

Many facets of Polaritons

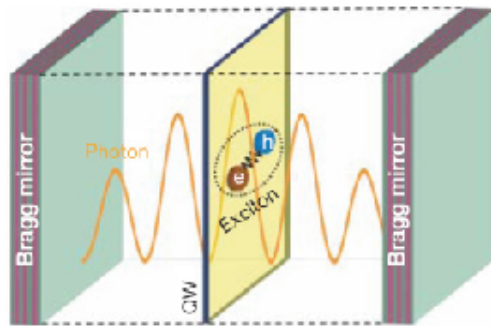
Marcia T. Portella Oberli



Advanced Semiconductors for Photonics and Electronics Lab

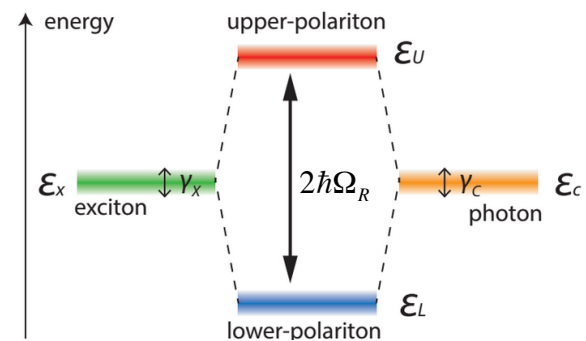
Microcavity Exciton Polaritons

Microcavity polaritons arise from the strong coupling of cavity photons to quantum well excitons



J. Kasprzak *et al.*, Nature (London) **443**, 409 (2006).

The eigenstates of the system are mixed exciton-photon quasi particles: polaritons



Hamiltonian in the strong coupling:

$$\hat{H} = E_X \hat{x}^+ \hat{x} + E_C \hat{c}^+ \hat{c} + \hbar \Omega_R (\hat{x}^+ \hat{c} + \hat{c}^+ \hat{x})$$

$$\rightarrow \hat{H} = \begin{pmatrix} E_C & \hbar \Omega_R \\ \hbar \Omega_R & E_X \end{pmatrix}$$

Diagonalization:

$$\hat{H} = E_{LP} \hat{a}^+ \hat{a} + E_{UP} \hat{b}^+ \hat{b} \quad \leftarrow \text{polariton basis}$$

$$\rightarrow \begin{pmatrix} \hat{a} \\ \hat{b} \end{pmatrix} = \begin{pmatrix} X & C \\ -C & X \end{pmatrix} \begin{pmatrix} \hat{x} \\ \hat{c} \end{pmatrix}$$

$$\Rightarrow E_{L,U} = \frac{1}{2} \left(E_C + E_X \mp \sqrt{(E_C - E_X)^2 + (2\Omega_R)^2} \right)$$

Hopfield coefficients

$$|X|^2 + |C|^2 = 1$$

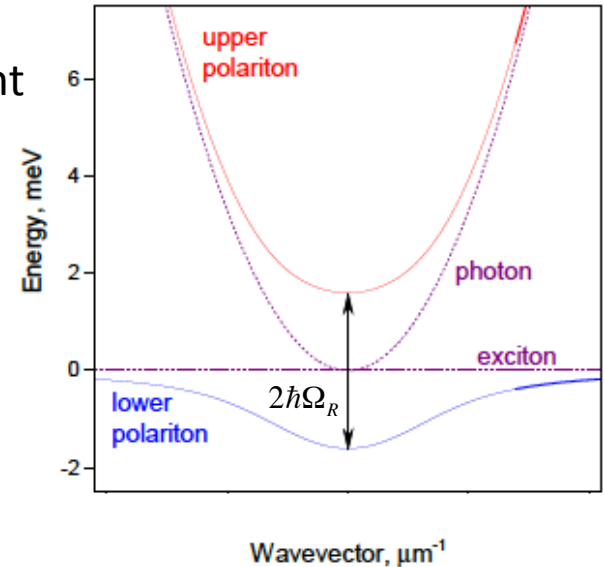
$$\hat{a} = X\hat{x} + C\hat{c}$$

$$\hat{b} = C\hat{x} - X\hat{c}$$

Microcavity Exciton Polaritons

Features

- Polaritons are composite bosons
 - low effective mass provided by their photonic content
 - nonlinearity provided by the excitonic content
- Easily accessible : optical excitation and detection

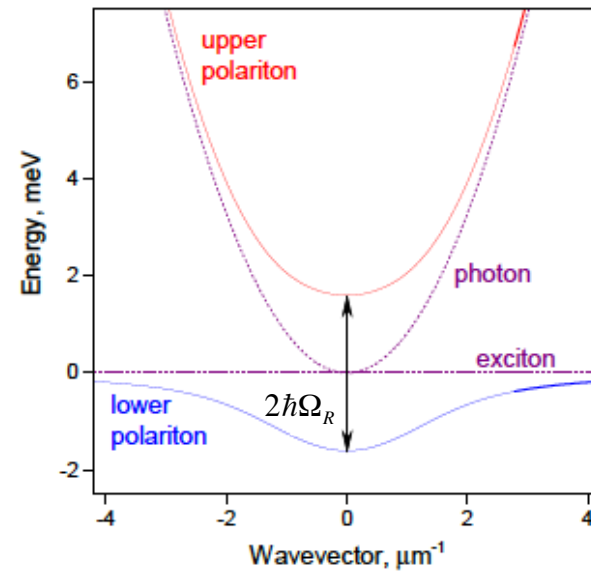
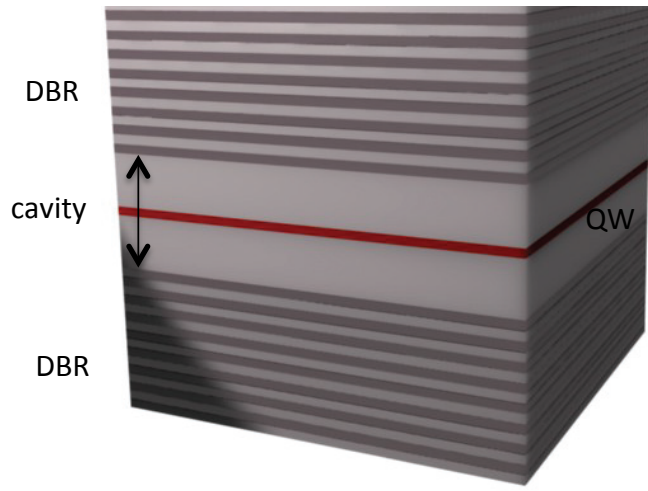


Dynamics \implies Gross-Pitaevskii equation

$$i\hbar \frac{\partial \psi}{\partial t} = \left[E - \frac{\hbar^2}{2m} \nabla^2 + \alpha_1 |\psi|^2 - i\gamma \right] \psi$$

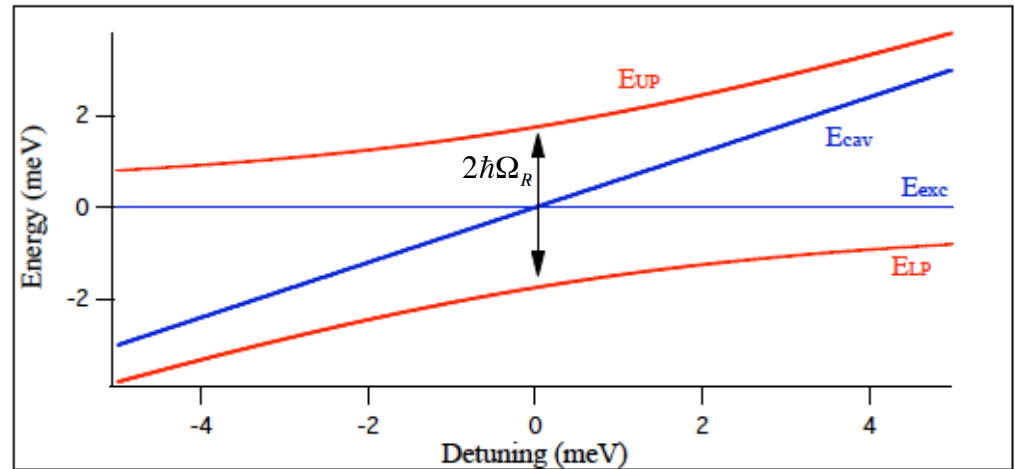
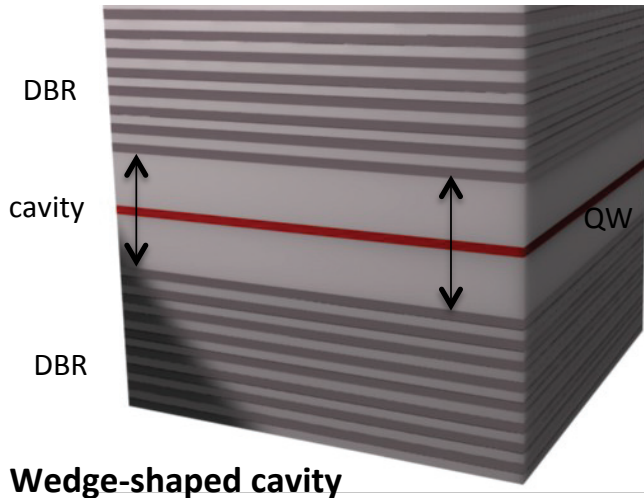
Microcavity Exciton Polaritons

Polaritons in planar microcavity

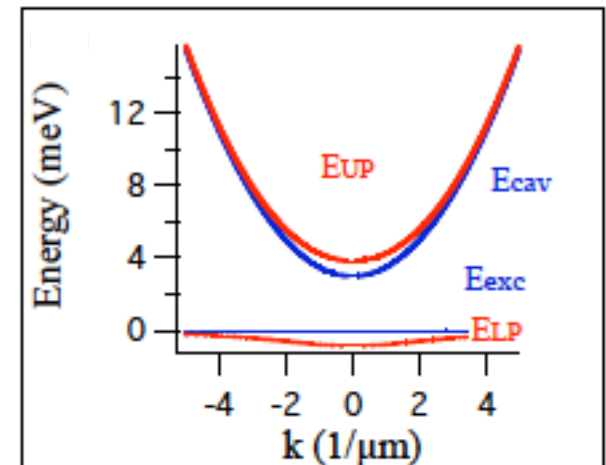
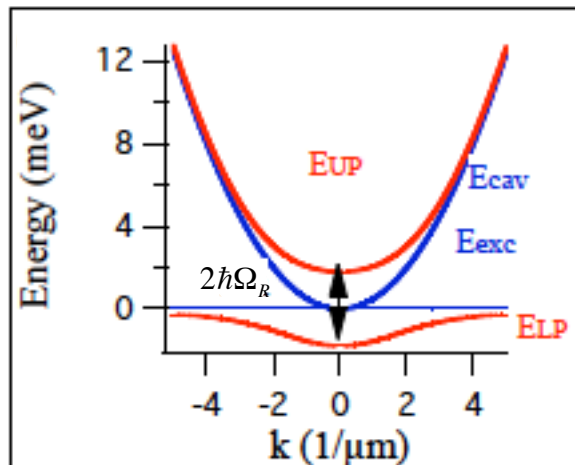
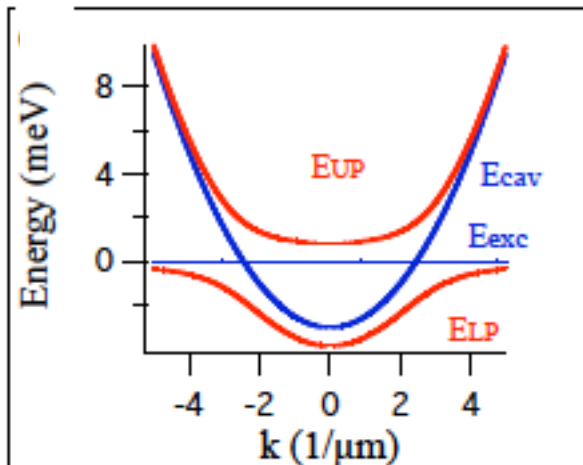


Microcavity Exciton Polaritons

Polaritons in planar microcavity



$$E_{LP,UP}(k) = \frac{1}{2} \left(E_X + E_c(k) \mp \sqrt{\delta^2 + 4\Omega_R^2} \right)$$



Cavity detuning

$|\text{polariton}\rangle = X |\text{exciton}\rangle + C |\text{photon}\rangle$

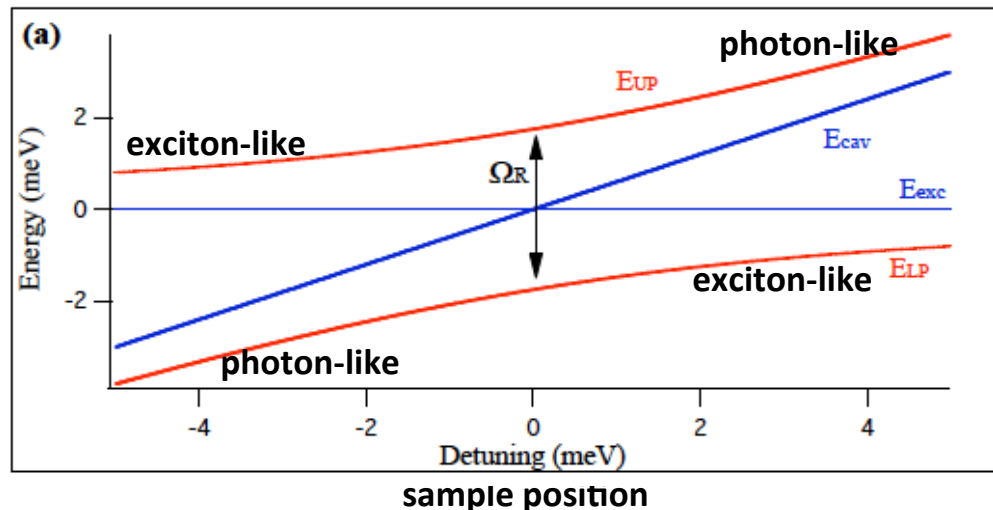
Hopfield coefficients

excitonic fraction

$$|X|^2 = \frac{1}{2} \left(1 + \frac{\delta}{\sqrt{\delta^2 + 4\hbar^2\Omega^2}} \right)$$

photonic fraction

$$|C|^2 = \frac{1}{2} \left(1 - \frac{\delta}{\sqrt{\delta^2 + 4\hbar^2\Omega^2}} \right)$$

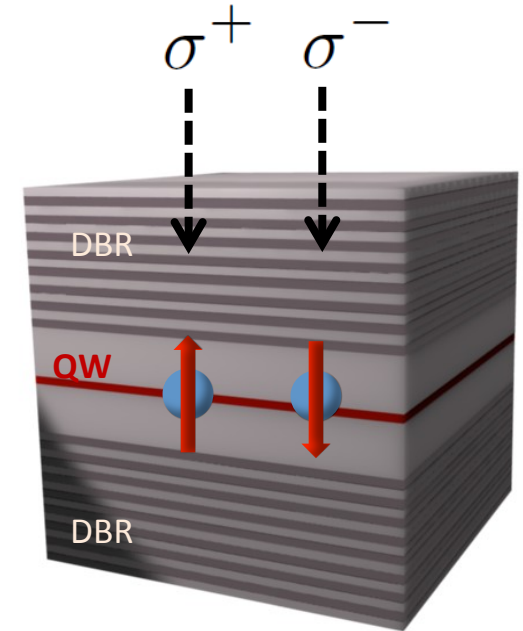


Two spin states of polariton

Polariton has two spin projections: spin **up** and **down**

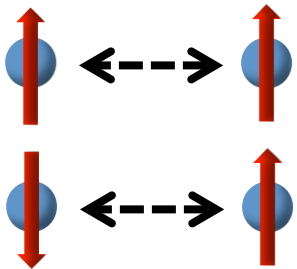
Spin up exciton couples σ^+ cavity photon polarization

Spin down exciton couples σ^- cavity photon polarization



Polariton Spinor Gross-Pitaevskii equation

$$i\hbar \dot{\psi}_{\pm} = \left[E_{\pm} - \frac{\hbar^2}{2m} \nabla^2 + \underbrace{\alpha_1}_{\Delta E} |\psi_{\pm}|^2 + \underbrace{\alpha_2}_{\Delta E} |\psi_{\mp}|^2 - i\gamma \right] \psi_{\pm}$$

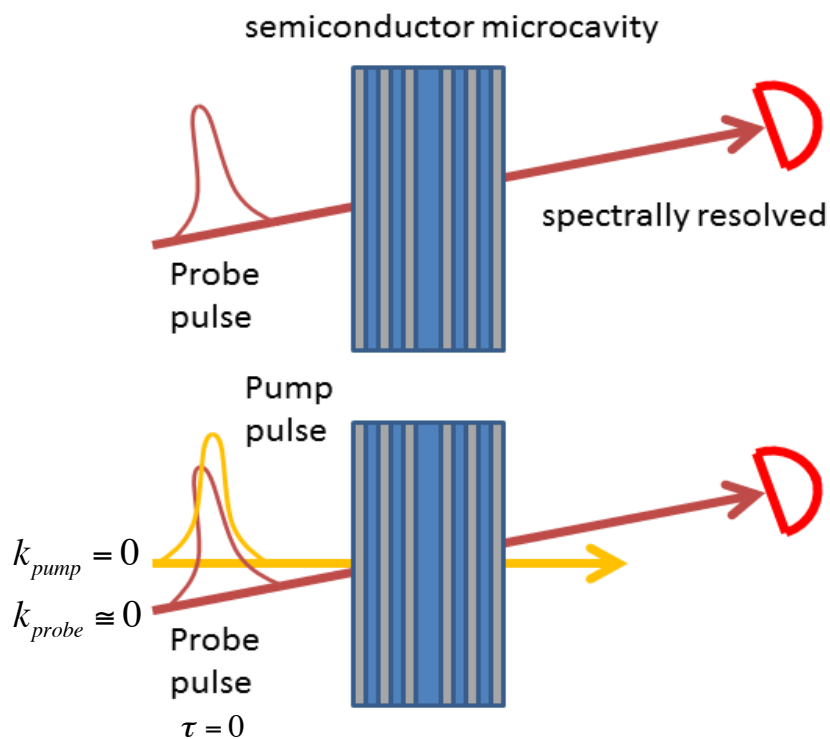


Repulsive polariton interaction with **parallel** spins

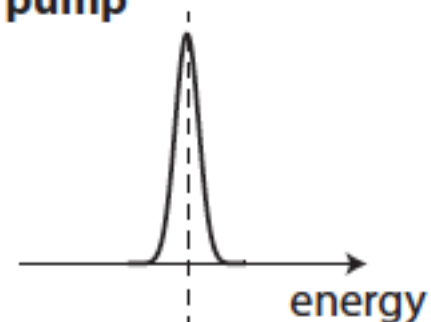
Attractive polariton interaction with **anti-parallel** spins

Spectrally resolved pump-probe spectroscopy

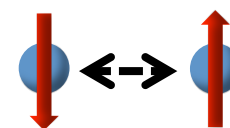
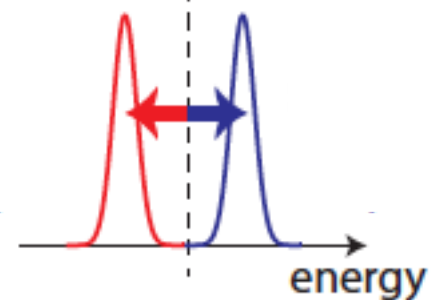
Pump-probe spectroscopy



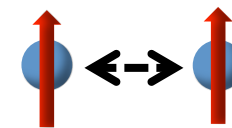
without pump



with pump



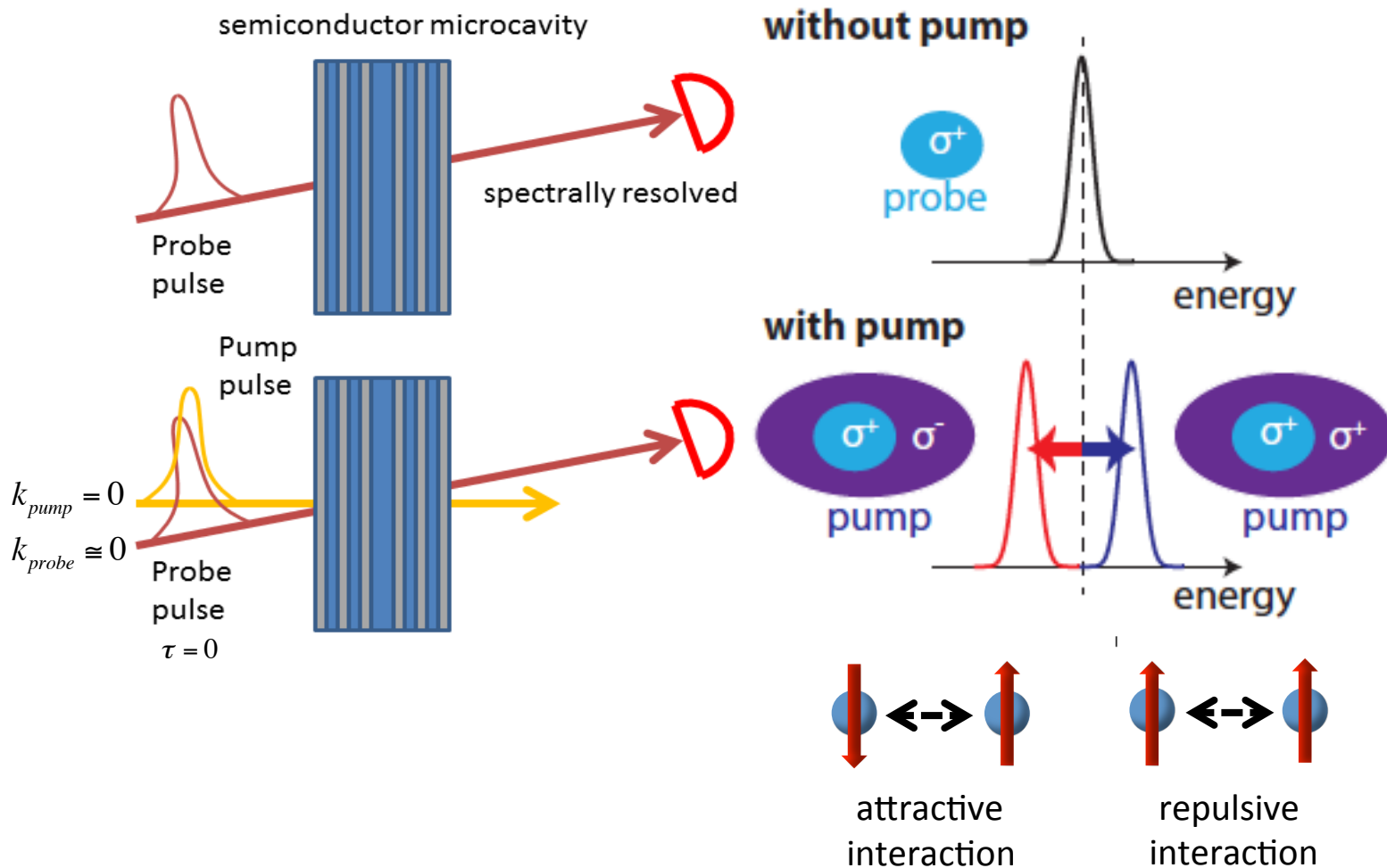
attractive
interaction



repulsive
interaction

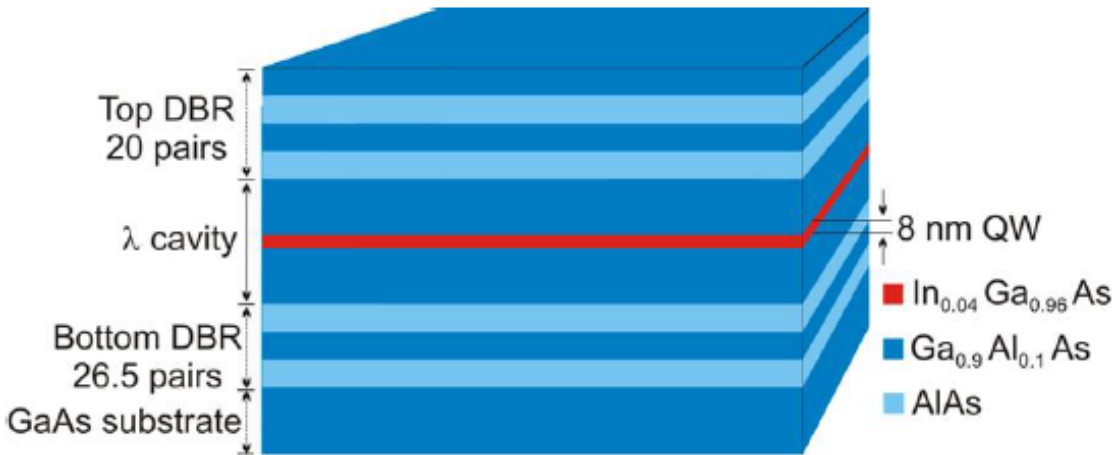
Spectrally resolved pump-probe spectroscopy

