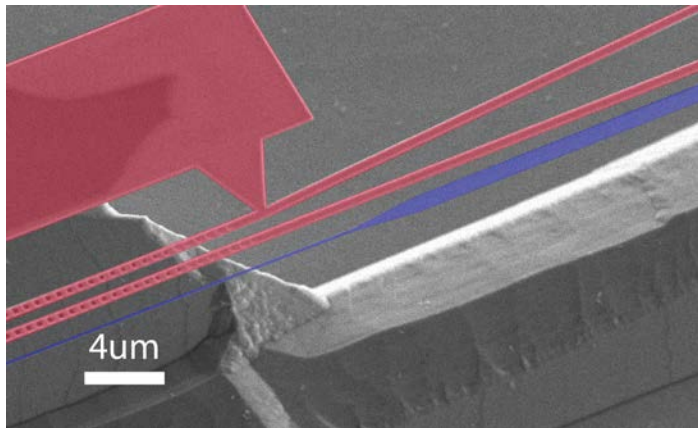
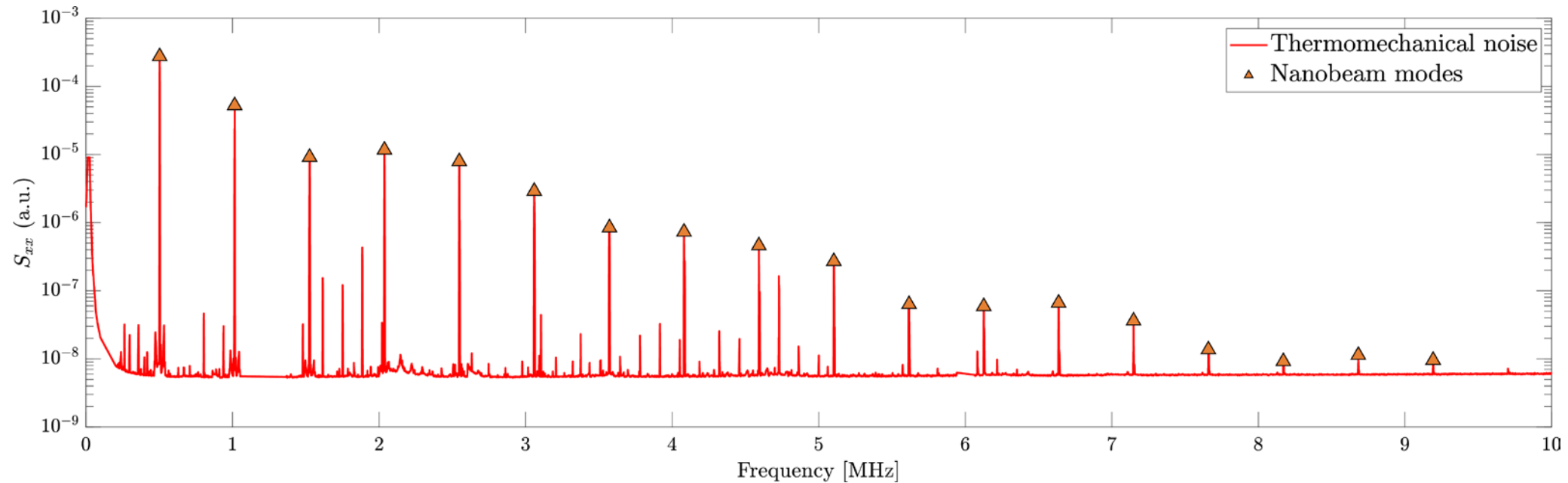


High-Q 1D Fabry-Pérot cavity on a waveguide with photonic crystal end mirrors ( $Q_{int} > 35000$ )  
 Simulations show  $g_0$  ranging from 0.1-1 MHz



160  $\mu\text{m}$

# Clamp-tapered beam integrated with 1D cavity



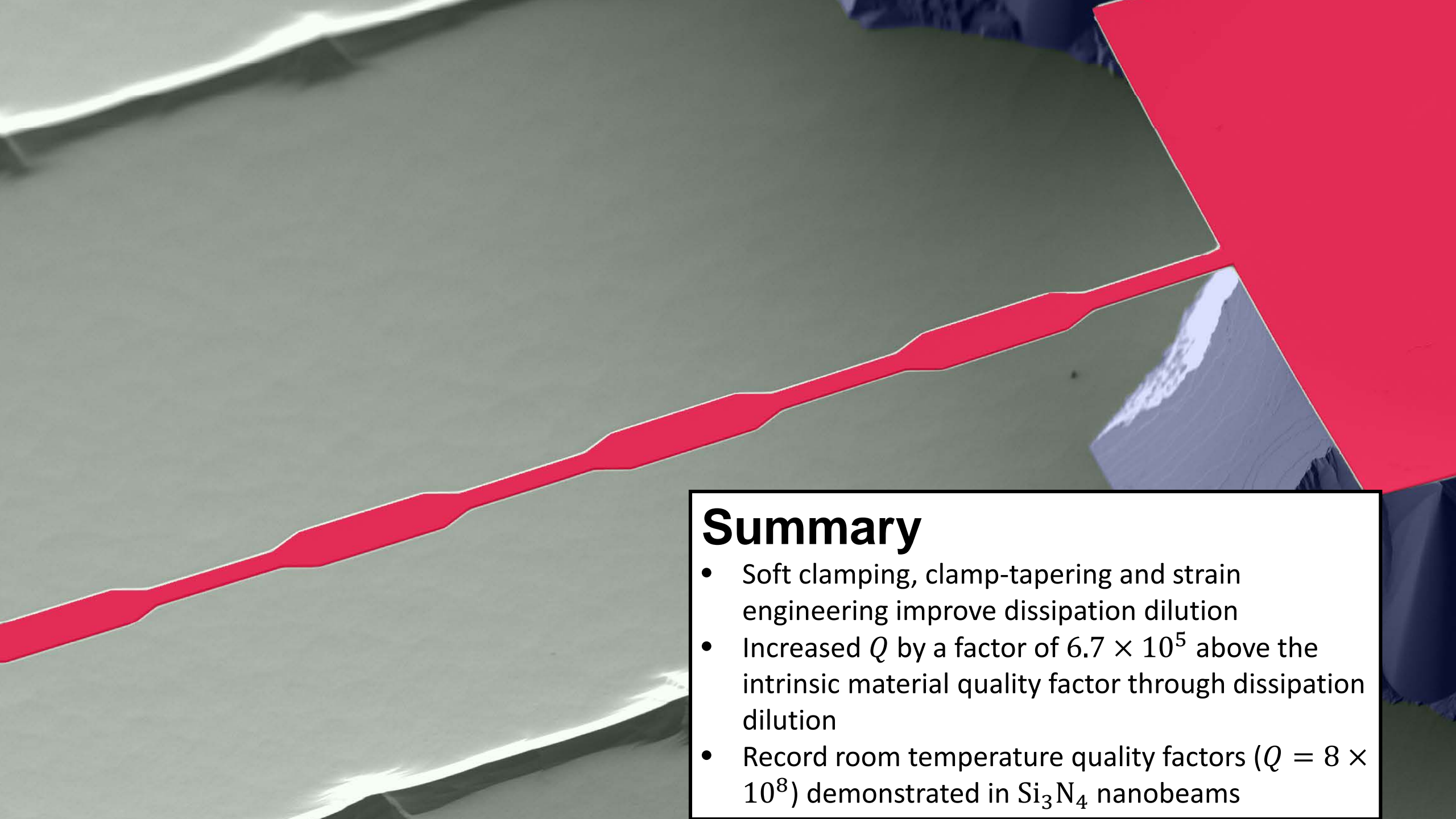
Recently measured device:

$$\omega_m = 450 \text{ kHz} \quad \Gamma_m = 2 \text{ Hz}$$

$$g_0 = 180 \text{ kHz} \quad \kappa = 14 \text{ GHz}$$

$$\rightarrow C_0 \sim 2$$



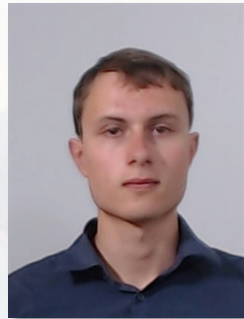


## Summary

- Soft clamping, clamp-tapering and strain engineering improve dissipation dilution
- Increased  $Q$  by a factor of  $6.7 \times 10^5$  above the intrinsic material quality factor through dissipation dilution
- Record room temperature quality factors ( $Q = 8 \times 10^8$ ) demonstrated in  $\text{Si}_3\text{N}_4$  nanobeams

# The team

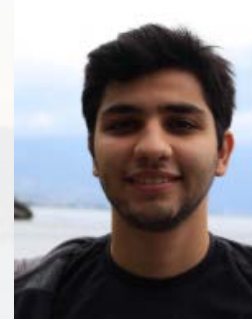
Sergey Fedorov



Alberto Beccari



Mohammad Bereyhi



Amir Ghadimi  
(Now at CSEM)



Amirali Arabmoheghi (Now at IBM Watson)



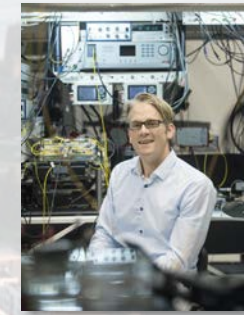
Ryan Schilling (Now at IBM Watson)



Dalziel Wilson (Now at Univ. Arizona)



Tobias Kippenberg



# Why do we care about dissipation?

Dissipation ( $\Gamma_m$ ) limits...

1. Force sensitivity

$$\delta F_{\text{th}} = \sqrt{4k_B T m_{\text{eff}} \Gamma_m}$$

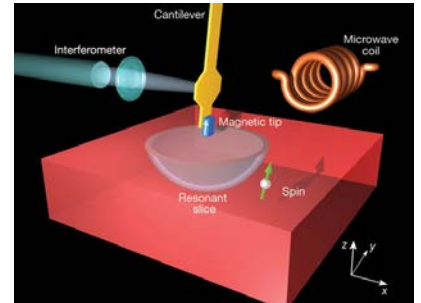
2. Frequency stability

$$S_{\omega\omega}(\omega) = 2 \frac{\langle X_{\text{th}}^2 \rangle}{\langle X_{\text{osc}}^2 \rangle} \frac{\omega^2}{\omega^2 + (\Gamma^2 / 2)^2} \Gamma_m$$