Pump-probe spectroscopy

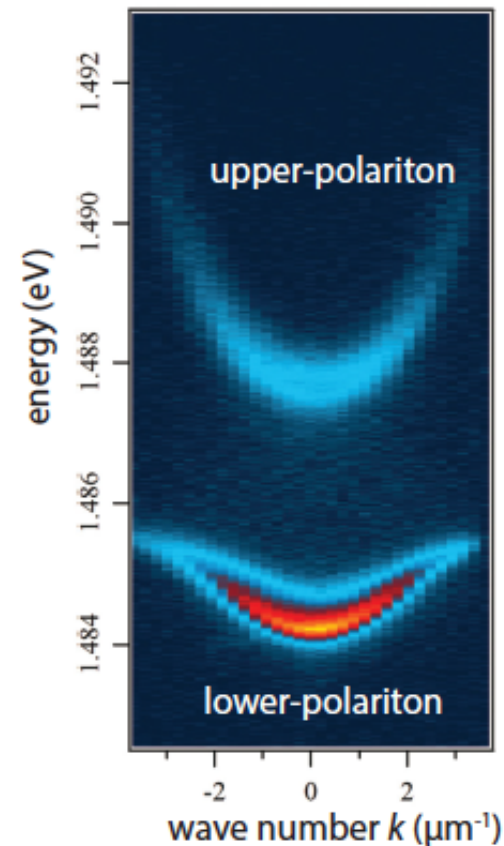


Sample

Microcavity sample



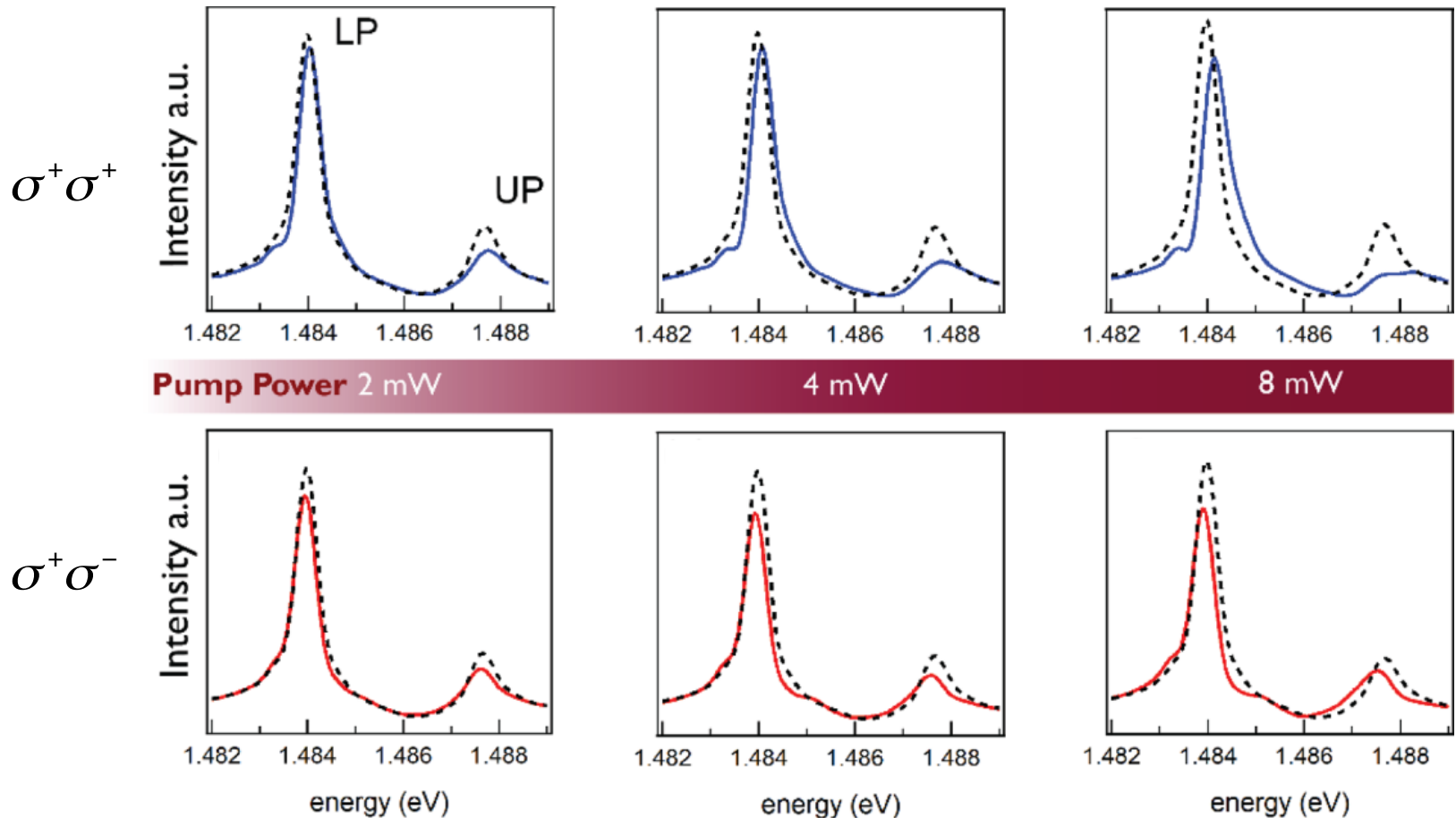
Photoluminescence spectrum



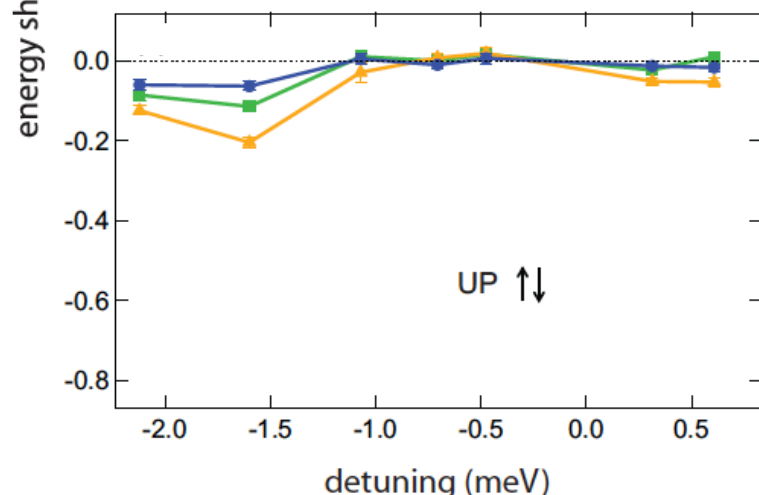
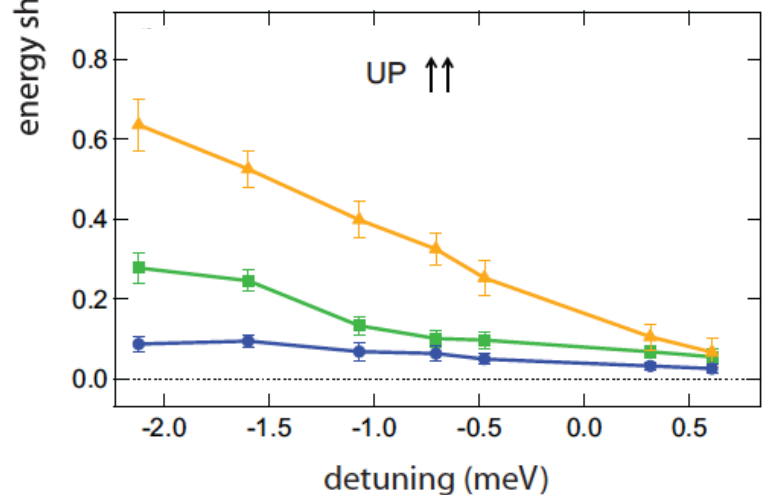
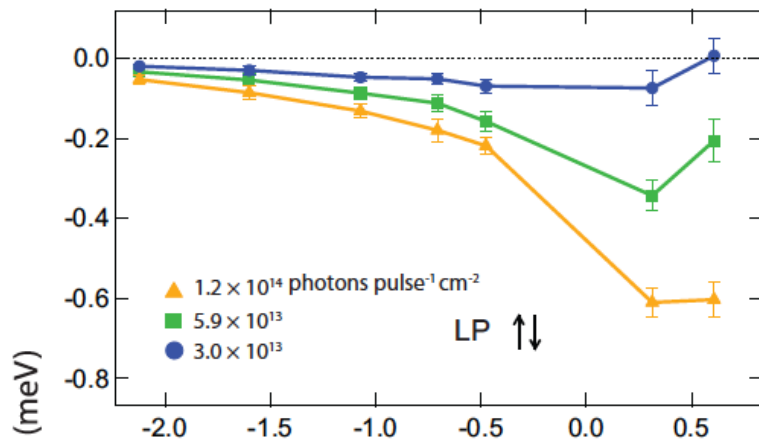
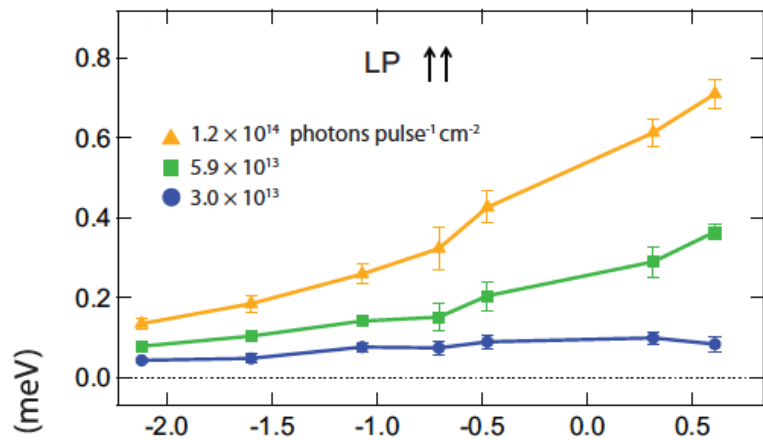
$$T = 5K \quad \delta = -0.8meV$$

Polariton spinor interactions

Pump probe signal

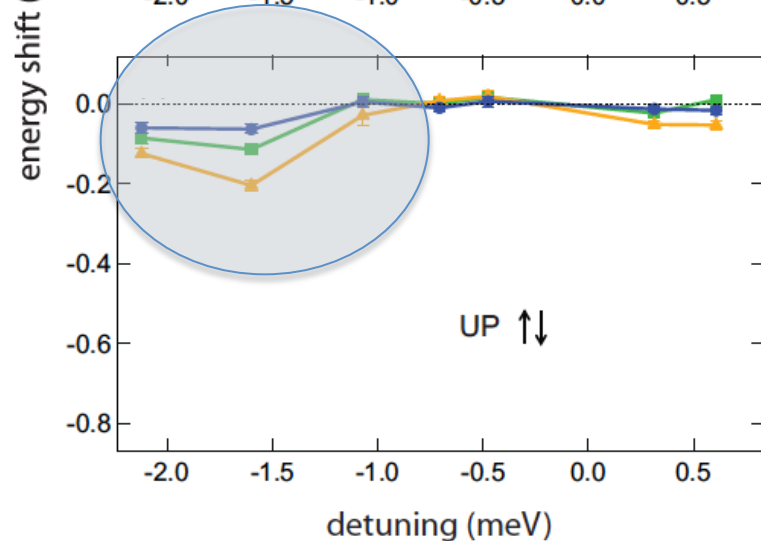
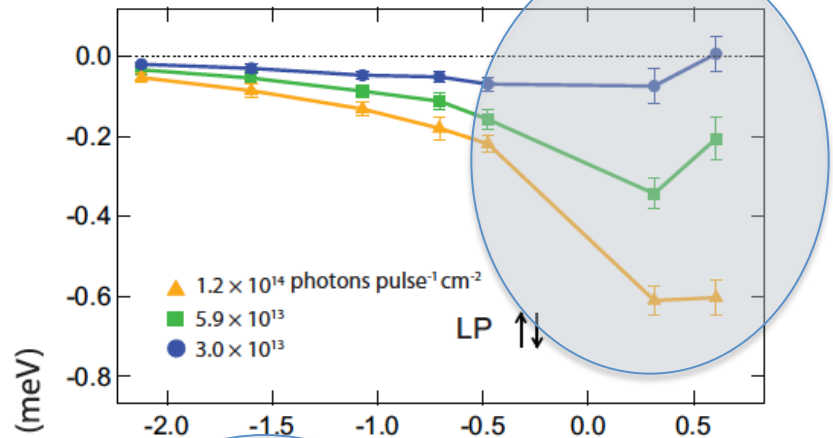
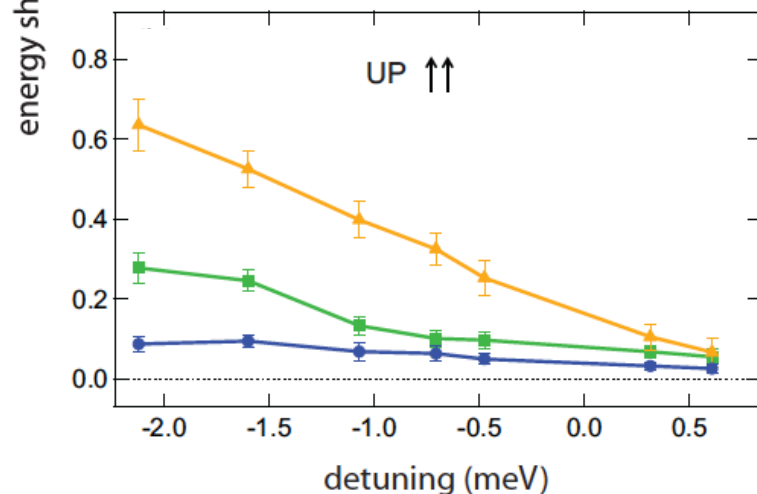
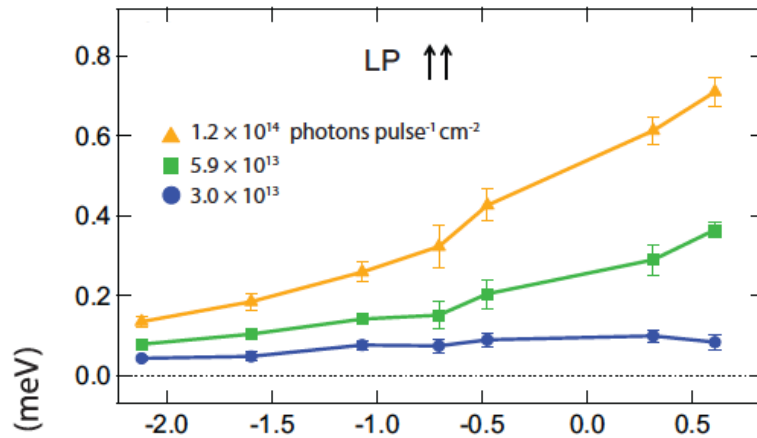


Polariton spinor interactions



Polariton spinor interactions

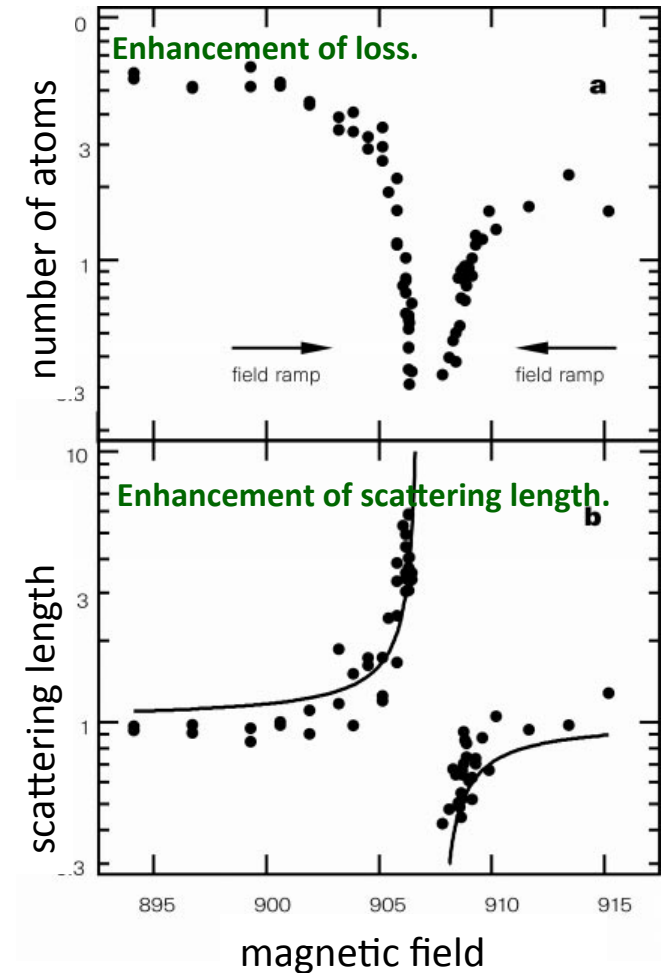
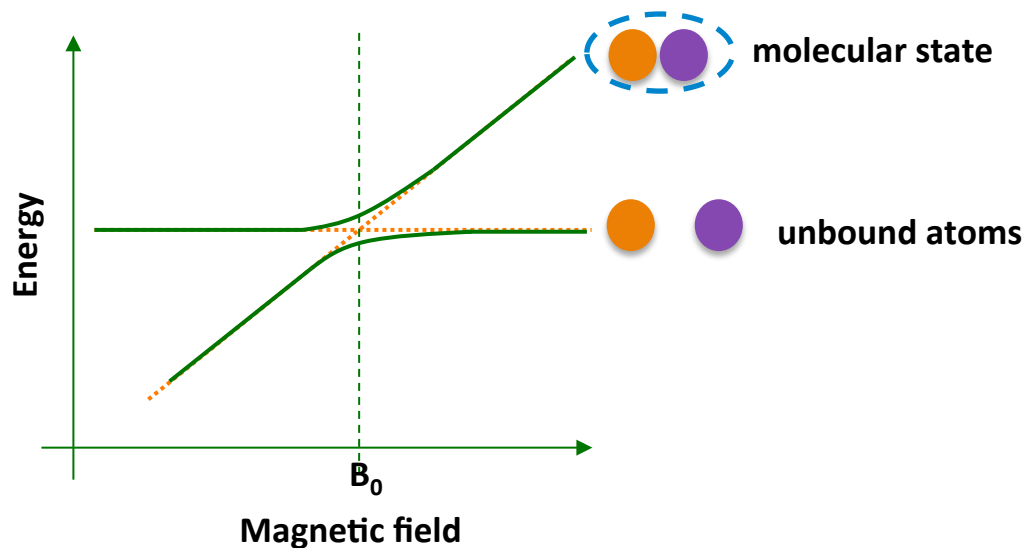
Deviation from the Hopfield dependence



Feshbach resonance

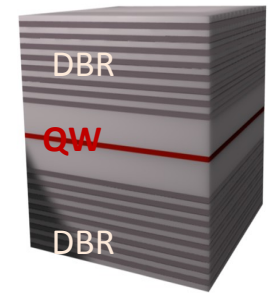
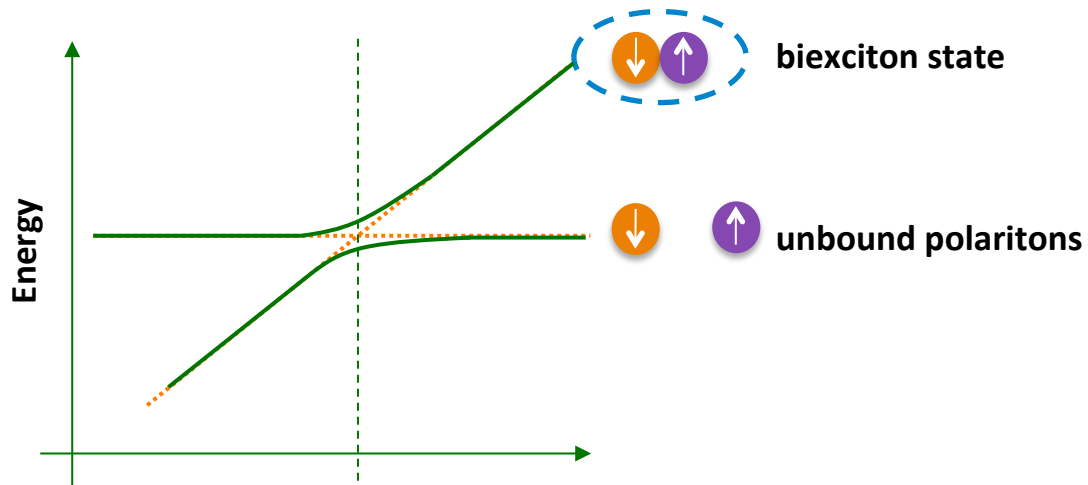
Feshbach resonance in cold atoms

A Feshbach resonance occurs when the energy of two interacting free atoms comes to resonance with a molecular bound state.



Polaritonic Feshbach resonance

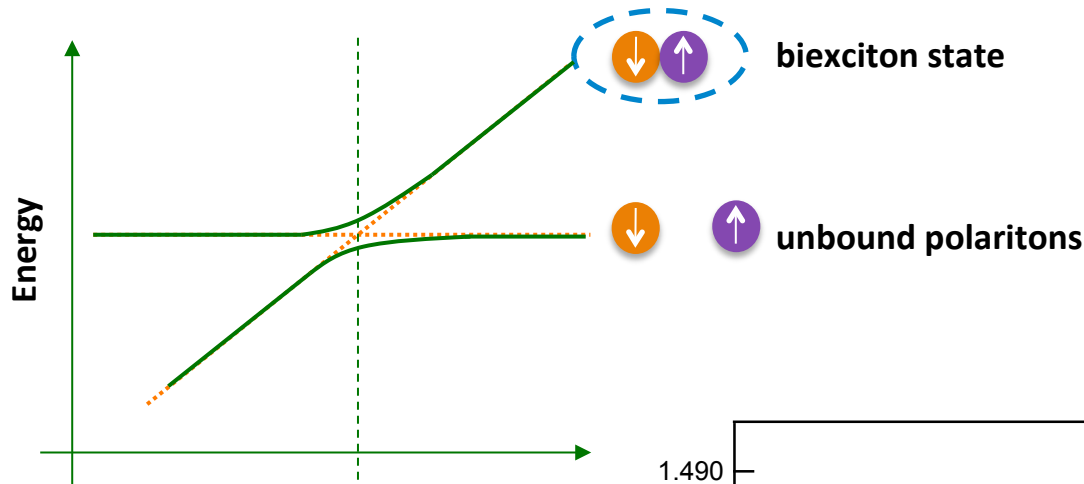
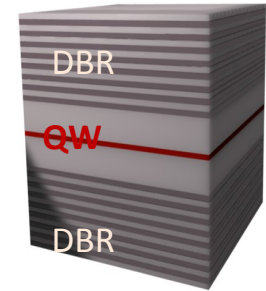
Feshbach resonance in microcavity polaritons



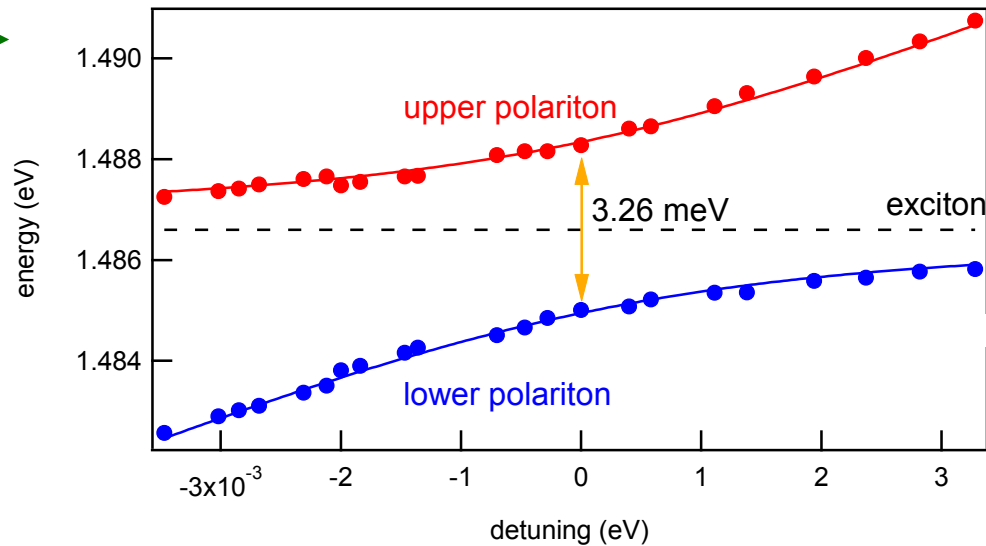
By tuning the relative energy

Polaritonic Feshbach resonance

Feshbach resonance in microcavity polaritons

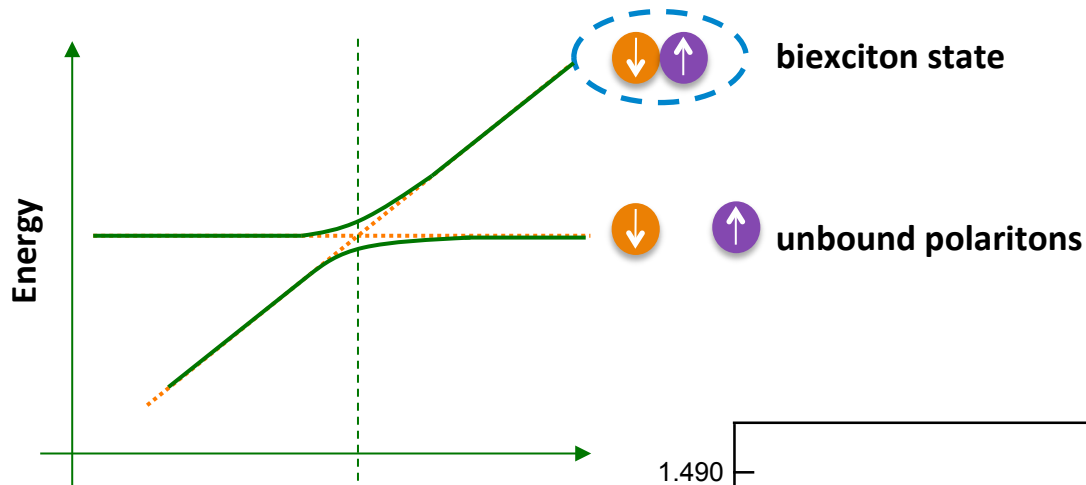
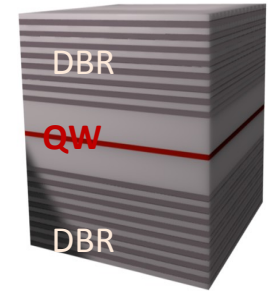


By tuning the relative energy

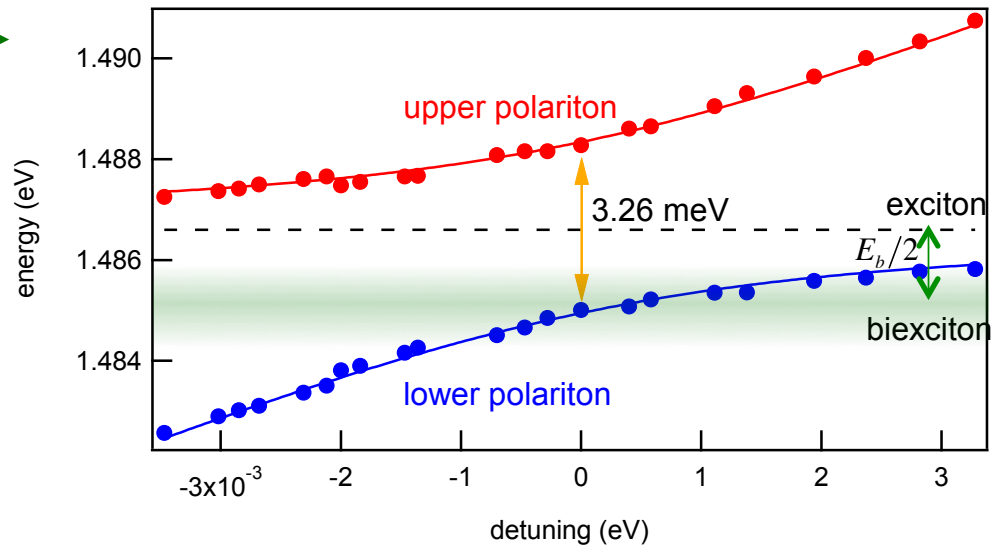


Polaritonic Feshbach resonance

Feshbach resonance in microcavity polaritons

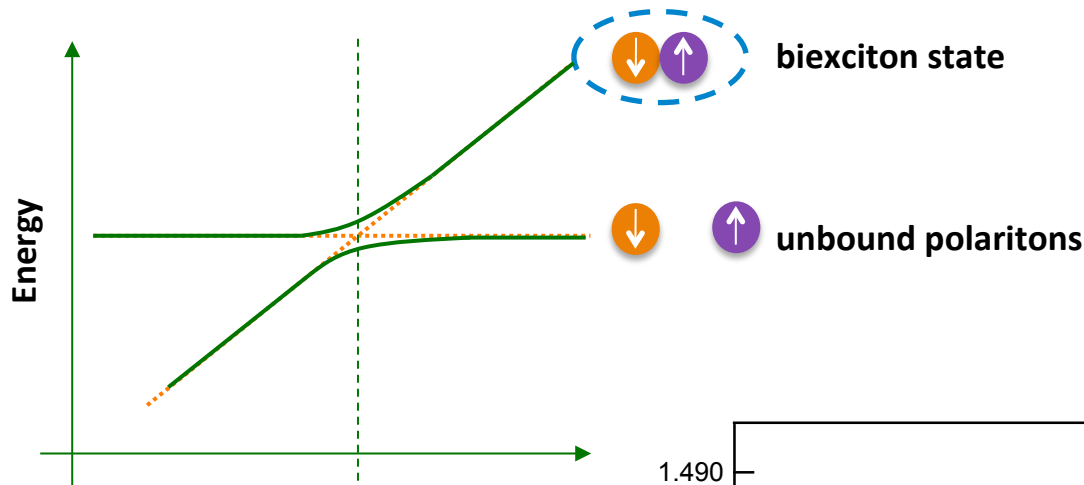
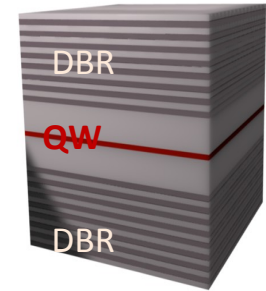


By tuning the relative energy

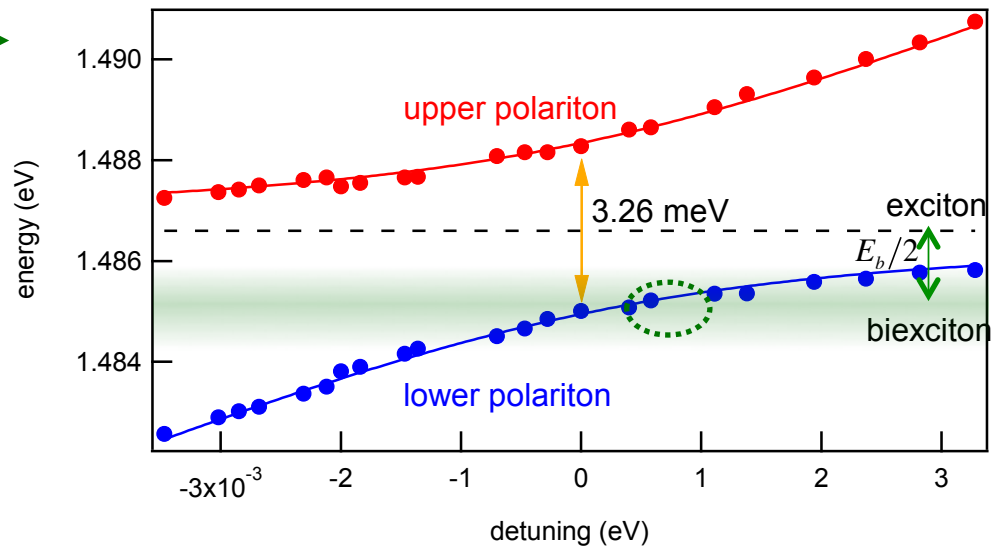


Polaritonic Feshbach resonance

Feshbach resonance in microcavity polaritons



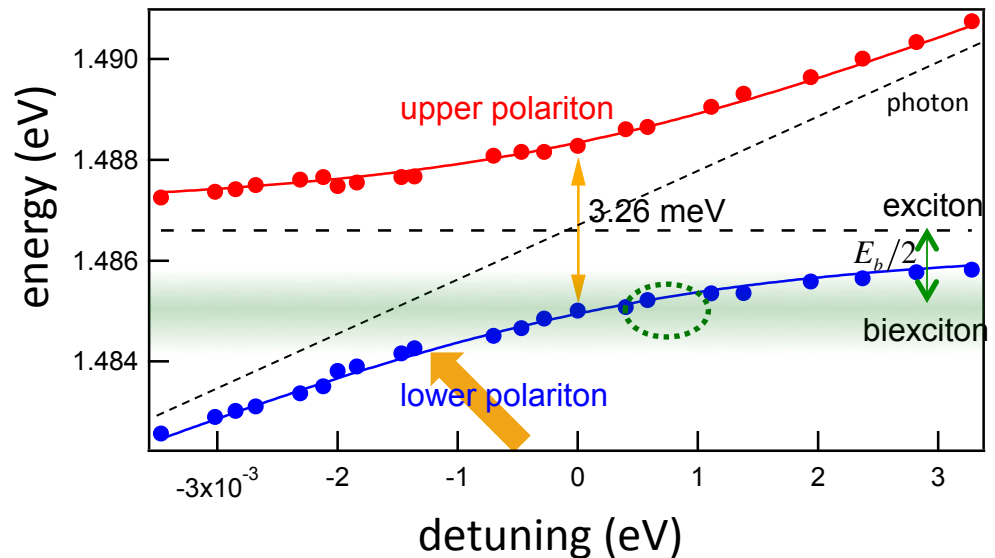
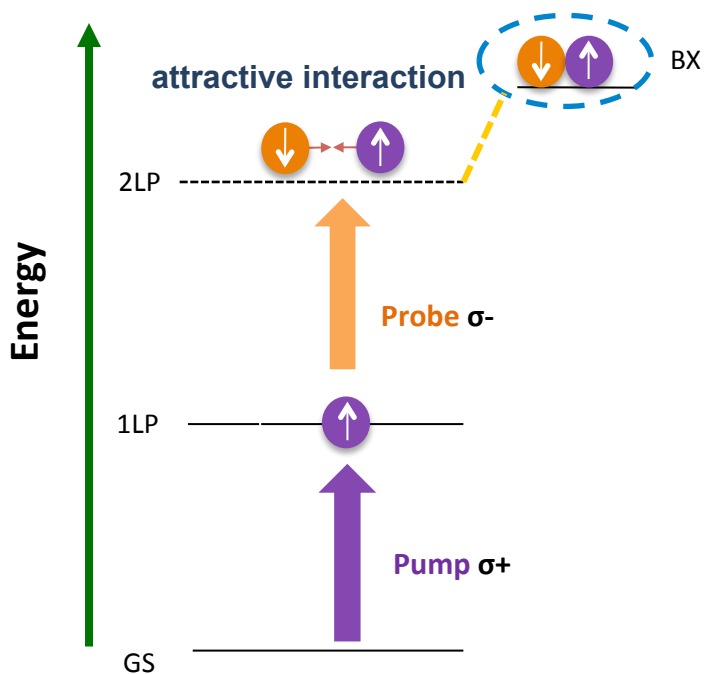
By tuning the relative energy



Polaritonic Feshbach resonance

The scheme to induce biexcitonic Feshbach resonance

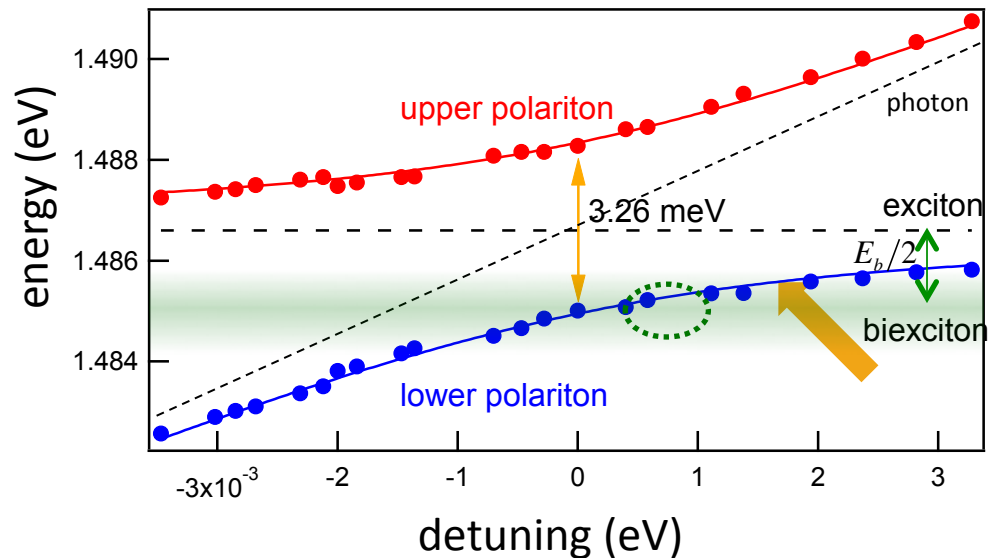
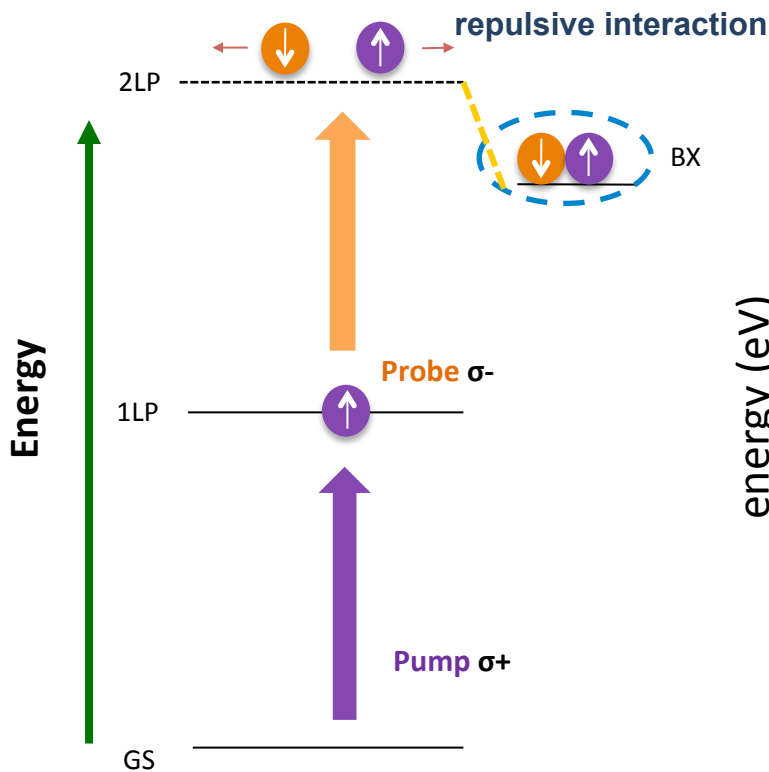
Below BX state



Polaritonic Feshbach resonance

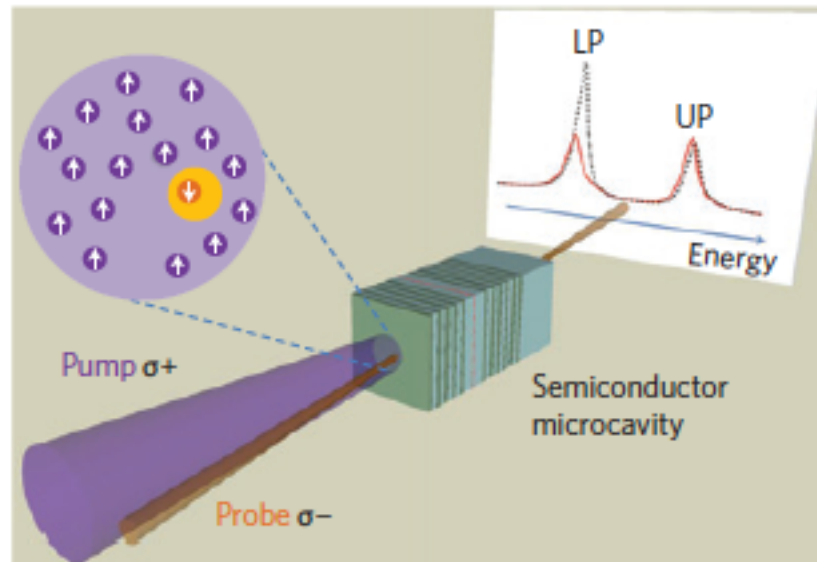
The scheme to induce biexcitonic Feshbach resonance

Above BX state

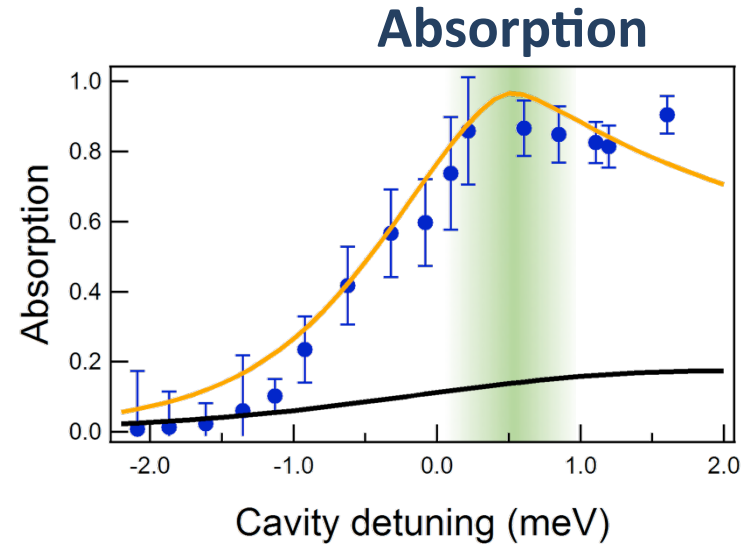
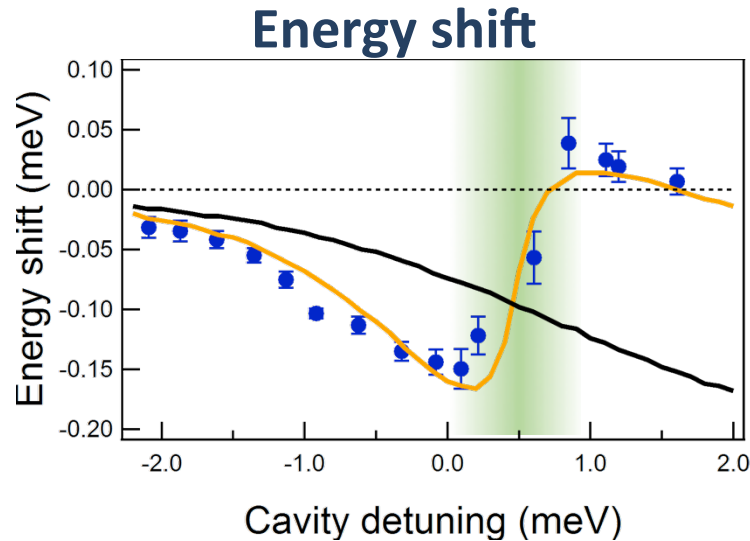