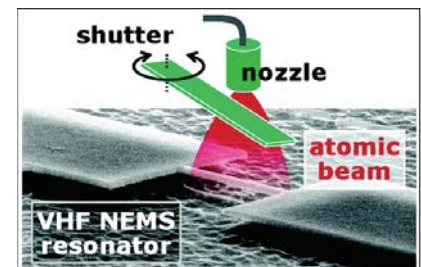
3. Mechanical coherence

$$\Gamma_{\text{th}} = \frac{k_B T}{\hbar \omega_m} \Gamma_m$$

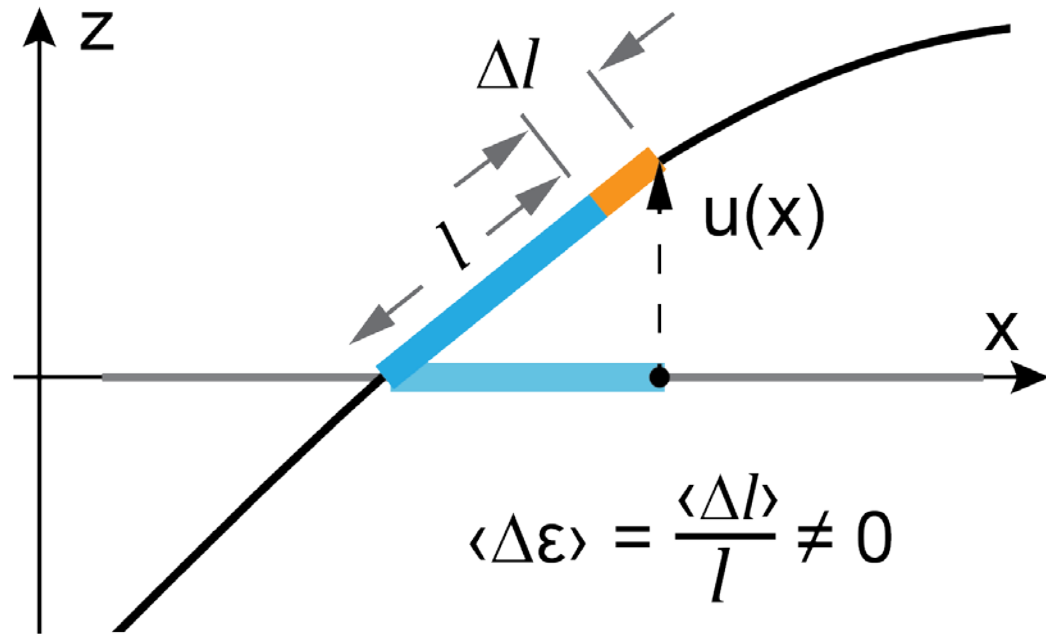
Force sensing  
Rugar et al. *Nature* (2004)



Mass sensing  
R.W. Andrews et al.,  
*Nat. Phys.* (2014)



# Dissipation dilution requirements



$$\Delta l = \frac{1}{2} [u'(x, t)]^2$$

$\Delta \epsilon$	Change in strain
$l$	Segment length
$\Delta l$	Segment elongation
$u(x)$	Mode amplitude

Dissipation dilution requires:

1. Static strain
2. Geometric nonlinearity of strain

Especially strong for flexural (violin) modes

Fedorov, Engelsen et al., *Phys. Rev. B* **99** (2019)

Gonzalez and Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)

# Origin of dissipation dilution in stressed materials

Dissipation dilution: 
$$D_Q = \frac{Q}{Q_{\text{int}}} = 1 + \frac{\langle W_{\text{dil}}(t) \rangle}{\langle W_{\text{lossy}}(t) \rangle}$$

Increasing static strain increases the lossless potential more than the lossy potential

Lossless potential: 
$$\langle W_{\text{dil}}(t) \rangle = E \int \epsilon \langle \Delta \epsilon(t) \rangle dV$$

$$\sigma = E e^{-i\phi} \epsilon \quad Q_{\text{int}} = 1 / \phi$$

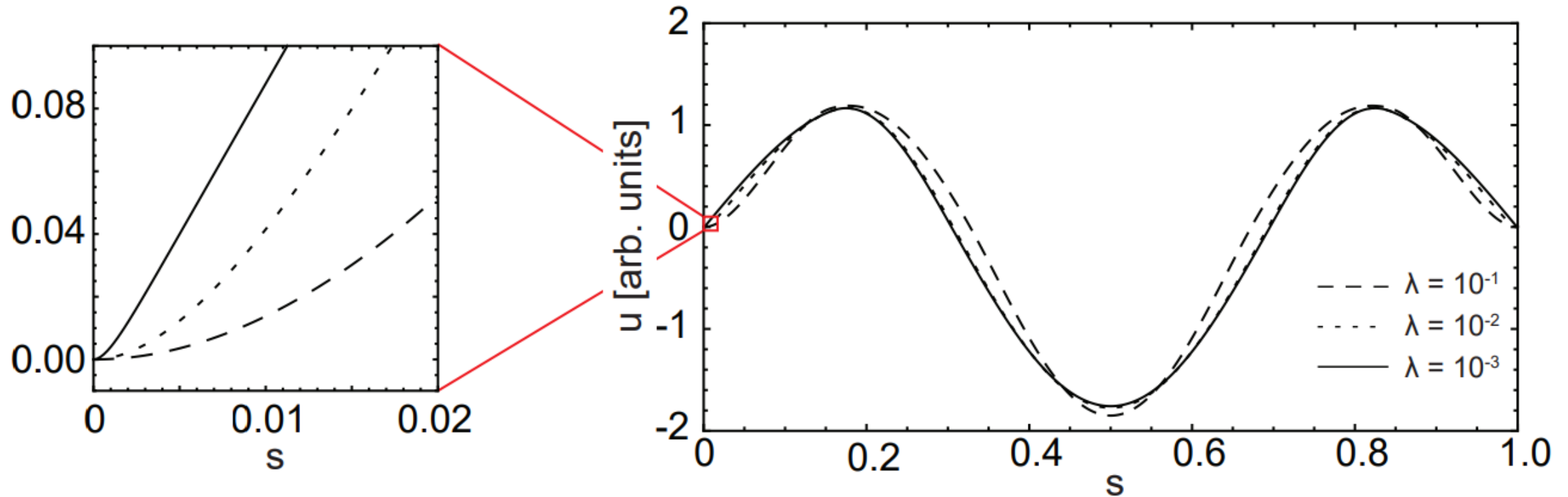
Lossy potential: 
$$\langle W_{\text{lossy}}(t) \rangle = \frac{E}{2} \int \langle [\Delta \epsilon(t)]^2 \rangle dV$$

$Q_{\text{int}}$	Intrinsic quality factor
$E$	Young's modulus
$\epsilon$	Static strain
$\phi$	Loss angle
$\sigma$	Stress
$\Delta \epsilon$	Change in strain

Fedorov, Engelsen et al., *Phys. Rev. B* **99** (2019)

Gonzalez and Saulson, *J. Acoust. Soc. Am.* **96.1**(1994)

# Curvature in clamping region of uniform beam

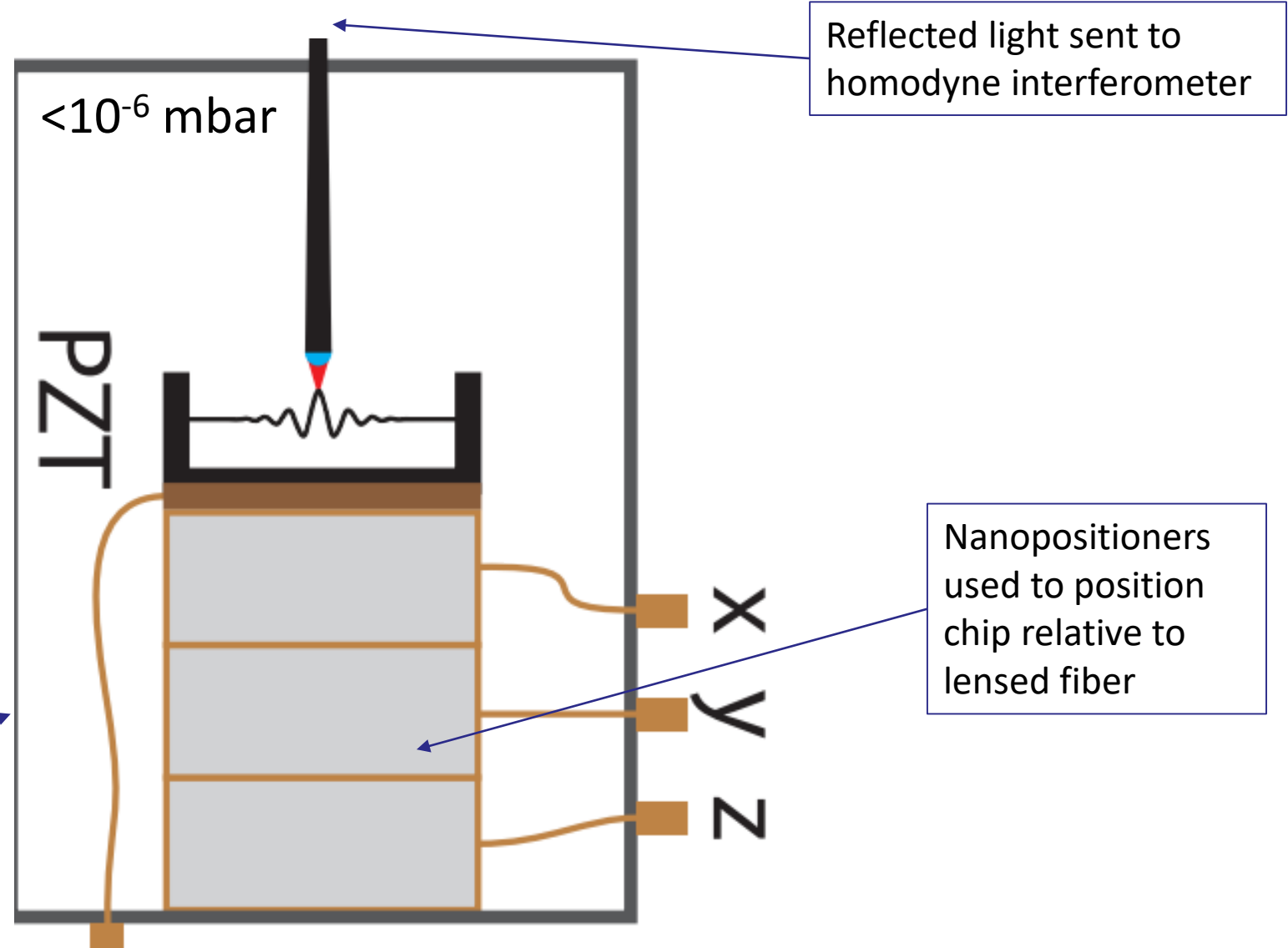


$s = x/L$ : the normalized beam length

Note that the characteristic length of clamping region is proportional to  $\lambda$

# Mechanical characterization setup

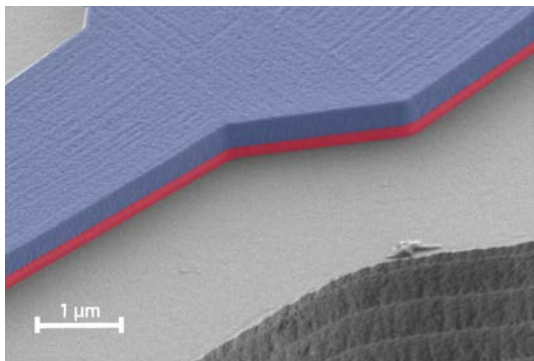
Can resolve  
Brownian motion  
of mechanical  
modes



# Si<sub>3</sub>N<sub>4</sub> nanobeam process flow

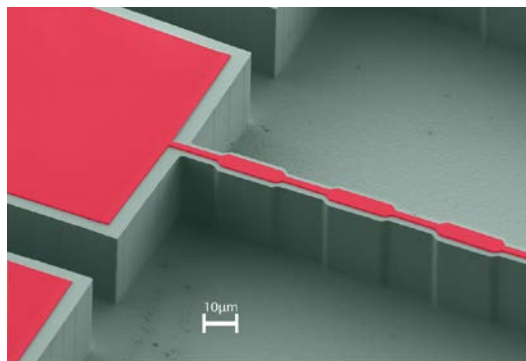
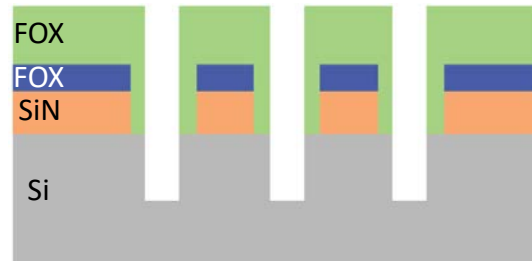
## Patterning