Polaritonic Feshbach resonance

The pump and probe experiment



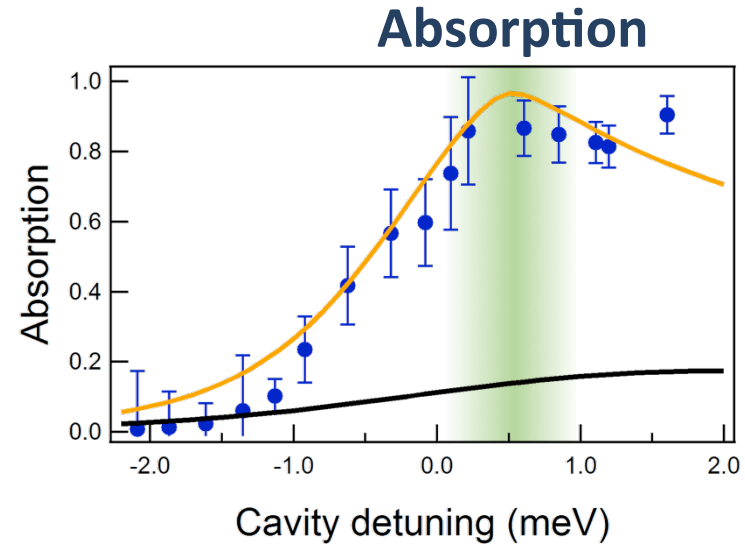
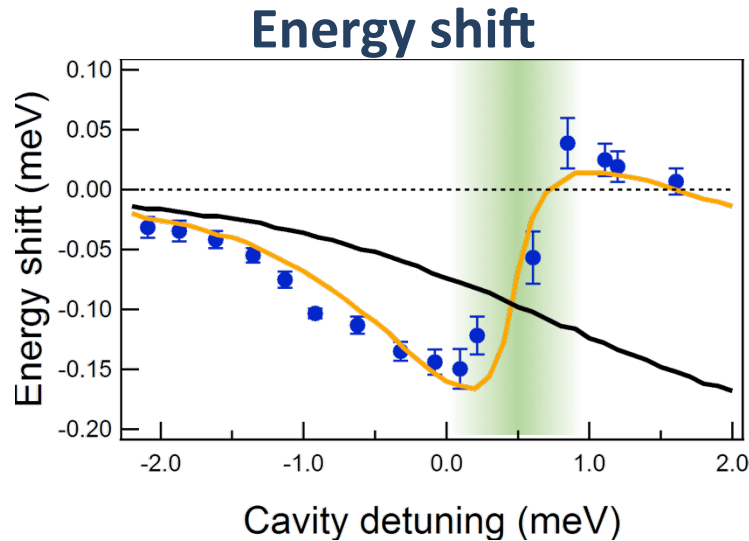
Polaritonic Feshbach resonance



$$H = \Omega_X (a_{c\sigma} \psi_{X\sigma,i}^+ + a_{c\sigma}^+ \psi_{X\sigma,i}) + \frac{U_{+-}}{2} (\psi_{X\sigma,i}^+ \psi_{X(-\sigma),i}^+ \psi_{X(-\sigma),i} \psi_{X\sigma,i}) + g_{BX} (\psi_{Bi}^+ \psi_{X\uparrow i} \psi_{X\downarrow i} + \psi_{Bi} \psi_{X\uparrow i}^+ \psi_{X\downarrow i}^+)$$

photon-exciton
background interaction
two excitons-biexciton scattering

Polaritonic Feshbach resonance



$$H = \underbrace{\Omega_X (a_{c\sigma} \psi_{X\sigma,i}^+ + a_{c\sigma}^+ \psi_{X\sigma,i})}_{\text{photon-exciton}} + \underbrace{\frac{U}{2} (\psi_{X\sigma,i}^+ \psi_{X(-\sigma),i}^+ \psi_{X(-\sigma),i} \psi_{X\sigma,i})}_{\text{background interaction}} + \underbrace{g_{BX} (\psi_{Bi}^+ \psi_{X\uparrow i} \psi_{X\downarrow i} + \psi_{Bi} \psi_{X\uparrow i}^+ \psi_{X\downarrow i}^+)}_{\text{two excitons-biexciton scattering}}$$

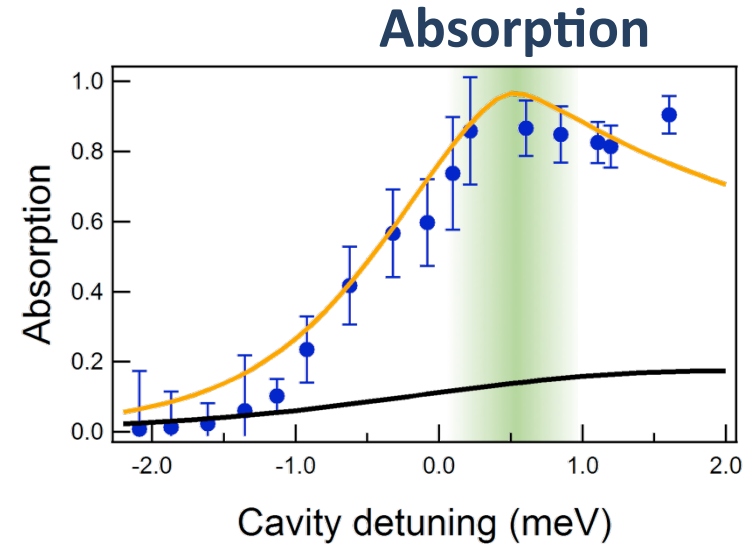
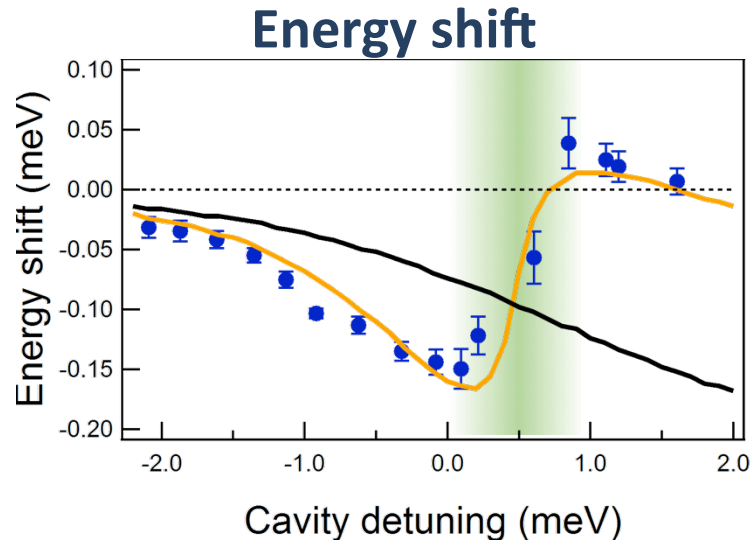
$$\Delta E_{L,\downarrow} = g^{+-} X_0^4 \left| \psi_{LP,\uparrow}^{pu} \right|^2 + \text{Re} \left[\frac{g_{bx}^2 X_0^4 \left| \psi_{LP,\uparrow}^{pu} \right|^2}{2\varepsilon_{LP} - \varepsilon_B + i\gamma_B} \right]$$

Energy shift

$$\alpha = g^{+-} X_0^4 + g_{bx} X_0^4 \frac{2\varepsilon_L - \varepsilon_B}{(2\varepsilon_L - \varepsilon_B)^2 + \gamma_B^2}$$

absorption

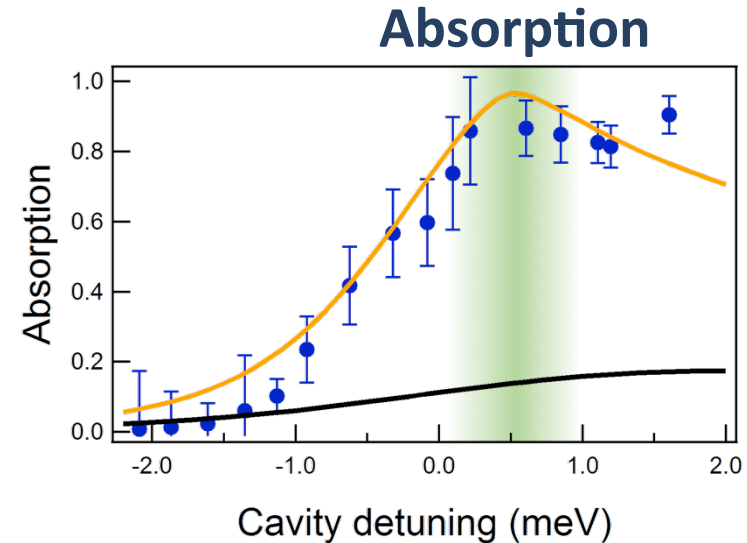
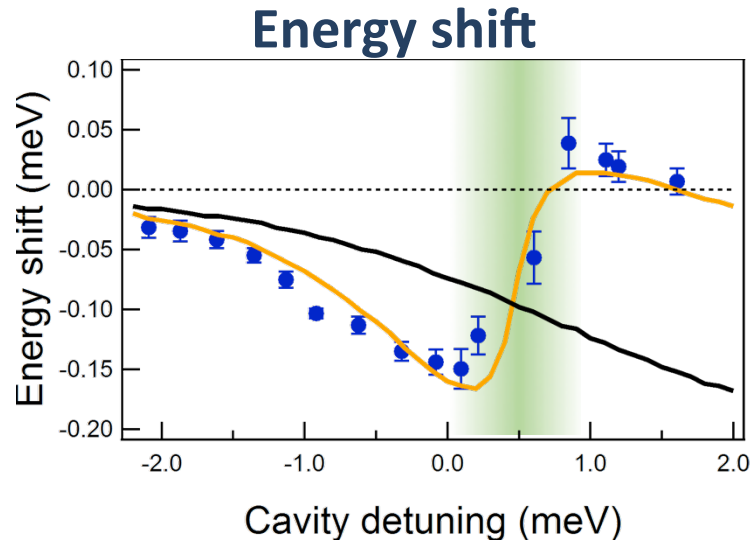
Polaritonic Feshbach resonance



characteristic shape of resonant scattering

- ✓ dispersive shape
- ✓ change of the magnitude and sign of the interaction
- ✓ absorption maximum at resonance region

Polaritonic Feshbach resonance



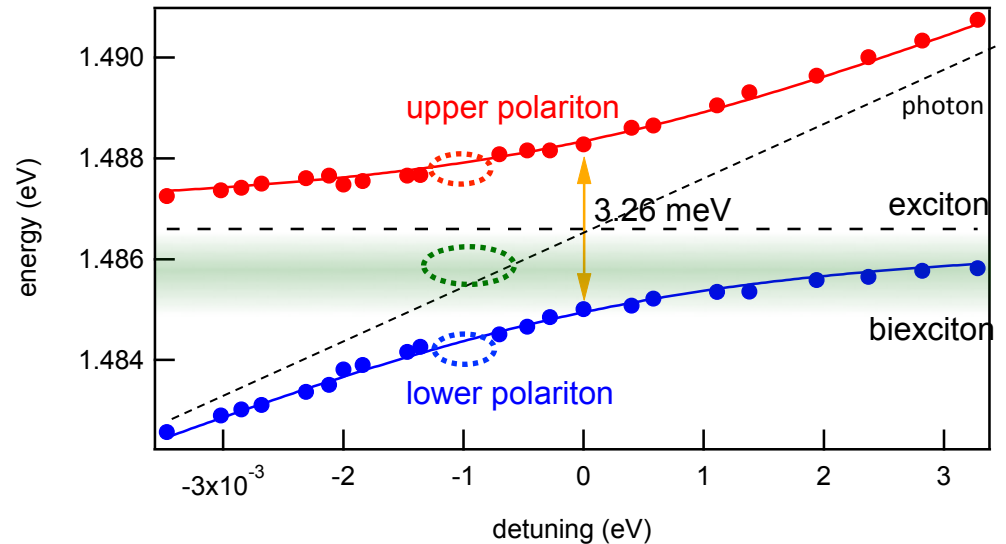
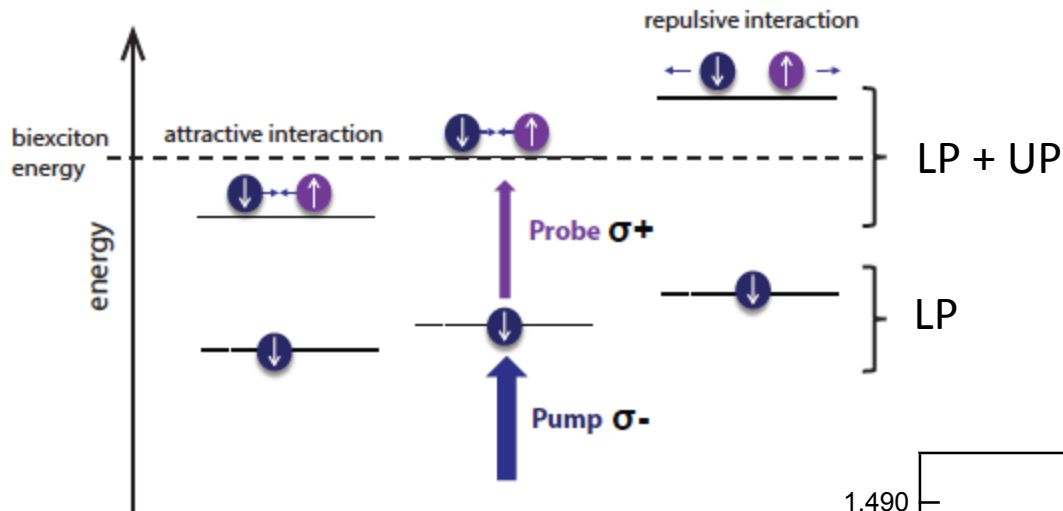
characteristic shape of resonant scattering

- ✓ dispersive shape
- ✓ change of the magnitude and sign of the interaction
- ✓ absorption maximum at resonance region

Control the strength and nature of the interaction

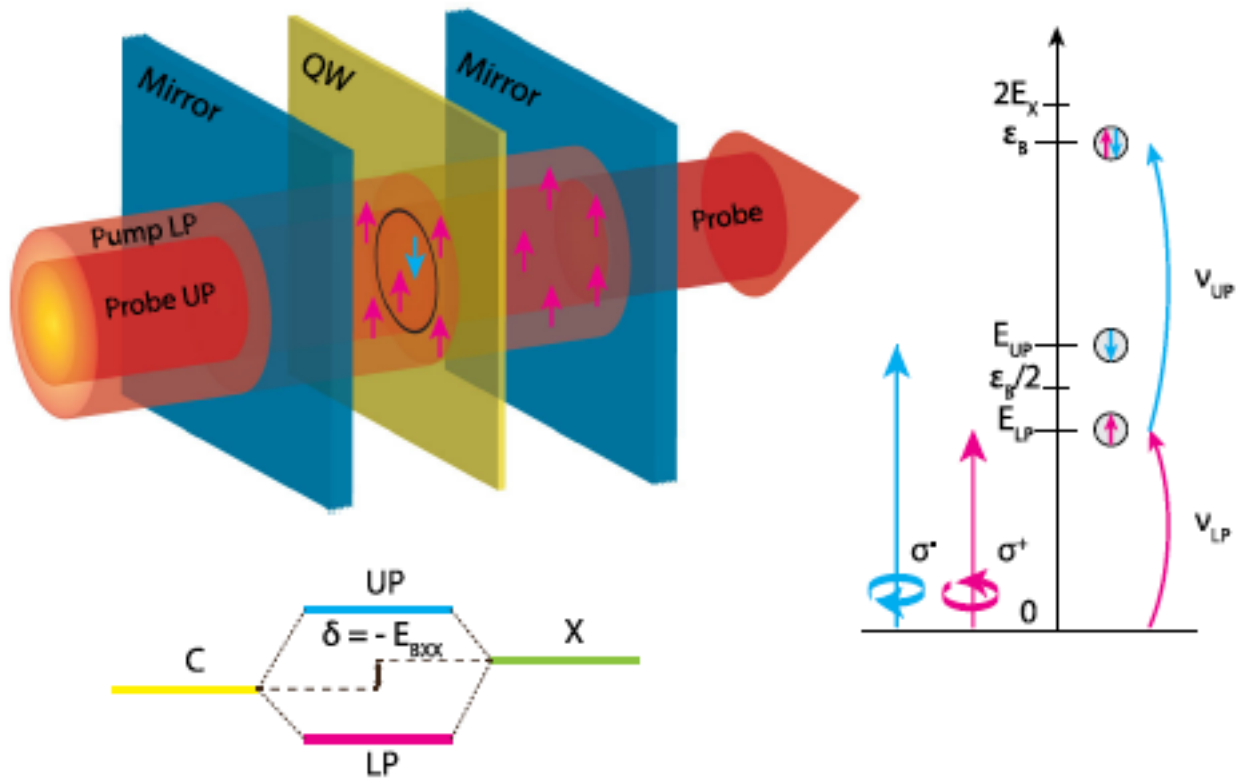
Polaritonic Cross Feshbach resonance

The scheme to induce cross Feshbach resonance

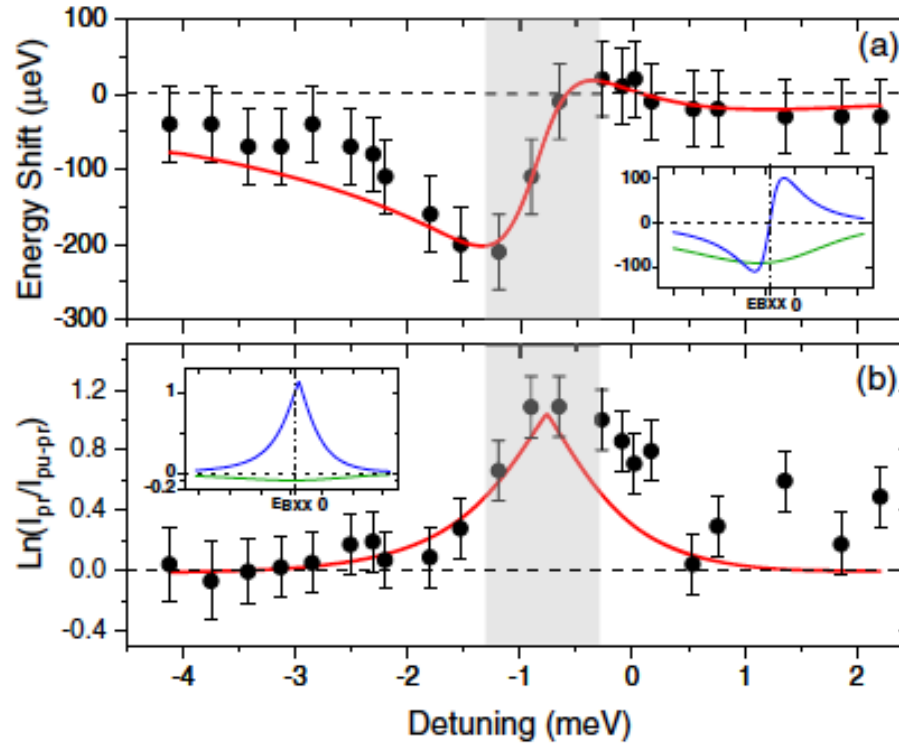


Polaritonic Cross Feshbach resonance

The pump and probe experiment



Polaritonic Cross Feshbach resonance



$$\Delta E_{U,\downarrow} = g^{+-} X_0^2 |C_0|^2 |\psi_{LP,\uparrow}^{pu}|^2 + \text{Re} \left[\frac{g_{bx}^2 X_0^2 |C_0|^2 |\psi_{LP,\uparrow}^{pu}|^2}{\varepsilon_{LP} + \varepsilon_{UP} - \varepsilon_B + i\gamma_B} \right]$$

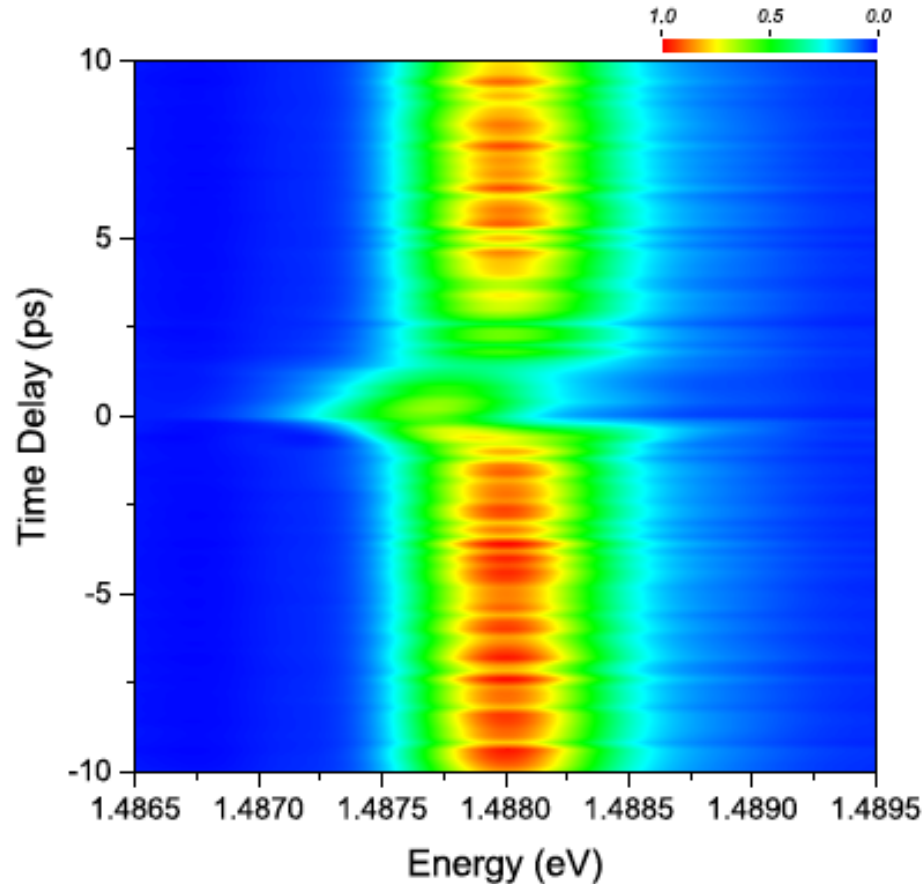
Energy shift

$$\alpha_B = g_{bx}^2 X_0^2 |C_0|^2 |\psi_{LP,\uparrow}^{pu}|^2 \frac{\gamma_B}{(\varepsilon_{LP} + \varepsilon_{UP} - \varepsilon_B)^2 + \gamma_B^2}$$

Absorption

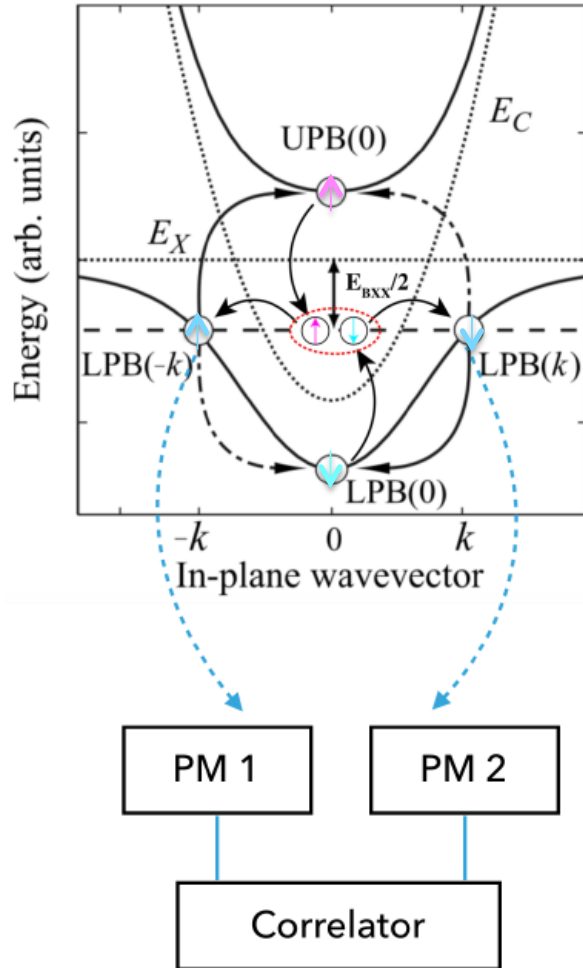
Polaritonic Cross Feshbach resonance

Dynamics of the cross Feshbach resonance



Cavity detuning in the vicinity of the cross FR
 $\delta = -1.2 meV$

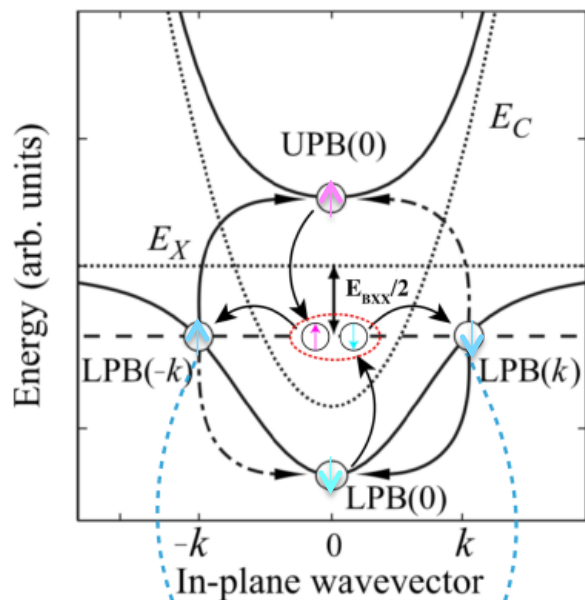
Scheme for generating pairs of entangled photons