Structures are patterned using electron beam lithography



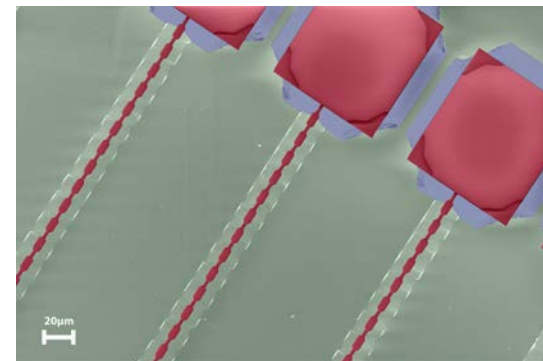
## Gap definition

Upscaled version of the first lithography followed by deep reactive ion etching



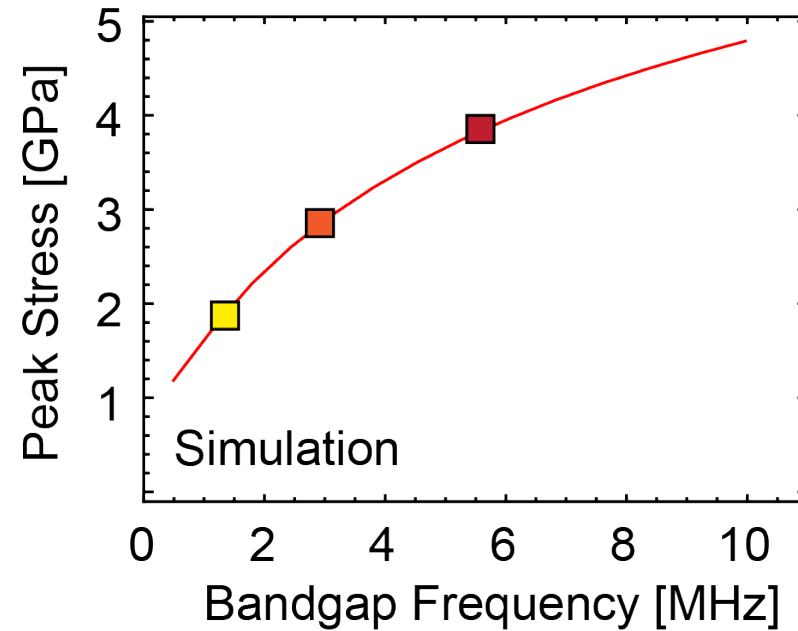
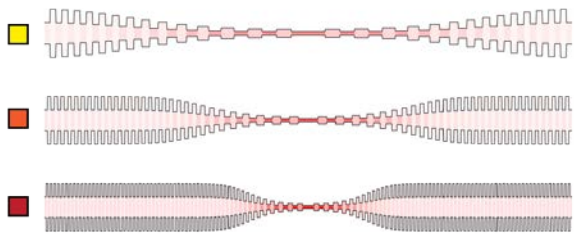
## Undercut

Si undercut using KOH

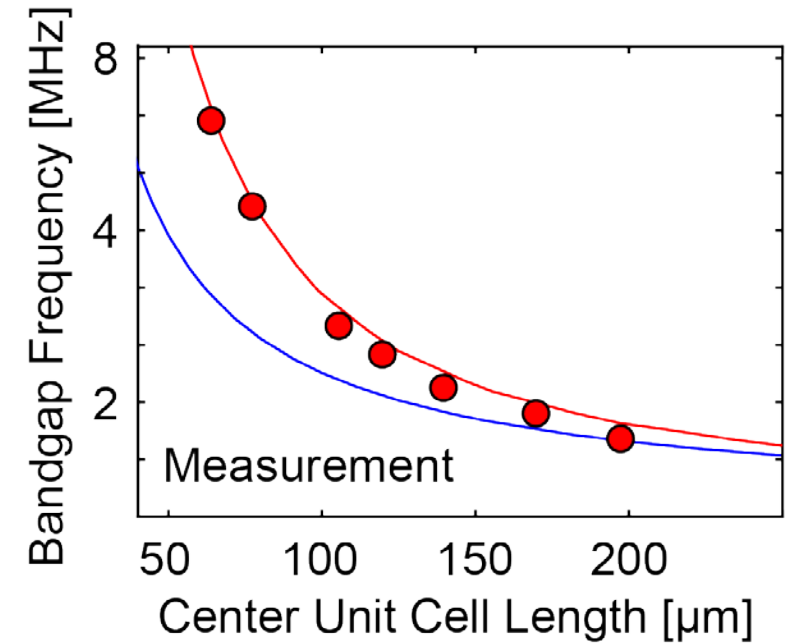




# How do we know what stress we achieve?

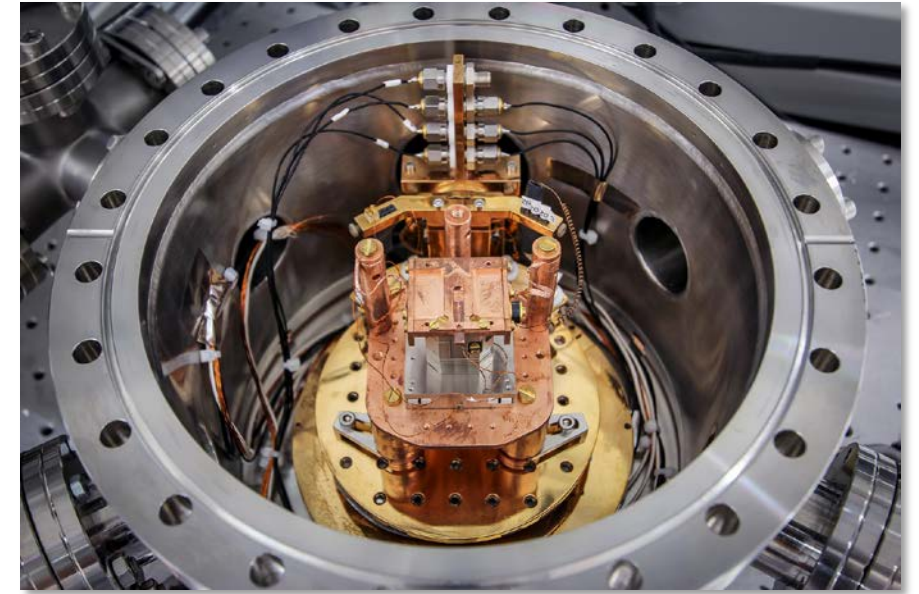
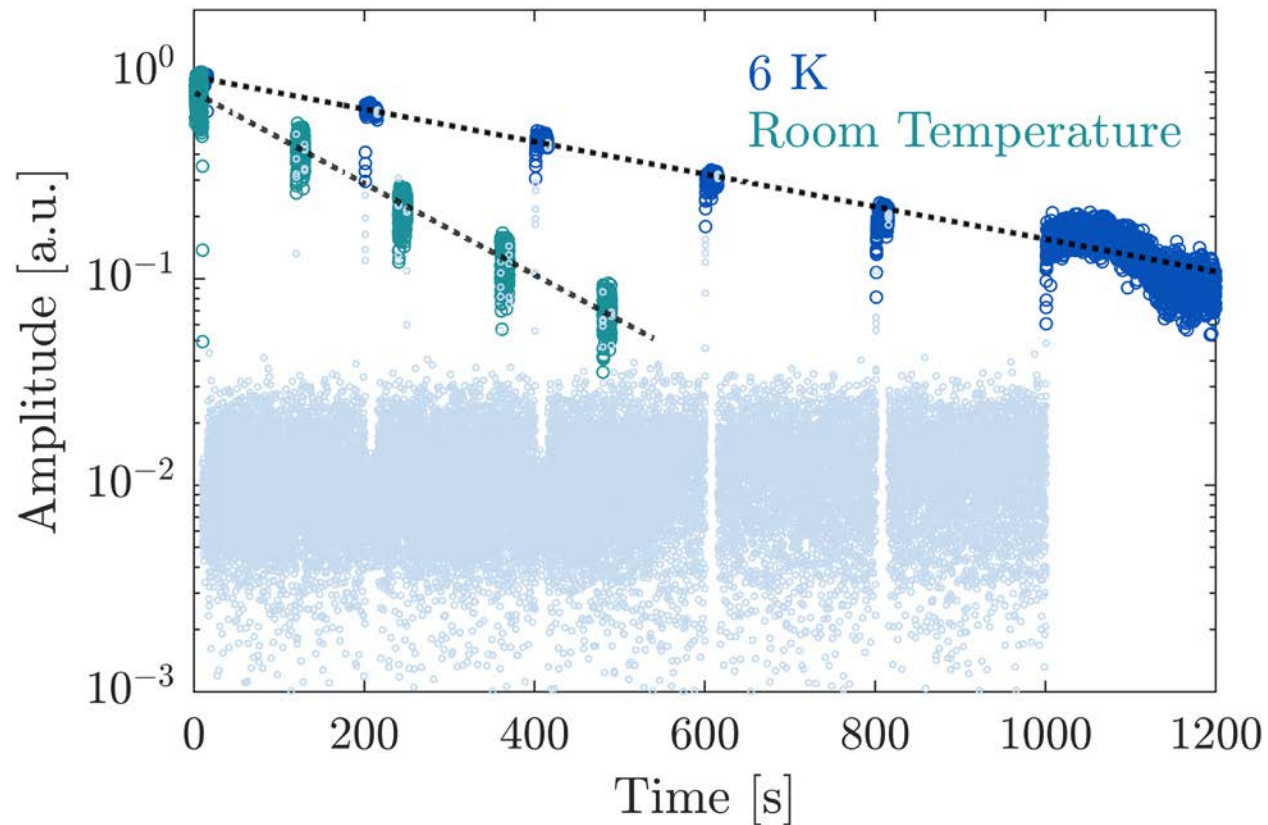


Expected bandgap frequency of the three geometries on the left shown as squares



- **Blue line:** expected bandgap frequency based on unit cell length
- **Red line** calculated including stress