Pair of photons entangled in momentum and polarization

$LP(-k) \uparrow \quad \downarrow LP(-k)$

Scheme for generating pairs of entangled photons

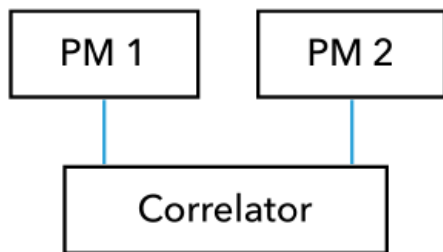


Pair of photons entangled in momentum and polarization

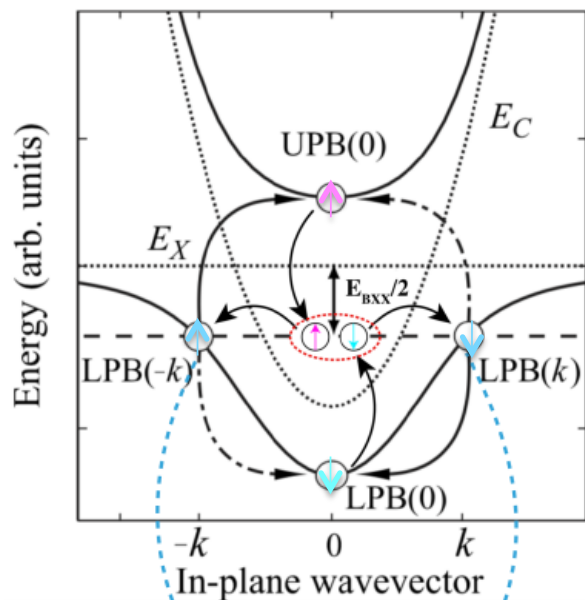
$$LP(-k) \uparrow \quad \downarrow \quad LP(-k)$$

Pair of photons entangled in energy and polarization

$$UP(k=0) \uparrow \quad \downarrow \quad LP(k=0)$$



Scheme for generating pairs of entangled photons

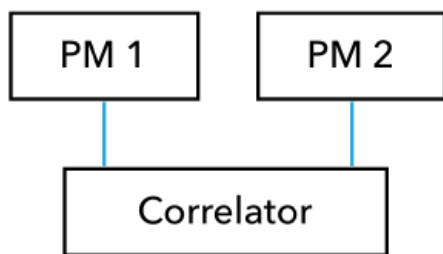


Pair of photons entangled in momentum and polarization

$$LP(-k) \uparrow \quad \downarrow \quad LP(-k)$$

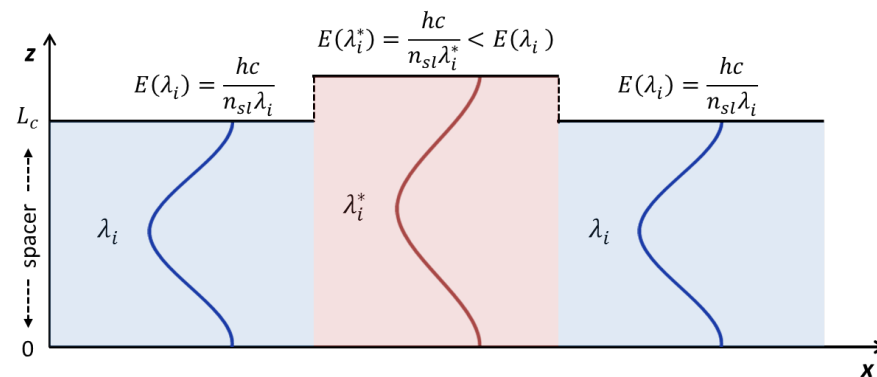
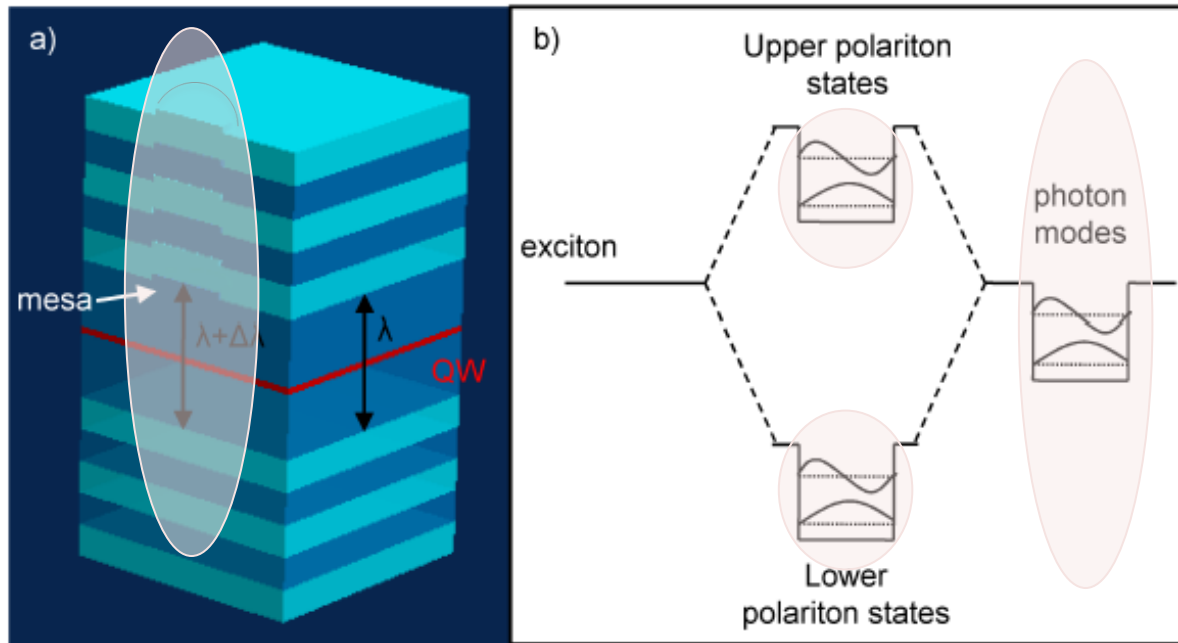
Pair of photons entangled in energy and polarization

$$UP(k=0) \uparrow \quad \downarrow \quad LP(k=0)$$

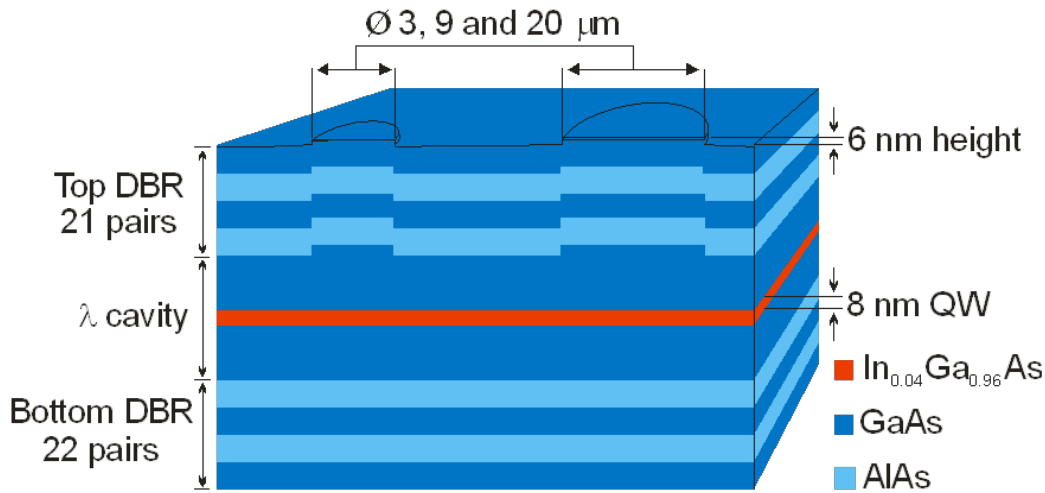


**The cross FR situation
will permit the entangled photon pairs
to be isolated from the transmitted laser beams**

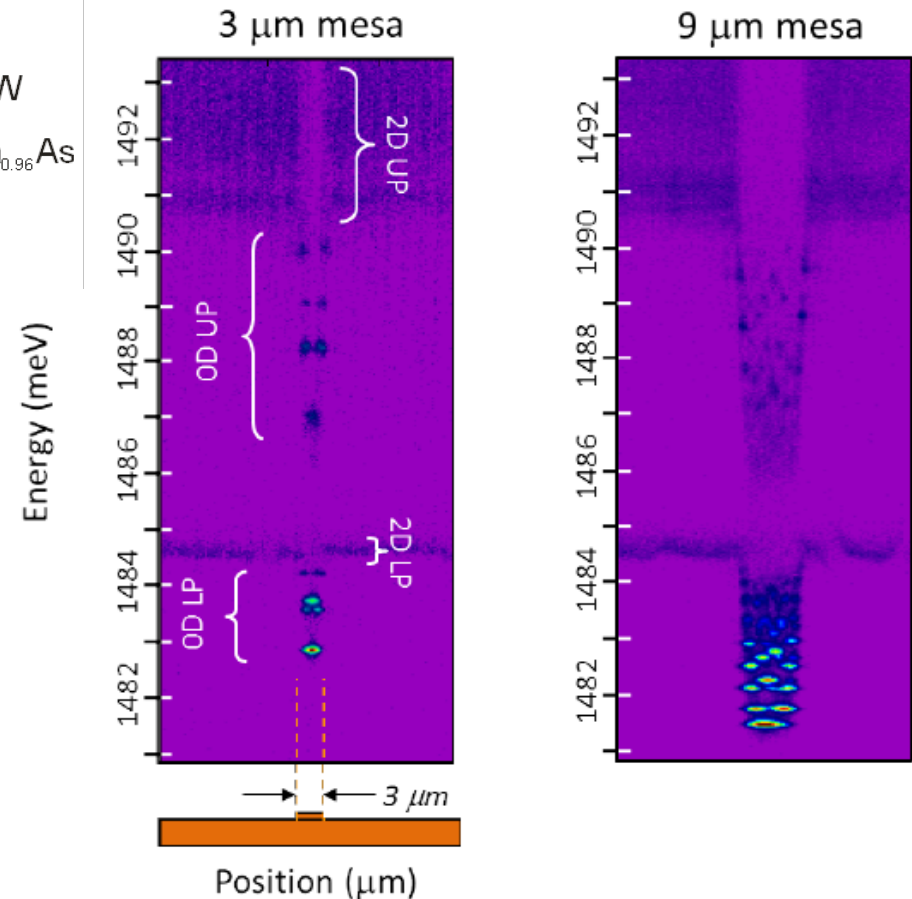
Confined zero-dimensional polaritons



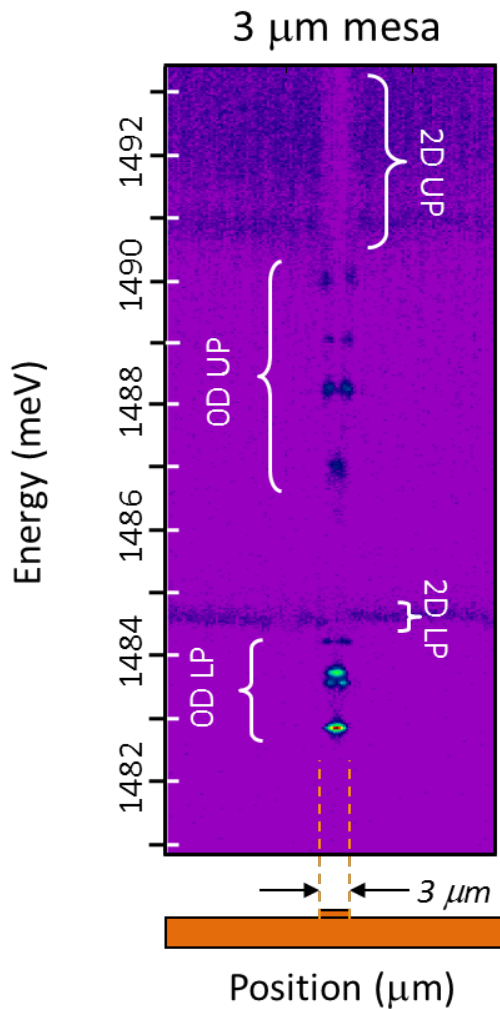
Confined zero-dimensional polaritons



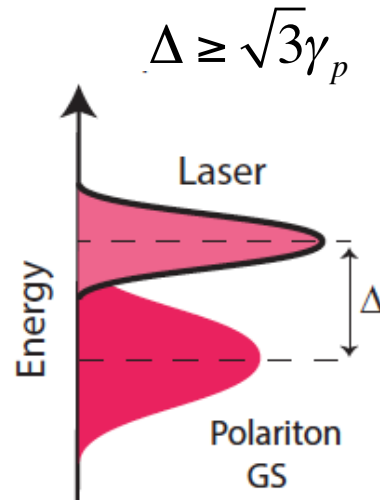
Spatially resolved spectrum



Polariton bistability

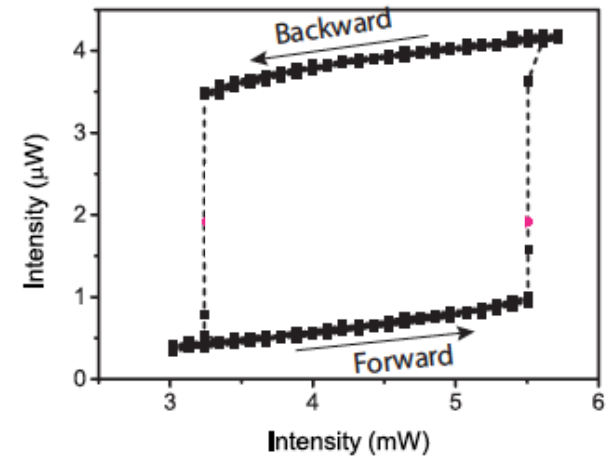


Bistability condition



$$\gamma_p = 70 \mu\text{eV}$$

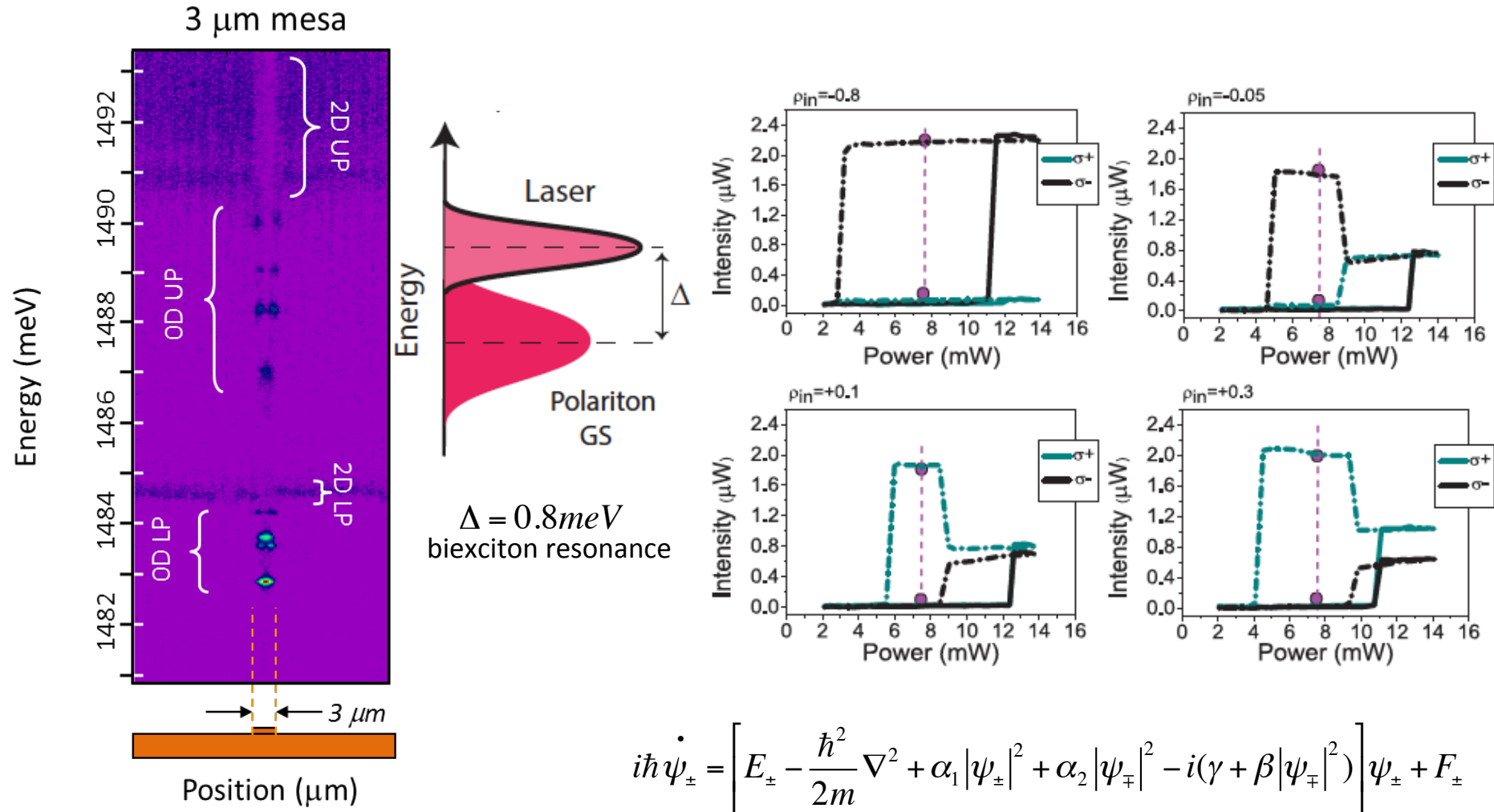
$$\Delta = 0.4 \text{ meV}$$



Laser polarization σ^+

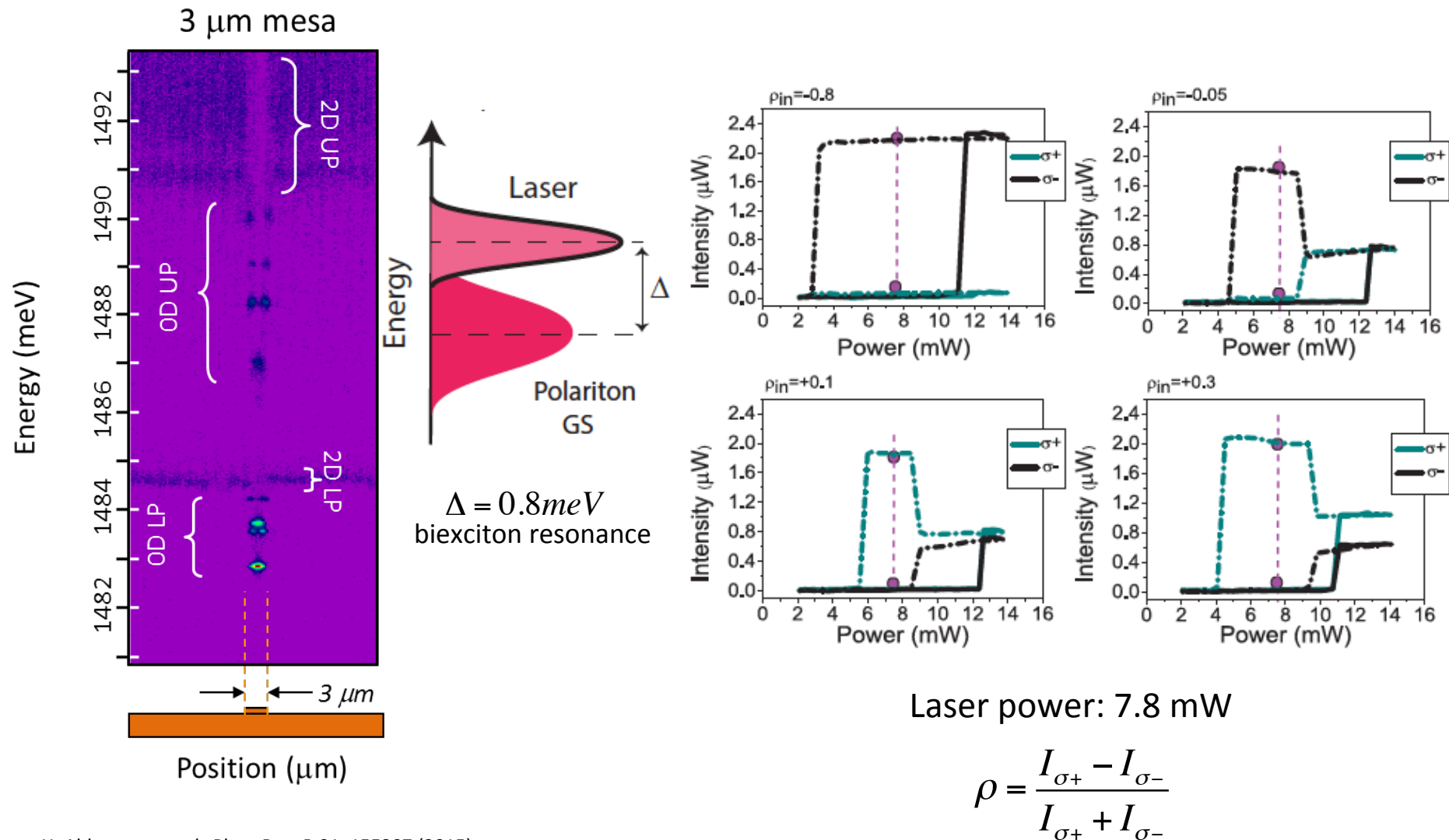
$$i\hbar \frac{\partial \psi}{\partial t} = \left[E - \frac{\hbar^2}{2m} \nabla^2 + \alpha_1 |\psi|^2 - i\gamma \right] \psi + F$$

Polariton spinor bistability

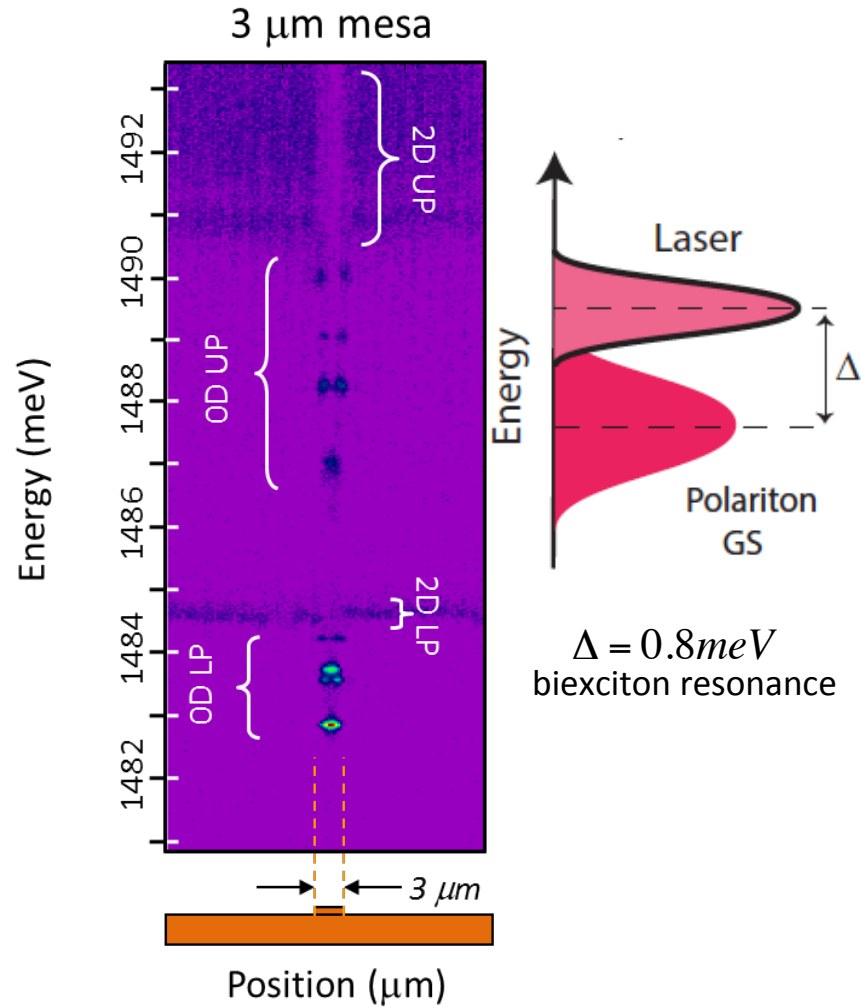


$$i\hbar \dot{\psi}_{\pm} = \left[E_{\pm} - \frac{\hbar^2}{2m} \nabla^2 + \alpha_1 |\psi_{\pm}|^2 + \alpha_2 |\psi_{\mp}|^2 - i(\gamma + \beta |\psi_{\mp}|^2) \right] \psi_{\pm} + F_{\pm}$$