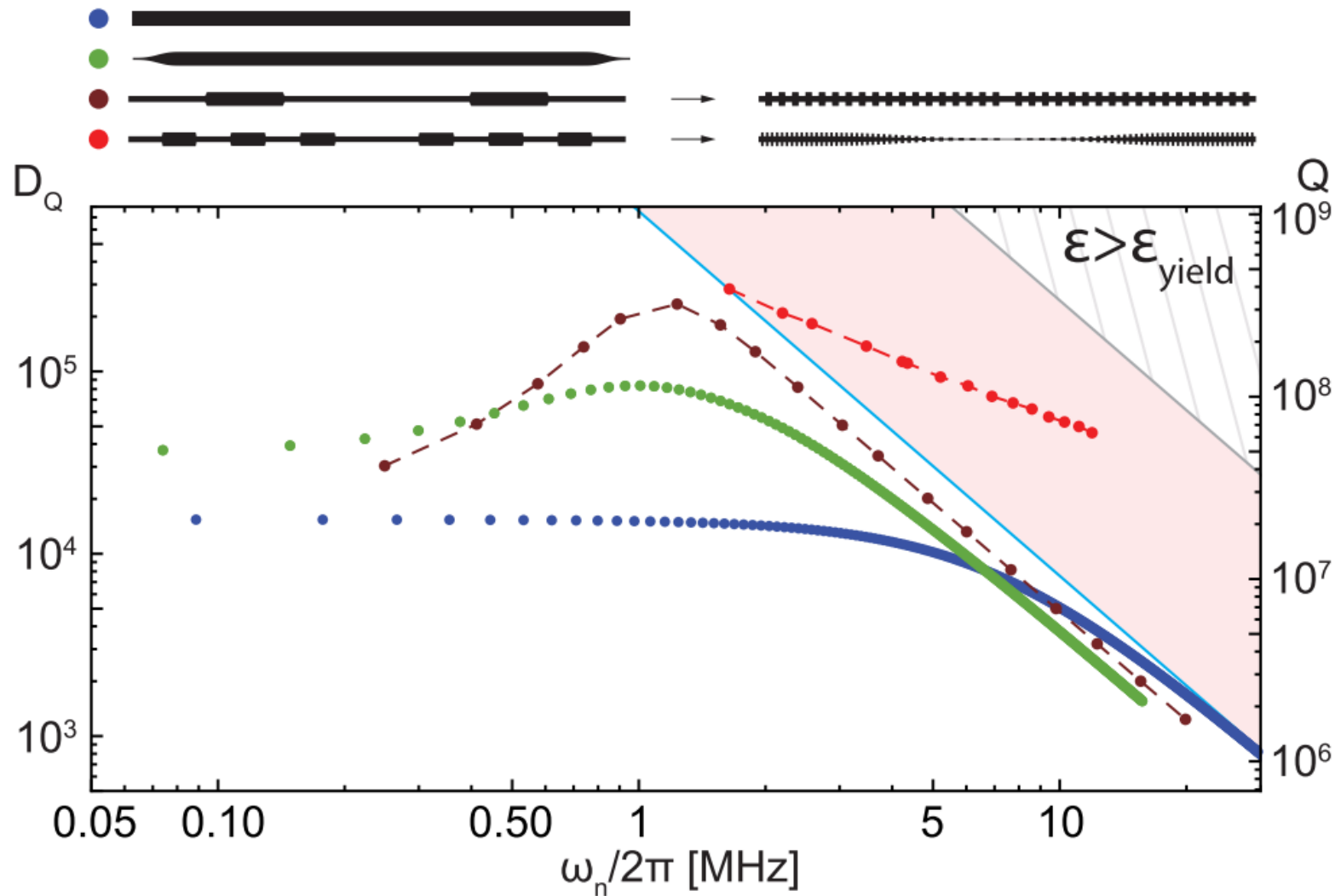
# Cryogenic characterization



300 K		5.8 K	
$\Omega_m/2\pi$ [MHz]	$Q$ [ $\cdot 10^6$ ]	$\Omega_m/2\pi$ [MHz]	$Q$ [ $\cdot 10^6$ ]
1.020	650	0.985	<b>1480</b>
0.986	520	0.958	<b>1420</b>
0.848	130	0.823	<b>1340</b>
0.849	160	0.823	<b>1020</b>

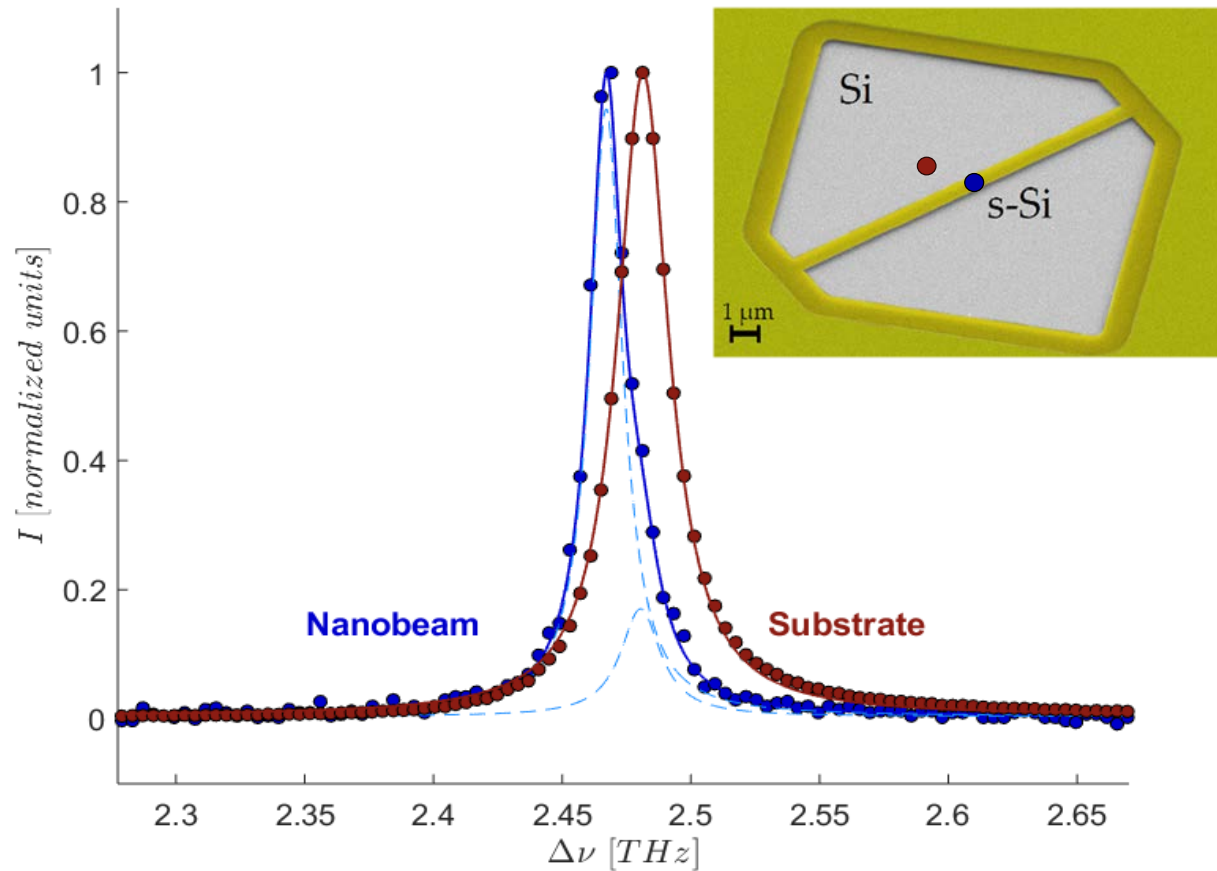
- Enhancement factor ranging from 2-10
- Frequency shift likely due to thermal expansion mismatch