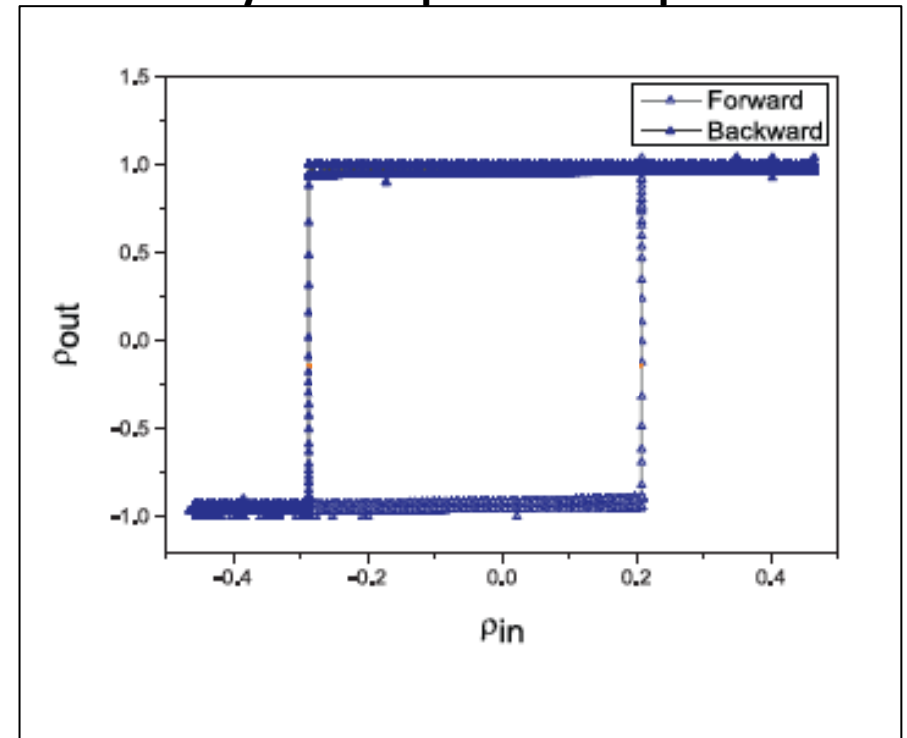
Polariton spinor bistability



Polariton spinor bistability



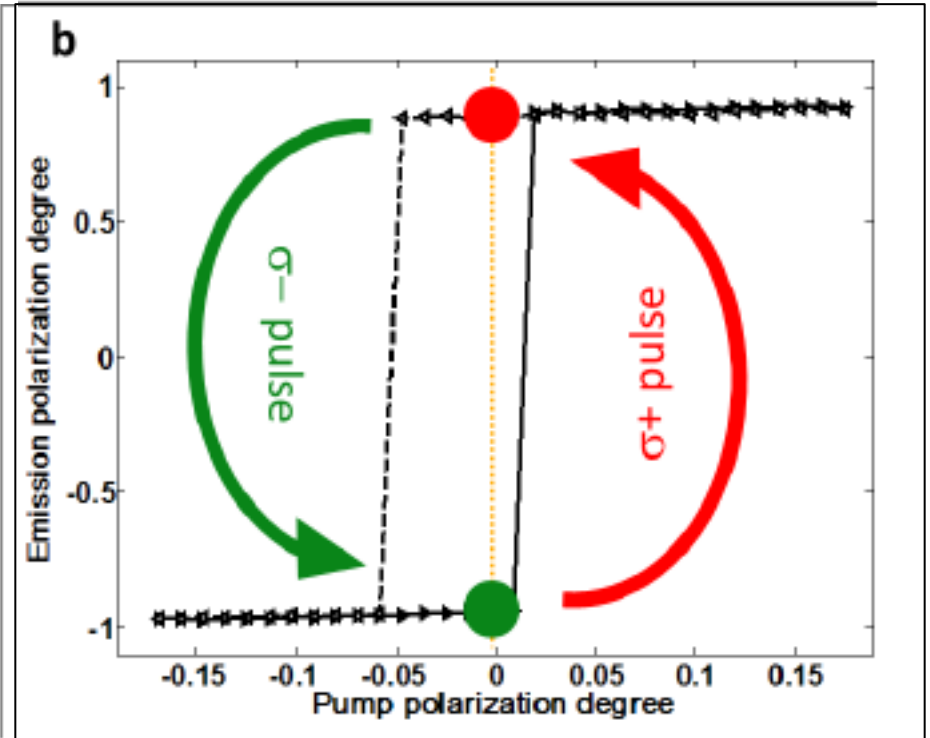
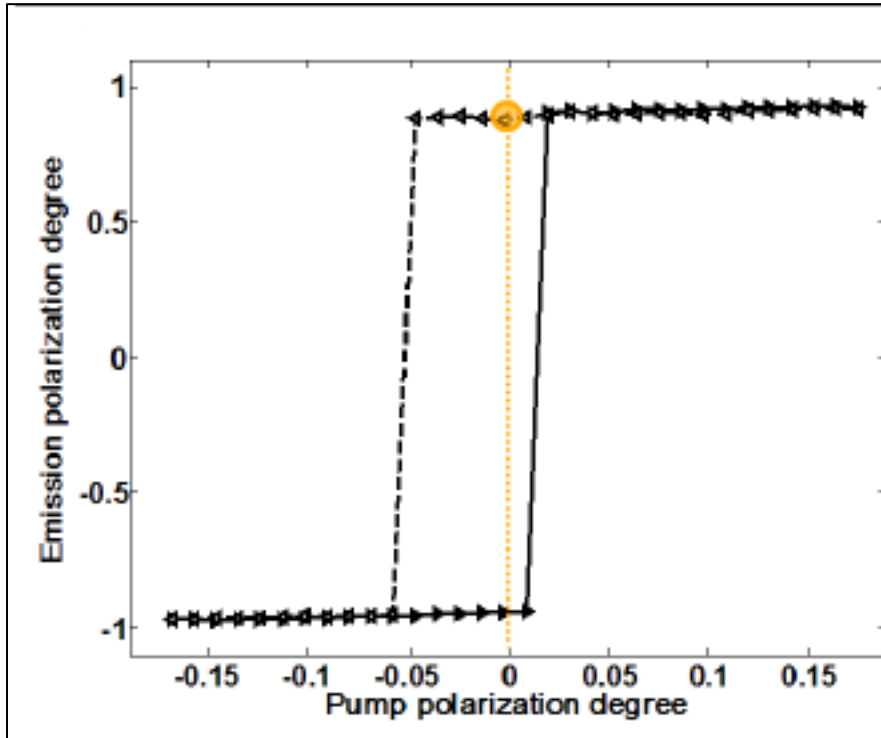
Bistability of the spin state of polaritons



Laser power: 7.8 mW

$$\rho = \frac{I_{\sigma_+} - I_{\sigma_-}}{I_{\sigma_+} + I_{\sigma_-}}$$

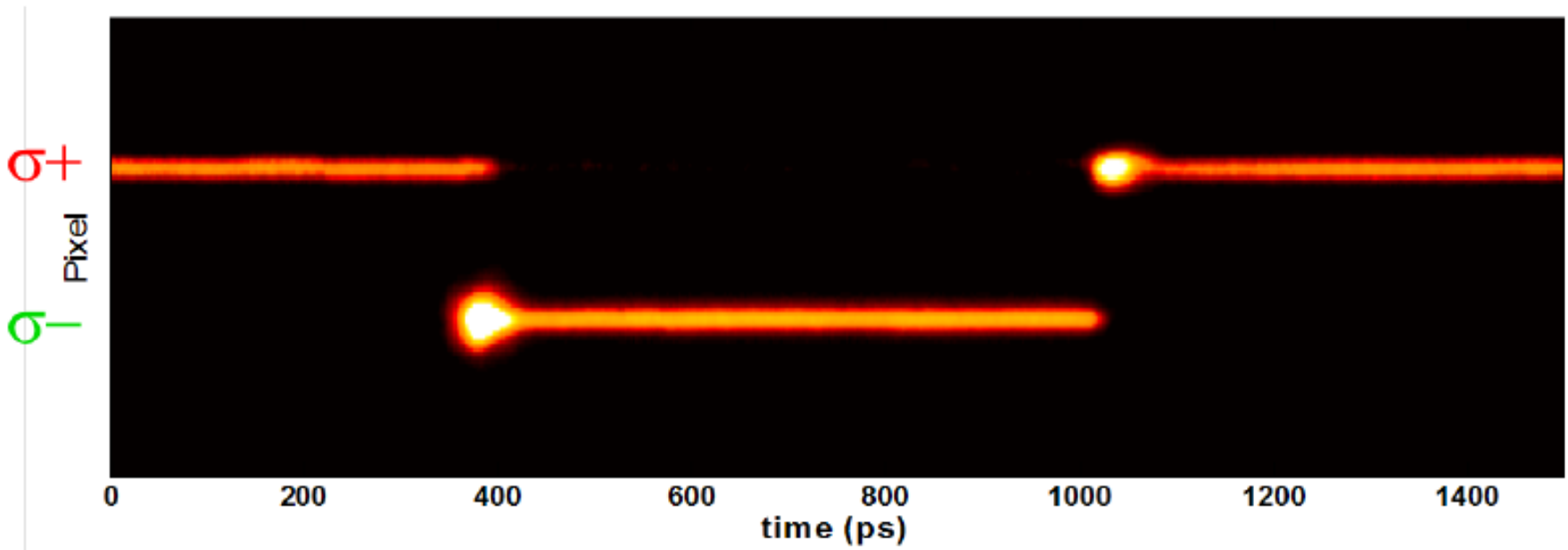
Spin switch



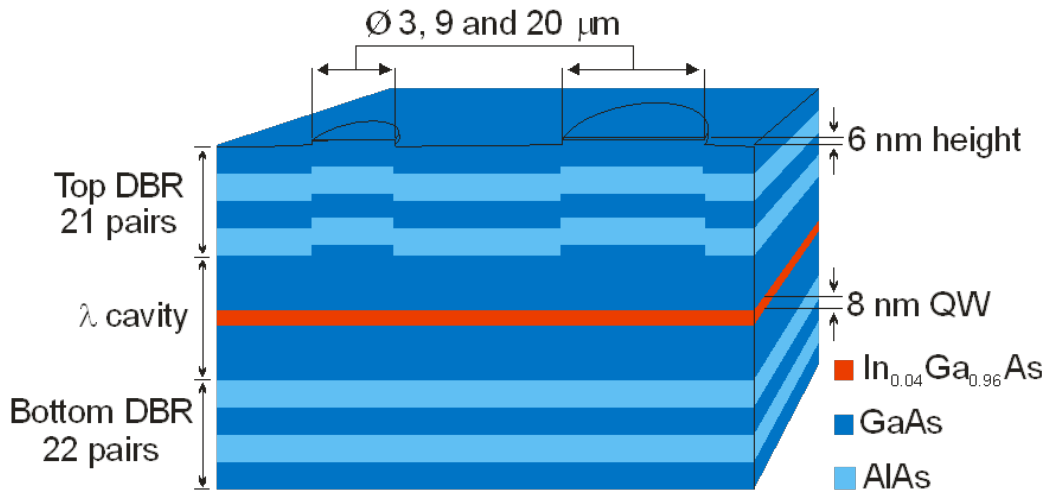
Laser power: 7.8 mW

$$\text{Emission polarization: } \rho = \frac{I_{\sigma^+} - I_{\sigma^-}}{I_{\sigma^+} + I_{\sigma^-}}$$

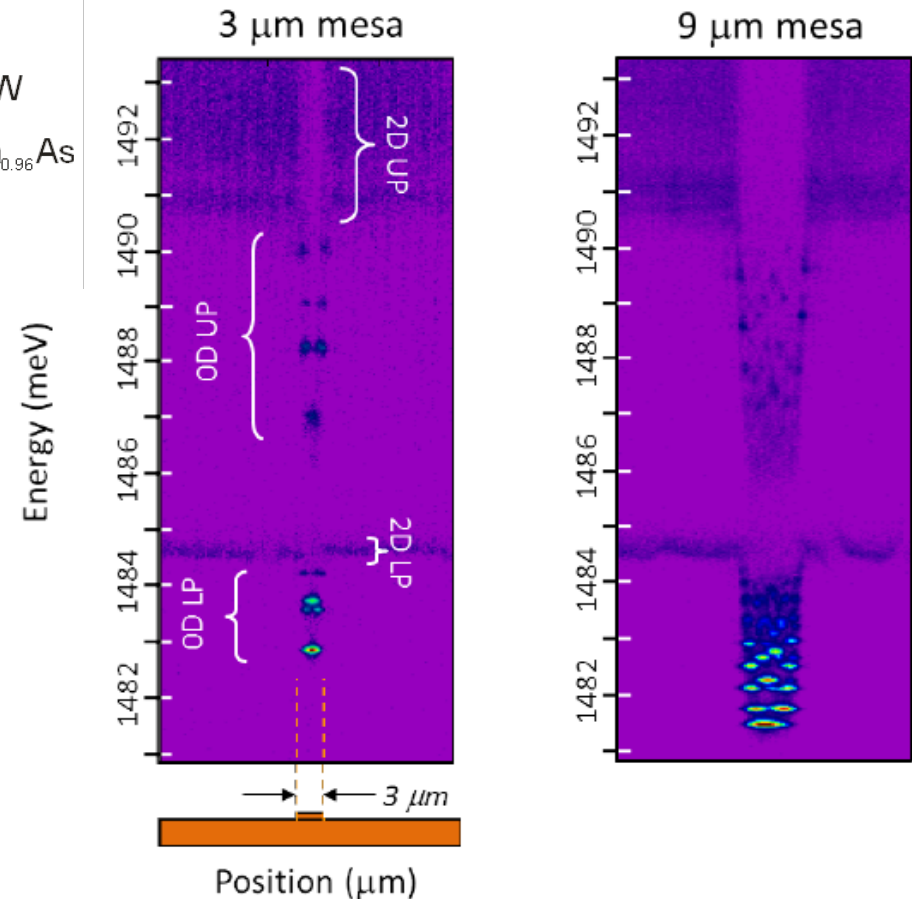
Spin memory



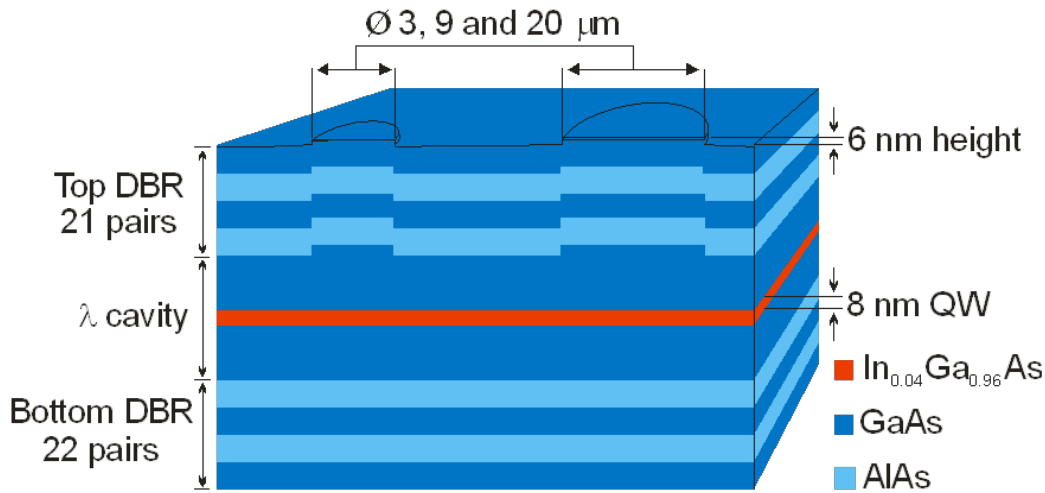
Confined zero-dimensional polaritons



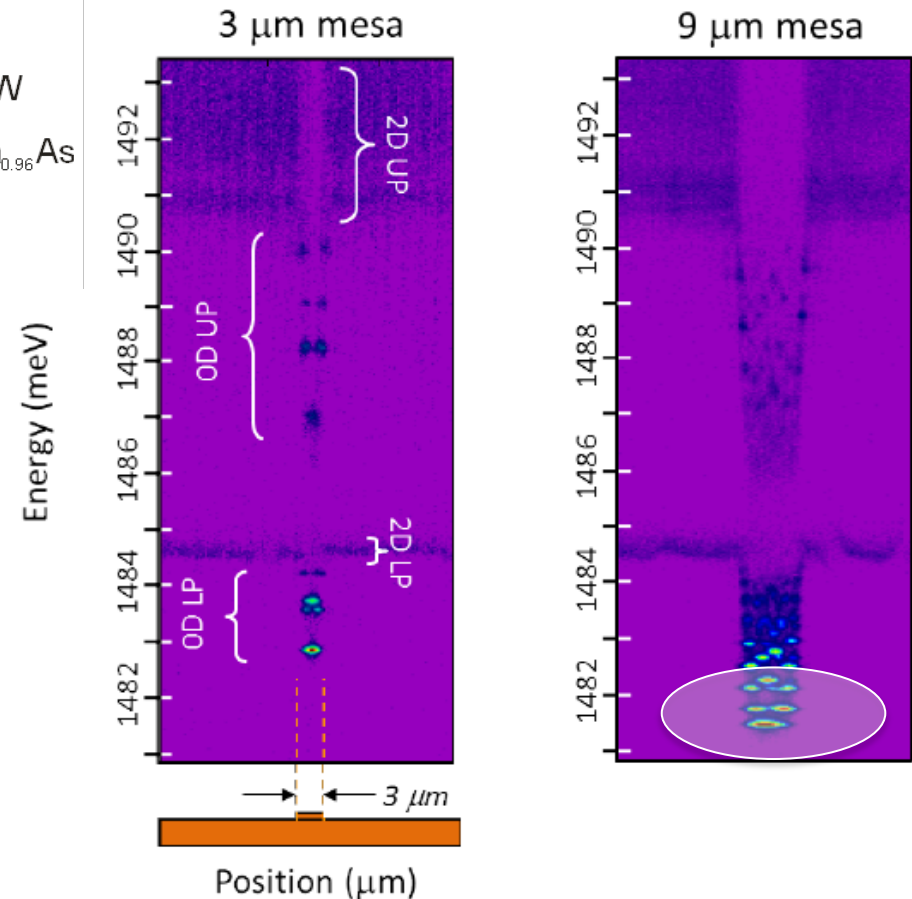
Spatially resolved spectrum



Confined zero-dimensional polaritons



Spatially resolved spectrum

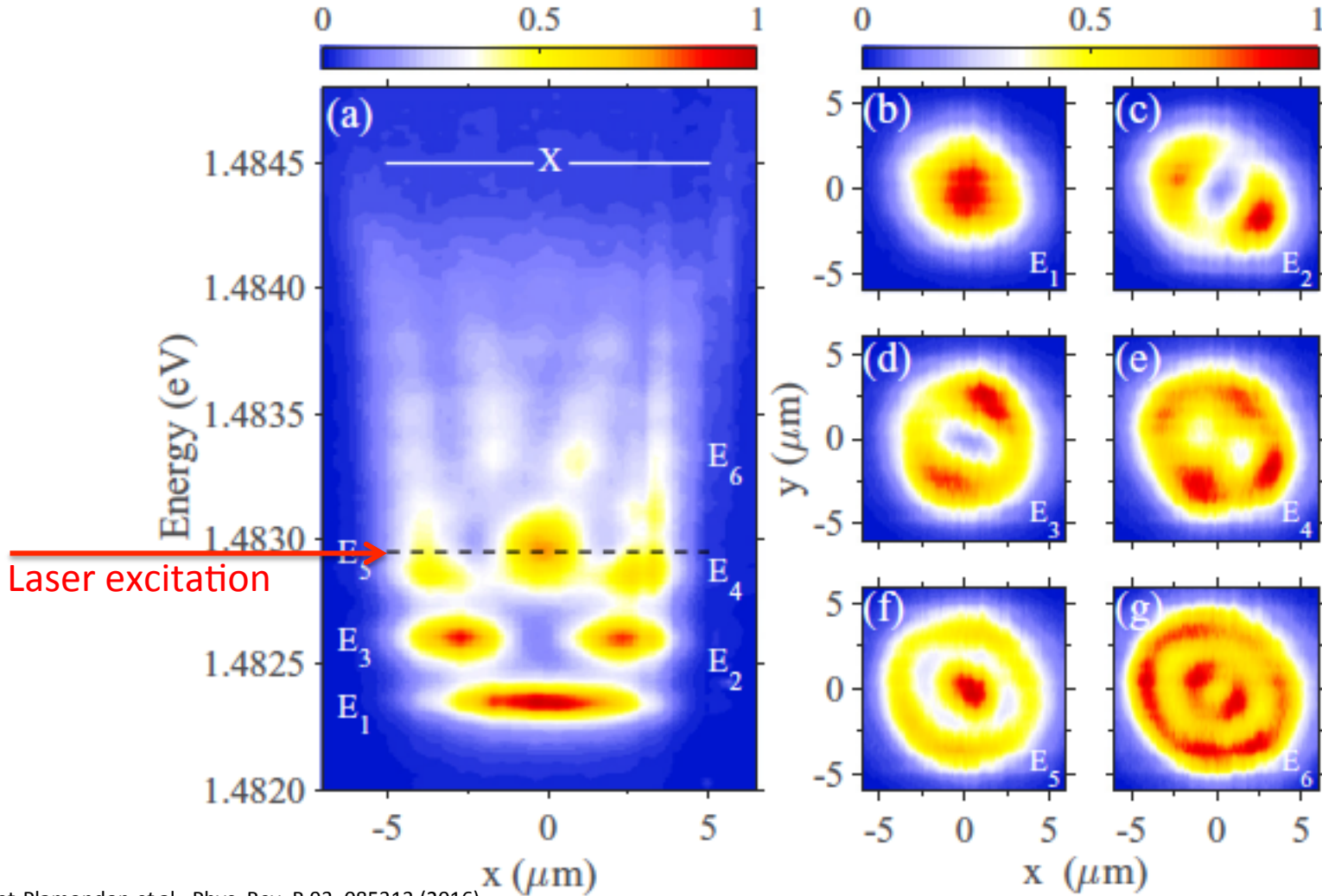


Spatial multistability

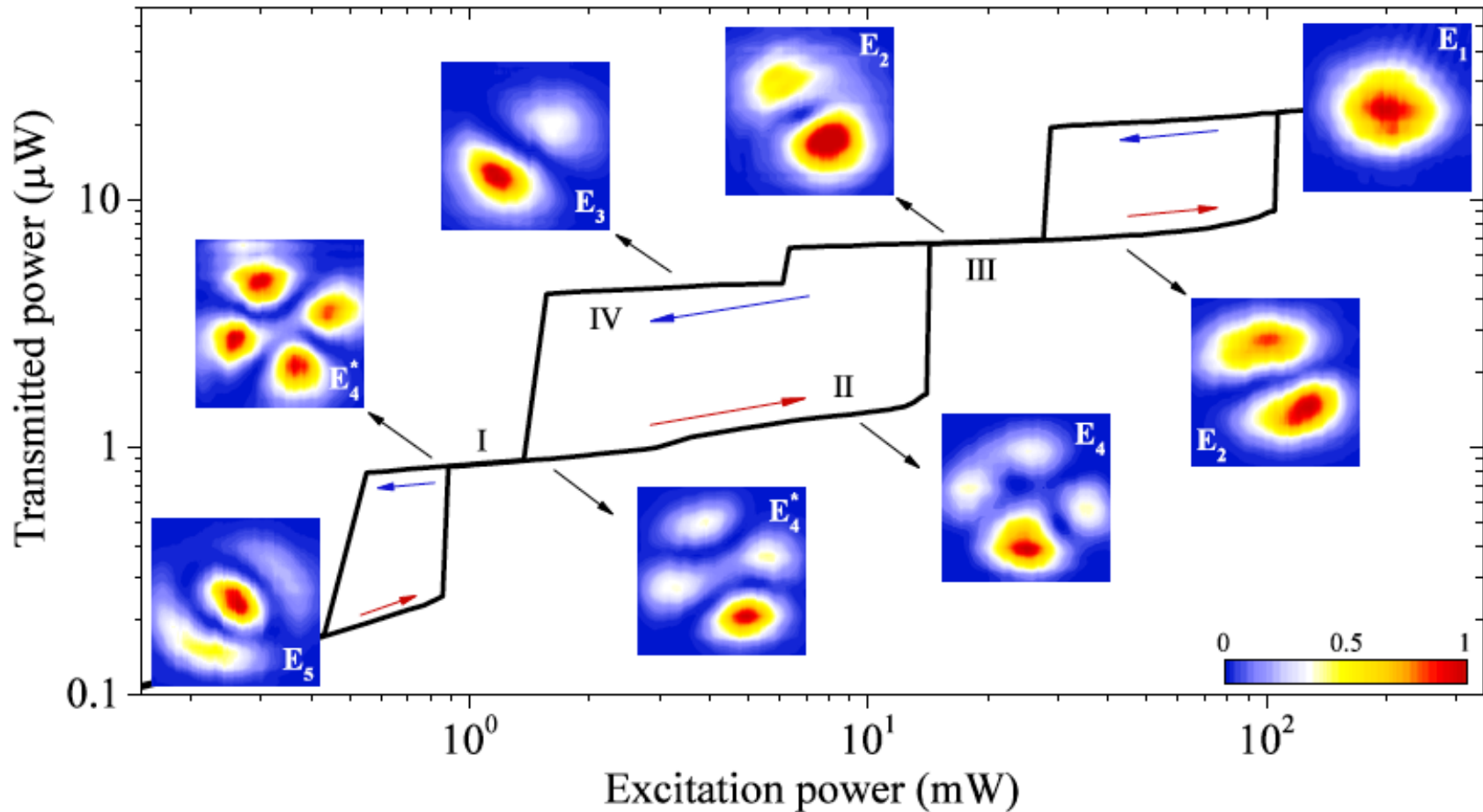
9 μm mesa

Real space spectrum

Spatial profile of the confined states



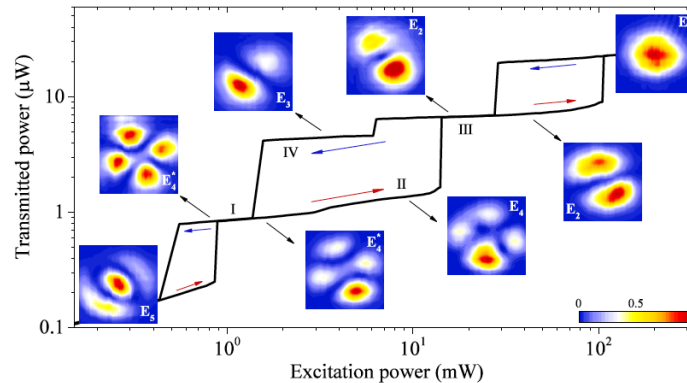
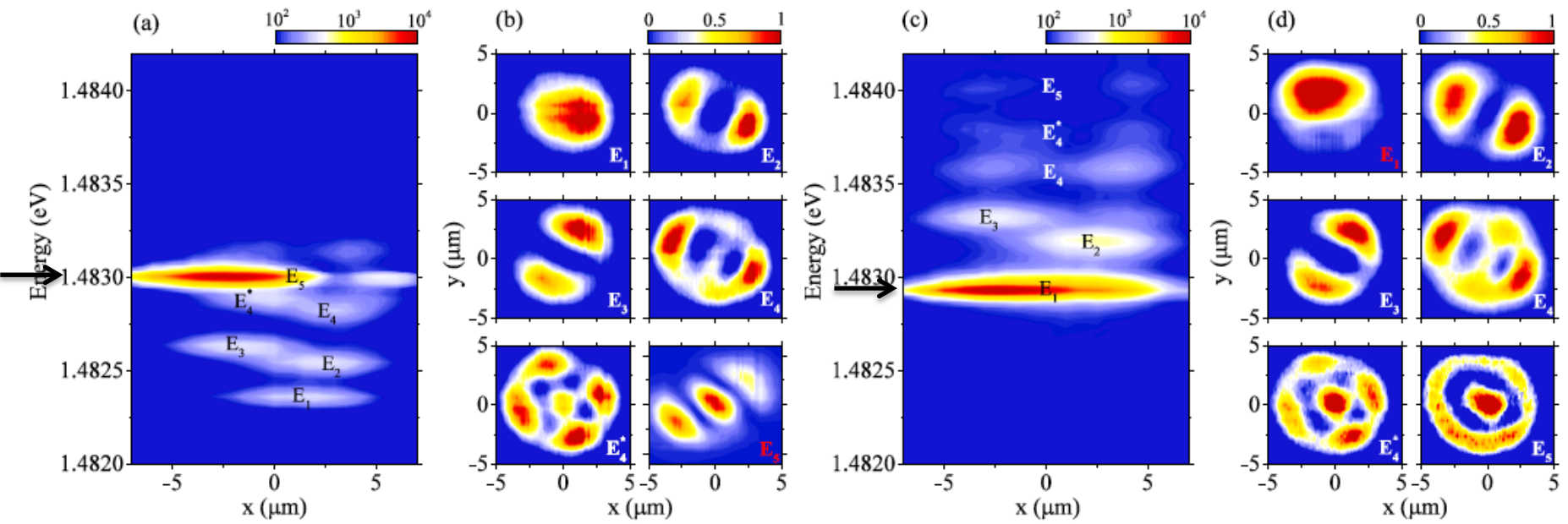
Spatial multistability



Spatial multistability

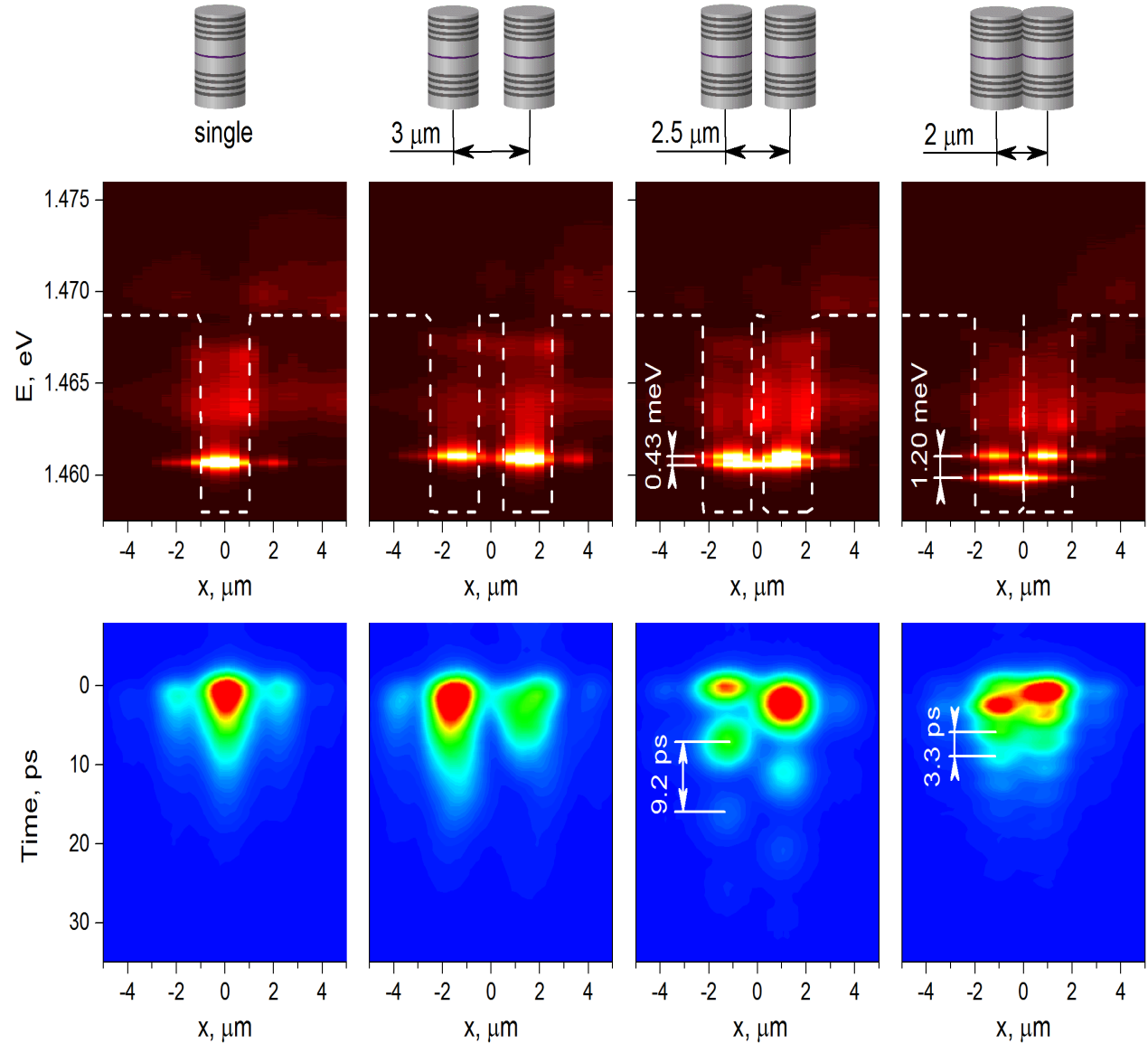
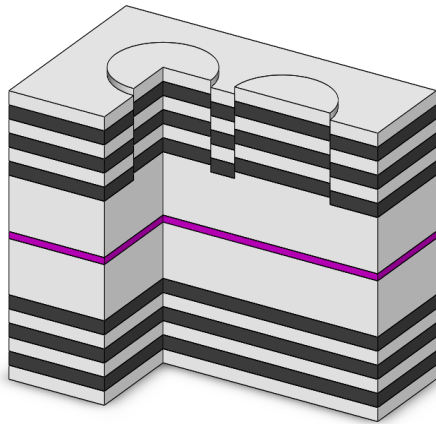
Bottom of the bistability curve

Top of the bistability curve

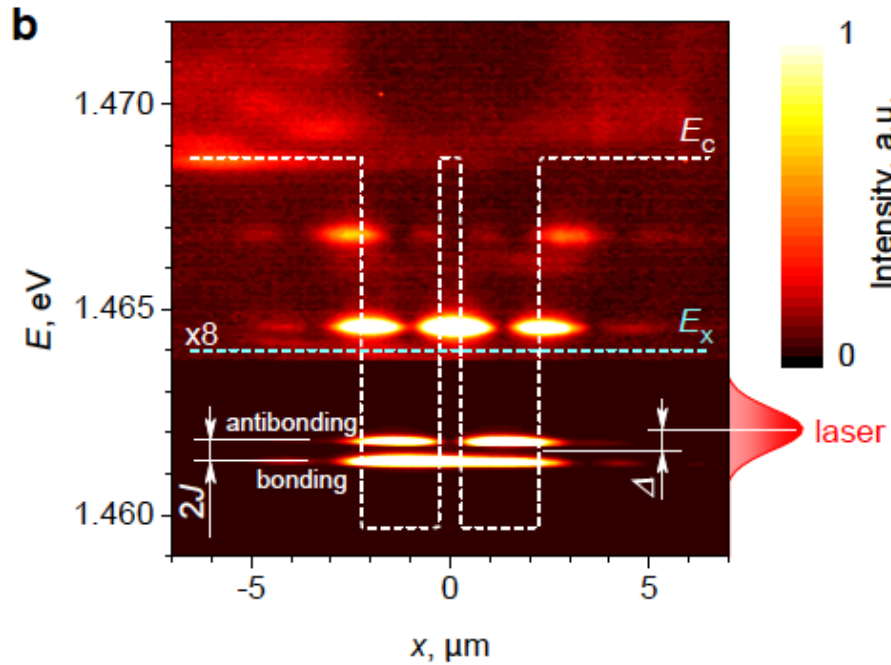


Coupled mesas

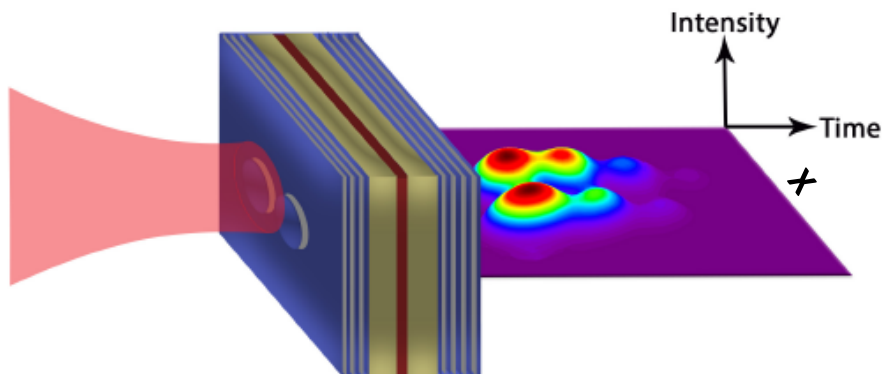
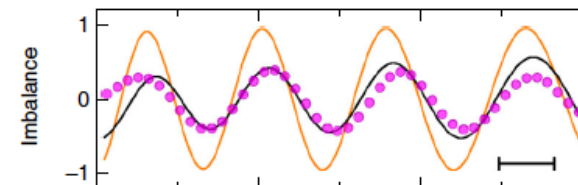
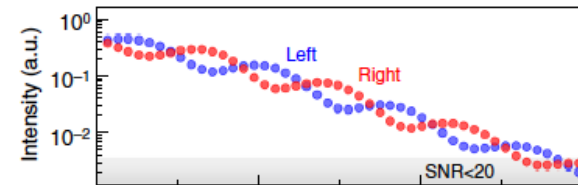
Coupled 2 μm mesas



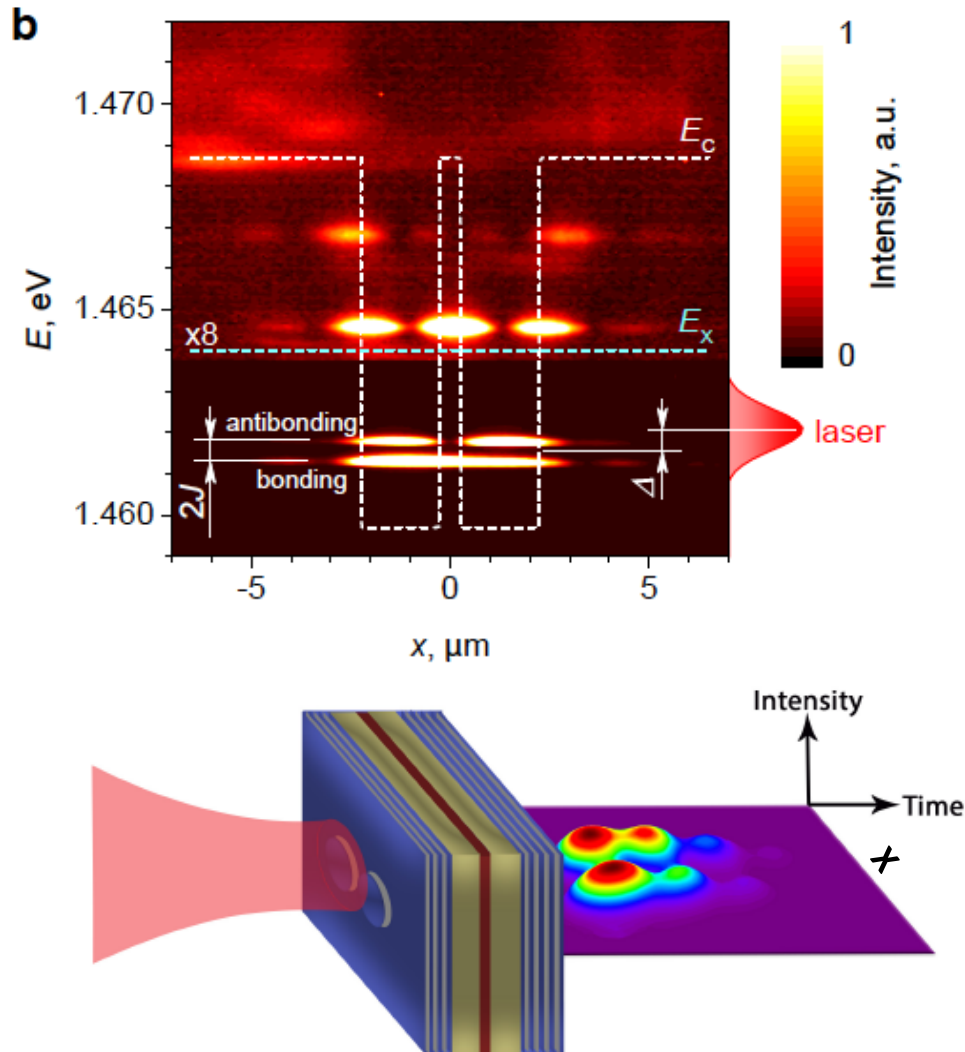
Polariton Josephson junction



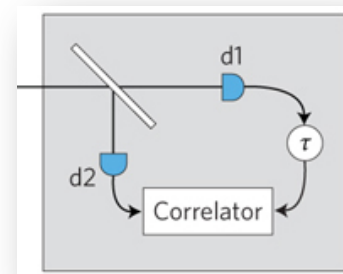
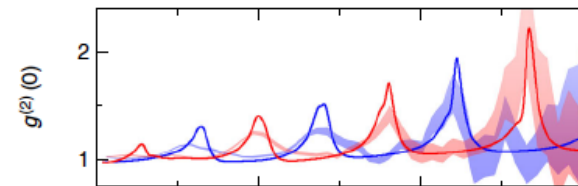
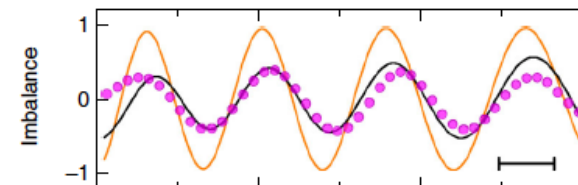
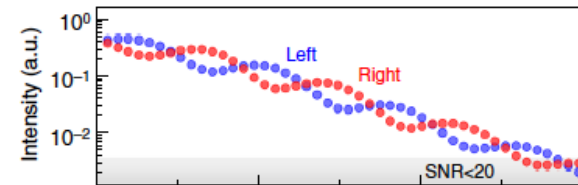
$$\hat{H} = \sum_{k=L,R} [\hbar\omega_c \hat{a}_k^+ \hat{a}_k + U \hat{a}_k^+ \hat{a}_k^+ \hat{a}_k \hat{a}_k] - J(\hat{a}_L^+ \hat{a}_R + \hat{a}_R^+ \hat{a}_L)$$



Polariton Josephson junction

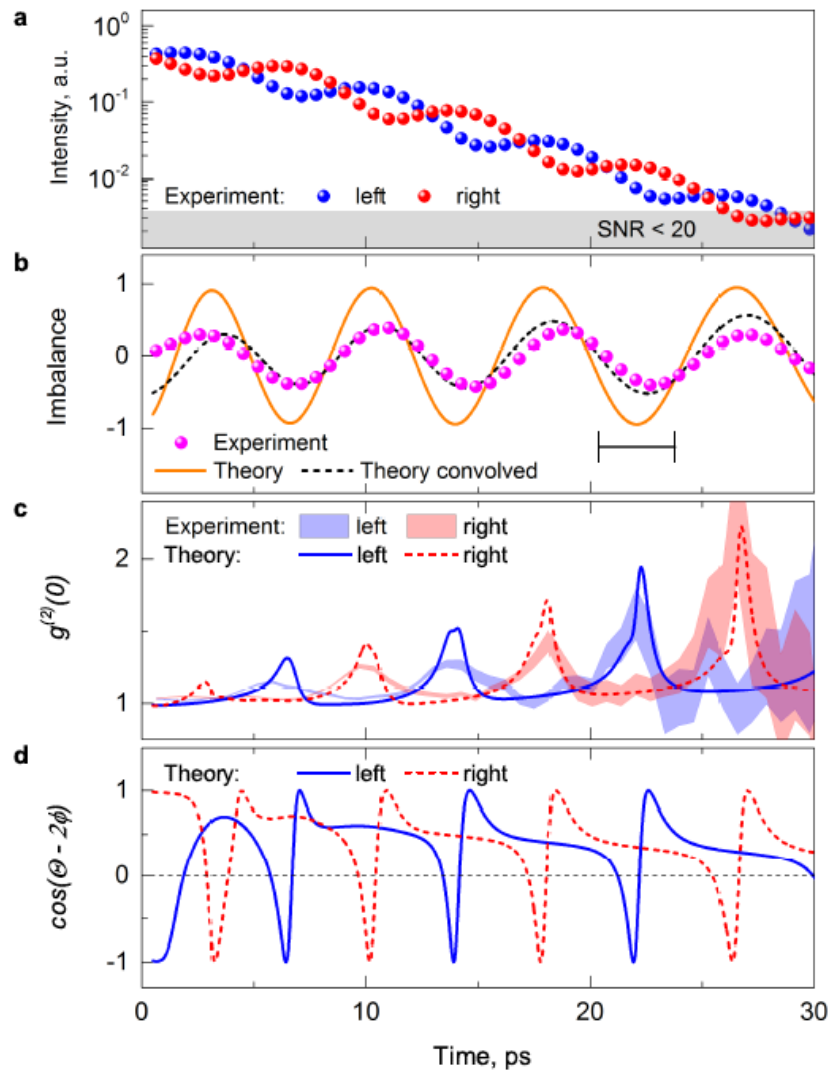


$$\hat{H} = \sum_{k=L,R} [\hbar\omega_c \hat{a}_k^\dagger \hat{a}_k + U \hat{a}_k^\dagger \hat{a}_k^\dagger \hat{a}_k \hat{a}_k] - J(\hat{a}_L^\dagger \hat{a}_R + \hat{a}_R^\dagger \hat{a}_L)$$



$$g^{(2)}(0) = \frac{\langle \hat{a}^\dagger \hat{a}^\dagger \hat{a} \hat{a} \rangle}{\langle \hat{a}^\dagger \hat{a} \rangle^2}$$