# Overview of dissipation engineering techniques

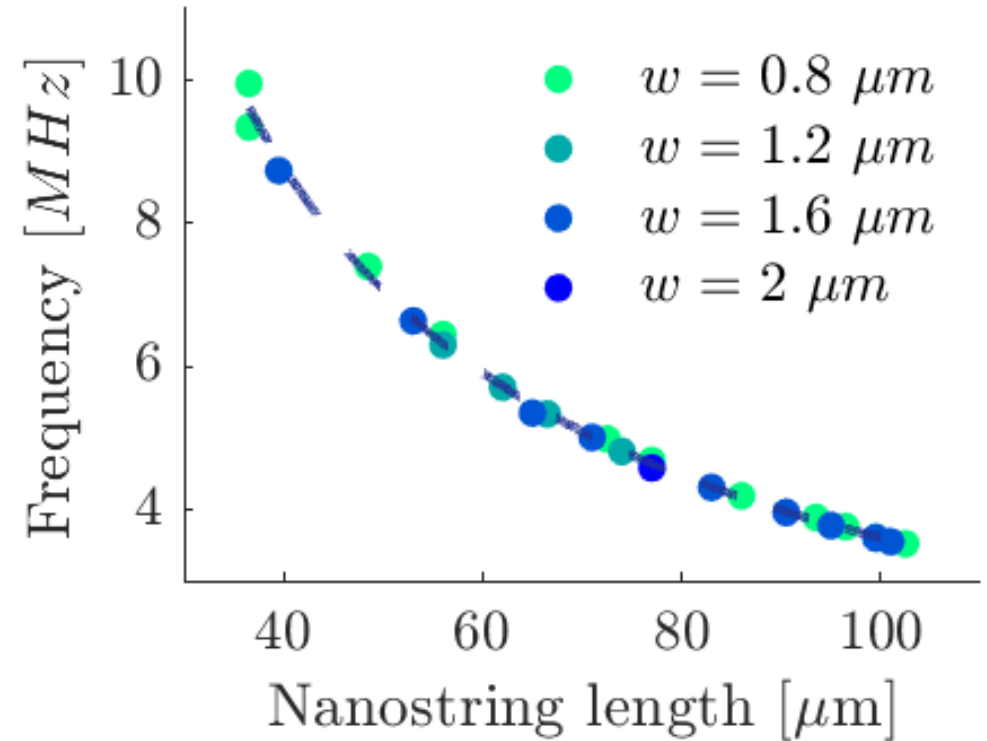


Values representative of  
3-mm long, 20-nm thick  
 $\text{Si}_3\text{N}_4$  beam

# Strained silicon stress



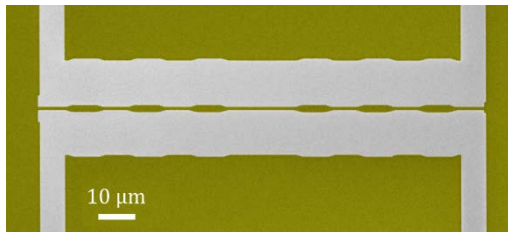
$$f_1 = \sqrt{\frac{\sigma(1-\nu)}{\rho}} \frac{1}{2L}$$



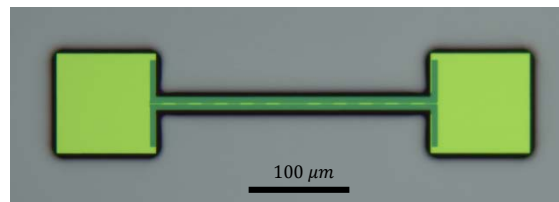
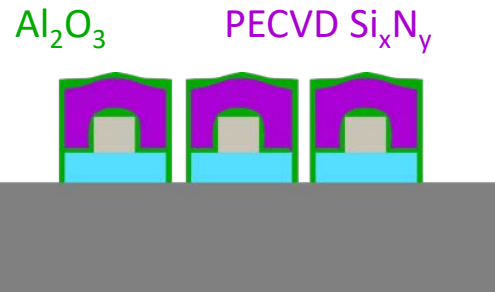
Verified that stress is in fact around 1.2 GPa after fabrication

# Strained silicon fabrication process

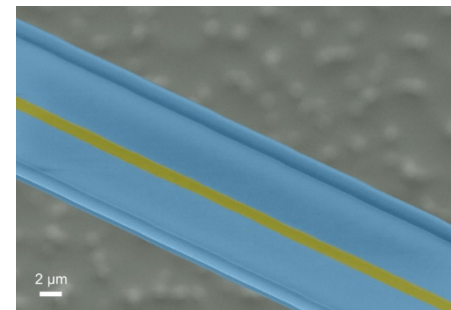
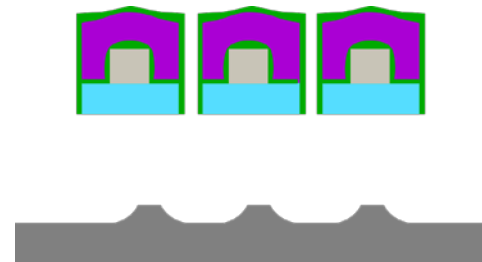
## Patterning



## Encapsulation



## Undercut



## Selective etch