Periodic squeezing in a polariton Josephson junction



Model: *H. Flayac and V. Savona, PRA 95, 043838 (2017)*

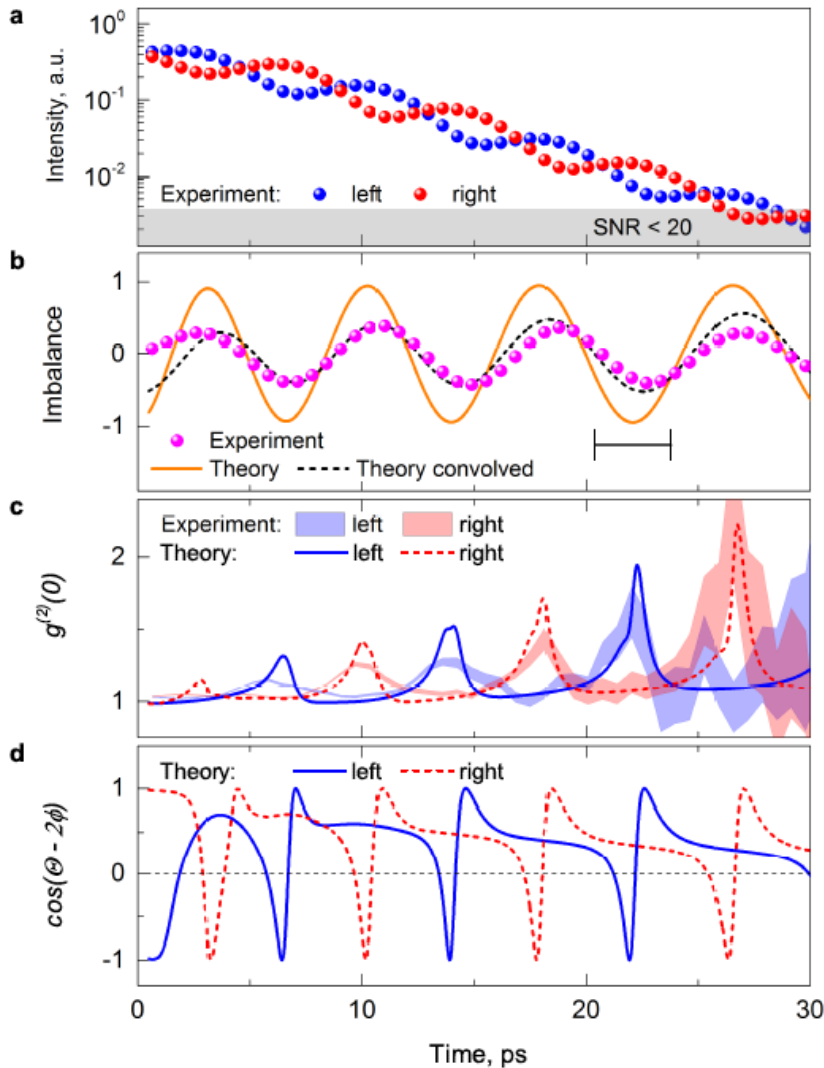
$$\hat{H} = \sum_{k=L,R} \left[\hbar\omega_c \hat{a}_k^\dagger \hat{a}_k + U \hat{a}_k^\dagger \hat{a}_k^\dagger \hat{a}_k \hat{a}_k \right] - J \left(\hat{a}_L^\dagger \hat{a}_R + \hat{a}_R^\dagger \hat{a}_L \right) + \sum_{k=L,R} \left[P_k(t) \hat{a}_k^\dagger + P_k^*(t) \hat{a}_k \right]$$

Polariton operators: $\hat{a}_k = \alpha_k + \delta\hat{a}_k$

$\alpha_k = \langle \hat{a}_k \rangle$
coherent mean field operator

$\delta\hat{a}_k$
quantum fluctuation operator

Periodic squeezing in a polariton Josephson junction



Model: H. Flayac and V. Savona, *PRA* **95**, 043838 (2017)

$$\hat{H} = \sum_{k=L,R} \left[\hbar\omega_c \hat{a}_k^+ \hat{a}_k + U \hat{a}_k^+ \hat{a}_k^+ \hat{a}_k \hat{a}_k \right] - J \left(\hat{a}_L^+ \hat{a}_R + \hat{a}_R^+ \hat{a}_L \right) + \sum_{k=L,R} \left[P_k(t) \hat{a}_k^+ + P_k^*(t) \hat{a}_k \right]$$

Polariton operators: $\hat{a}_k = \alpha_k + \delta\hat{a}_k$

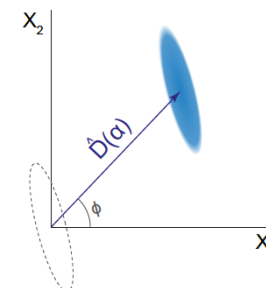
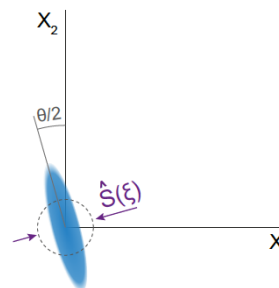
$\alpha_k = \langle \hat{a}_k \rangle$
coherent mean field operator

$\delta\hat{a}_k$
quantum fluctuation operator

$$\Rightarrow g^{(2)}(0) \Rightarrow \cos(\theta - 2\varphi)$$

Squeezing operator $\rightarrow \hat{S} = \exp[\xi^* \hat{a}^2 - \xi \hat{a}^{+2}]$

Squeezed coherent state $\rightarrow |\xi, \alpha\rangle = \hat{S}|\alpha\rangle$

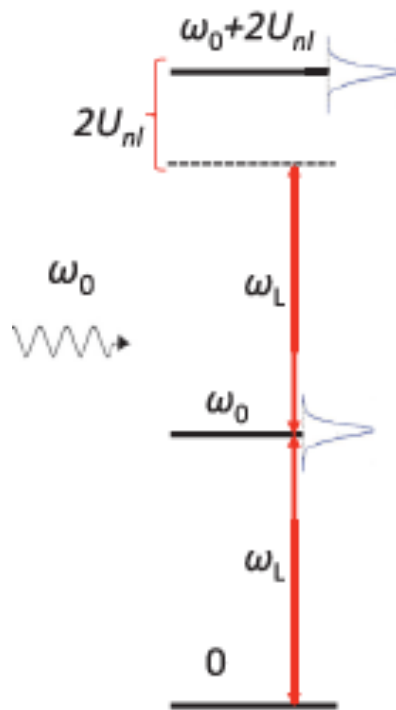


Squeezing
 $\rightarrow \xi = r e^{i\theta}$

Displacement
 $\rightarrow \alpha = \bar{\alpha} e^{i\varphi}$

Polariton quantum blockade

Towards polariton quantum blockade



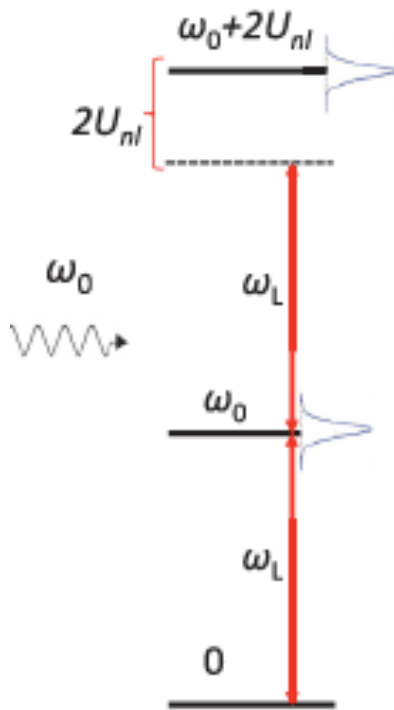
Strong nonlinearity $U_{nl} > \gamma$

The two-polariton state is shifted by $2U_{nl} > 2\gamma$

The presence of a single polariton in the cavity is able to block the entrance of the second one

Polariton quantum blockade

Towards polariton quantum blockade



Strong nonlinearity $U_{nl} > \gamma$

The two-polariton state is shifted by $2U_{nl} > 2\gamma$

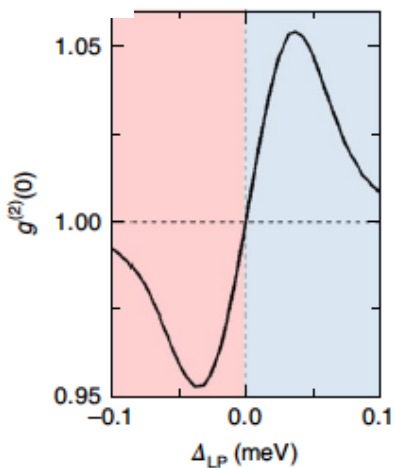
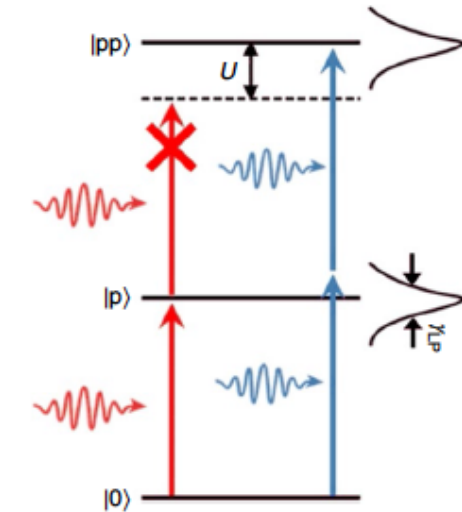
The presence of a single polariton in the cavity is able to block the entrance of the second one

$$U_{nl} \cong \frac{3(\hbar\omega_0)^2}{4\epsilon_0 V_{eff}} \frac{\chi^{(3)}}{\epsilon_r^2}$$

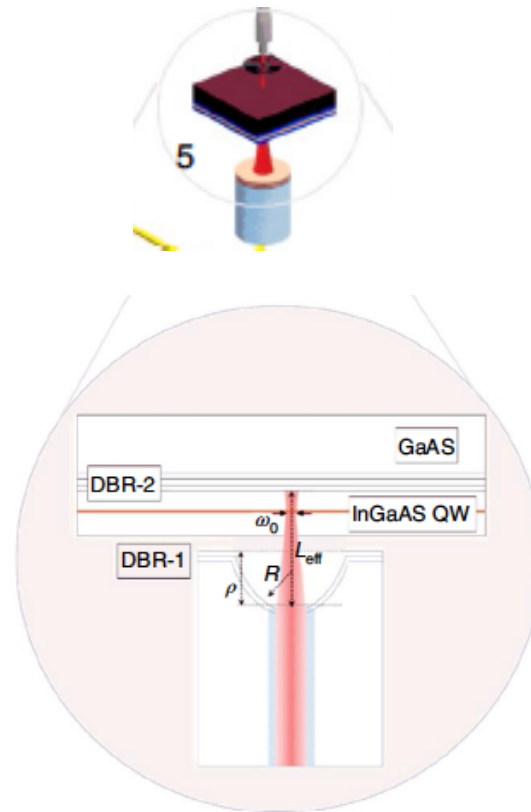
$$g^2(0) = \frac{\langle c^+ c^+ c c \rangle}{\langle c^+ c \rangle^2} = \frac{1}{(1 + 4(U/\gamma)^2)}$$

Polariton quantum blockade

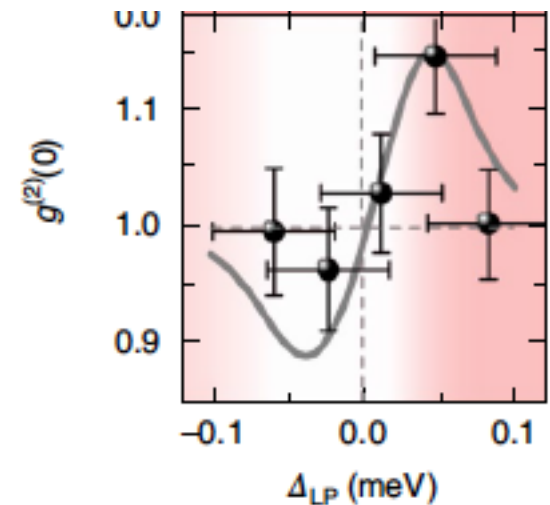
The Experiment



Fibre microcavity

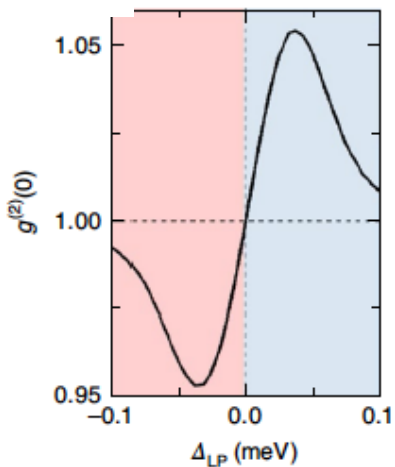
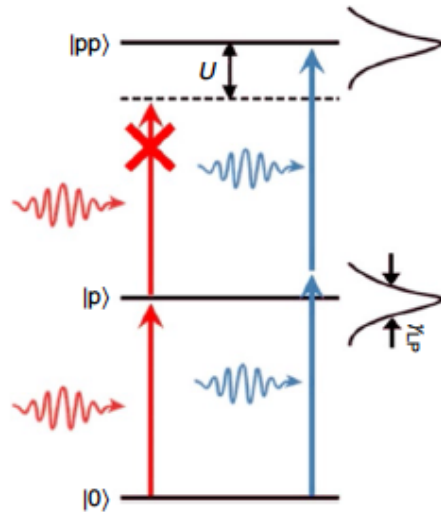


$$r=1.17\mu\text{m}$$

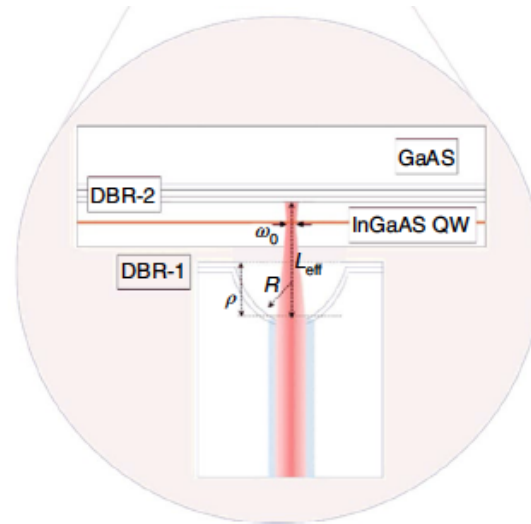
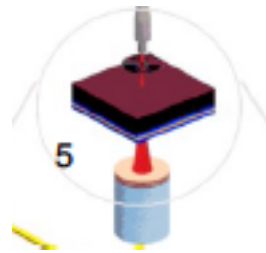


Polariton quantum blockade

The Experiment

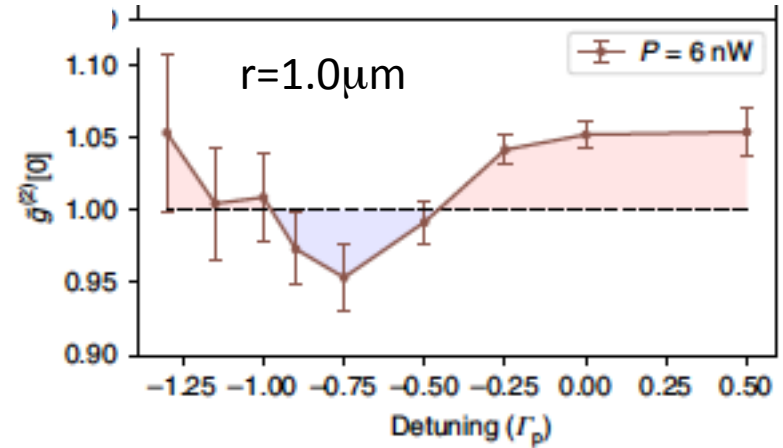


Fibre microcavity

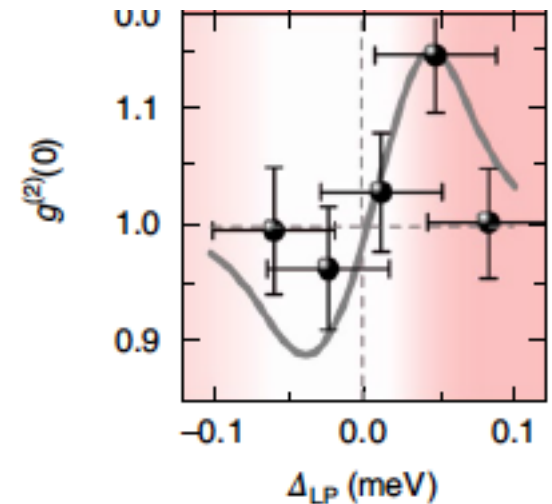


$r=1.17\mu\text{m}$

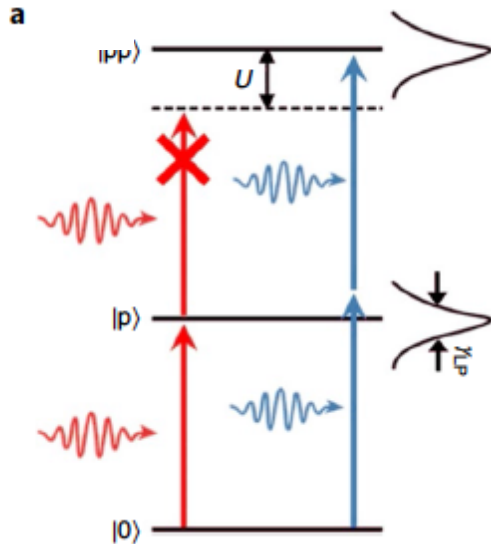
G. Munoz-Matutano et al, Nat. Mat. 18, 21



A. Delteil et al, Nat. Mat. 18, 219 (2019)



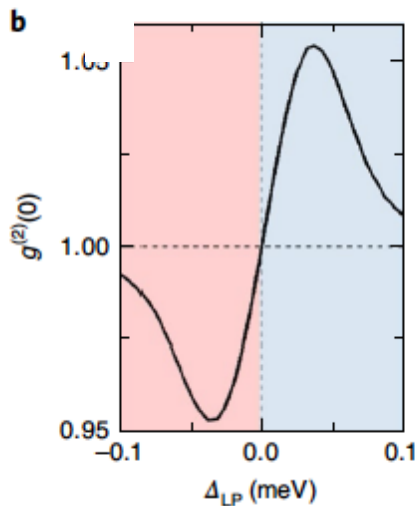
Polariton quantum blockade



Sample with smaller diameter:

⇒ smaller volume

⇒ stronger interaction



$$U \cong \frac{3(\hbar\omega_0)^2}{4\epsilon_0 V_{eff}} \frac{\chi^{(3)}}{\epsilon_r^2}$$

$$g^{(2)}(0) = \frac{1}{(1 + 4(U/\gamma)^2)}$$

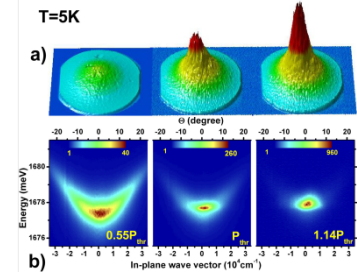
Many facets of Polaritons

$$| \text{polariton} \rangle = Ux | \text{exciton} \rangle + Uc | \text{photon} \rangle$$

- Light effective mass – photonic component
- Nonlinear interaction – excitonic component
- Spin-dependent interaction

Bose-Einstein condensation

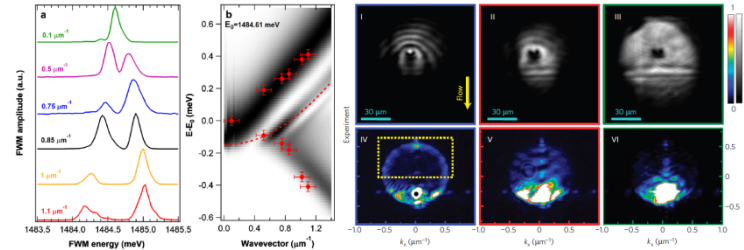
J. Kasprzak *et al.*, Nature (London) **443**, 409 (2006).



Superfluidity

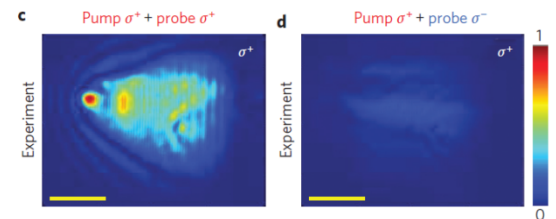
A. Amo *et al.*, Nature Phys. **5**, 805 (2009).

V. Kohnle *et al.*, Phys. Rev. Lett. **106**, 255302 (2011).



Spin switching

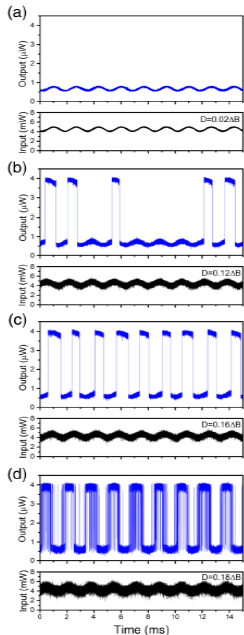
A. Amo *et al.*, Nature Photon. **4**, 361 (2010).



Stochastic resonance and Spinor Stochastic resonance

H. Abbaspour *et al.*, Phys. Rev. Lett. **113**, 057401 (2014).

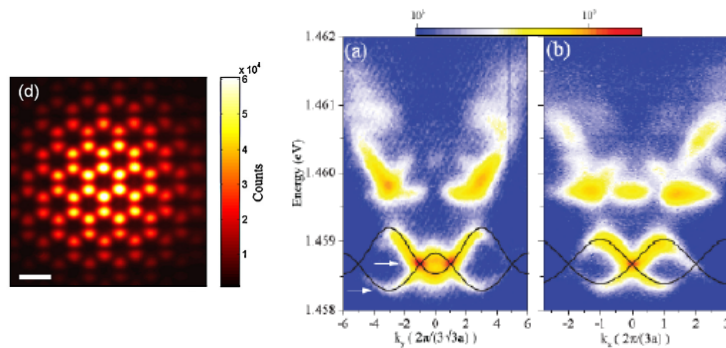
H. Abbaspour *et al.*, Phys. Rev. B **91**, 155307 (2015).



Polariton lattices

T. Jacqmin *et al.*, Phys. Rev. Lett. **112**, 116402 (2015)

C. Ouellet-Plamondon, Thèse 7603 EPFL



Many facets of Polaritons

● Feshbach resonances

Morteza Navadeh Toupchi
Naotomo Takemura
Stéphane Trebaol
Mitchell Anderson

● Bistability

Roland Cerna
Hadis Abbaspour
Claudéric Ouellet-Plamondon
Stéphane Trebaol
Grégory Sallen

● Superfluidity

Verena Kohnle
Yoan Léger

● Polariton squeezing in JJ

Albert Adiyatullin
Mitchell Anderson

● Samples

François Morier-Genoud

Fauzia Jabeen

Claudéric Ouellet-Plamondon

Grégory Sallen

Morteza Navadeh Toupchi

Albert Adiyatullin

● Daniel Oberli

● Benoît Deveaud